Architecture 324 Structures II

Composite Sections (Steel Beam + Slab)

- Composite Sections by LRFD
- · Analysis Methods



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Composite Design

Steel W section with concrete slab "attached" by shear studs.

The concrete slab acts as a wider and thicker com<u>pre</u>ssion flange.

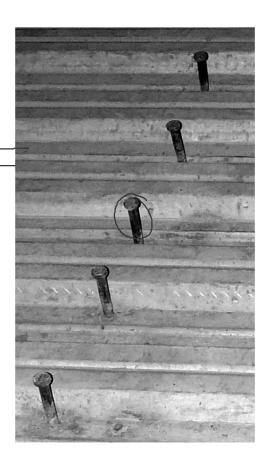
Strength increase by 33% to 50%

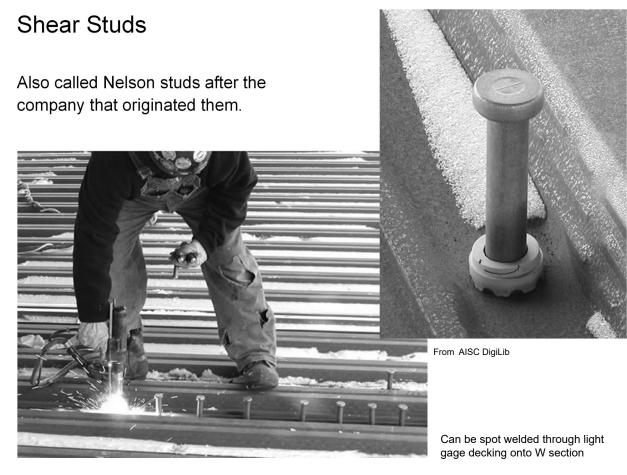
Deflection reduced by 70% to 80%

Can attain either longer spans or smaller members – more economical in long spans

Smaller floor depth, therefore reduced overall building heights and weights

Reduced <u>DL</u> of system, reduction of other material vertically (façade, walls, plumbing, wiring, etc.)





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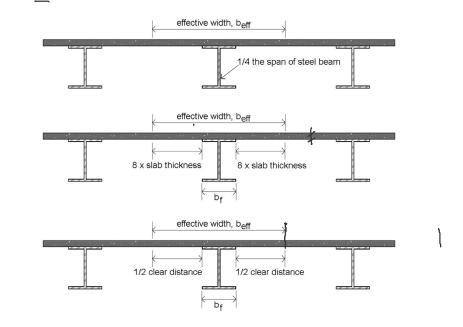
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Effective Flange Width, b_e Slab on both sides:

b_e is the **least** total width :

- Total width: ¼ of the beam span
- Overhang: 8 x slab thickness
- Overhang: $\widehat{1/2}$ the clear distance to next beam (i.e. b_e is the web on center spacing)

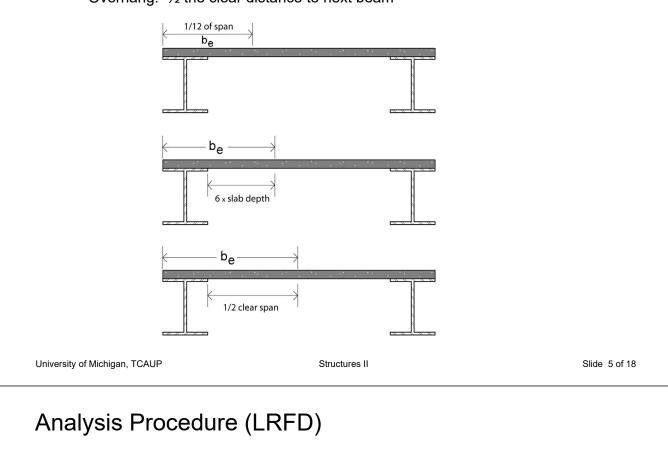


Effective Flange Width, b_e

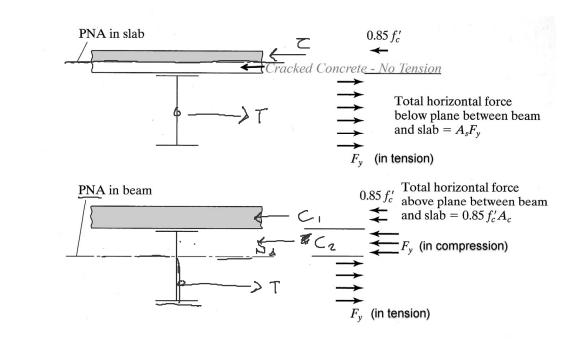
Slab on one side:

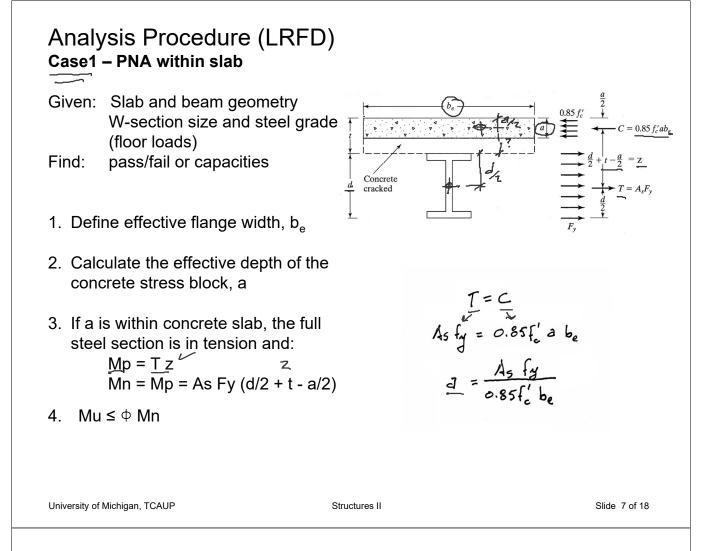
 $\overline{b_e}$ is the **least** total width (i.e. overhang + steel flange) :

- Total width: 1/12 of the beam span
- Overhang: 6 x slab thickness
- Overhang: $\frac{1}{2}$ the clear distance to next beam



Case 1 – Plastic Neutral Axis (PNA) within slab Case 2 – PNA within steel section





Non-composite vs. Composite Sections

Given:

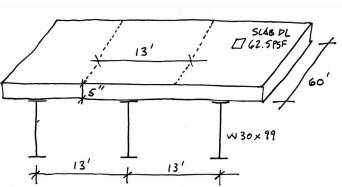
- DL_{slab} = 62.5 psf
- DL_{beam} = 99 plf
- LL = ?
- W 30x99
- F_v = 50 ksi
- f'c _{conc} = 4 ksi

For this example, floor capacity is found for two different floor systems:

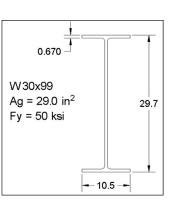
1. Find capacity of steel section independent from slab

VS.

2. Find capacity of steel and slab as a composite section



WEIGHT of SLAB <u>5</u>" 150 PCF = 62.5 PSF 12 13' × 62.5 PSF = 612.5 PLF



Part 1 Non-composite Capacity Analysis (steel beam alone - LRFD)

Given:

- DL_{slab} = 62.5 psf
- DL_{beam} = 99 plf
- W 30x99
- 1. Find section modulus, Z_x in the steel W-section chart.
- 2. Calculate Mn = Fy Zx.
- 4. Find wu from moment equation
- 5. Subtract the DL to find the remaining LL.
- 6. Calculate LL capacity in PSF.

WEIGHT of SLAB <u>5</u>" 150 PCF = 62.5 PSF 12 13' × 62.5 PSF = 812.5 PLF

$$\frac{130 \times 99}{M_{h}} = F_{y} Z_{x} = \frac{312}{50} \ln^{2}$$

$$\frac{15600}{M_{h}} = F_{y} Z_{x} = \frac{50(312)}{K_{SI}} = \frac{15600}{1300} - K$$

$$\frac{1300}{K} - K$$

$$\frac{170}{K} = \frac{1170}{K} + \frac{170}{K} + \frac{$$

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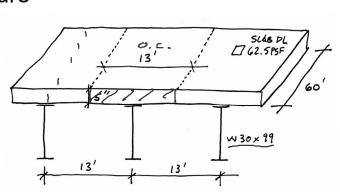
Composite Analysis Procedure

(Case1 - PNA within slab)

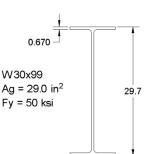
Given: Slab and beam geometry W-section size and steel grade (floor loads)

Find: pass/fail or capacities

- 1. Determine effective flange width, b_e
- 2. Calculate the effective depth of the concrete stress block, a
- If a is within concrete slab, the full steel section is in tension and:
 Mn = Mp = As Fy (d/2 + t a/2)
- 5. Use Mu to calculate factored loads with appropriate beam moment equation.



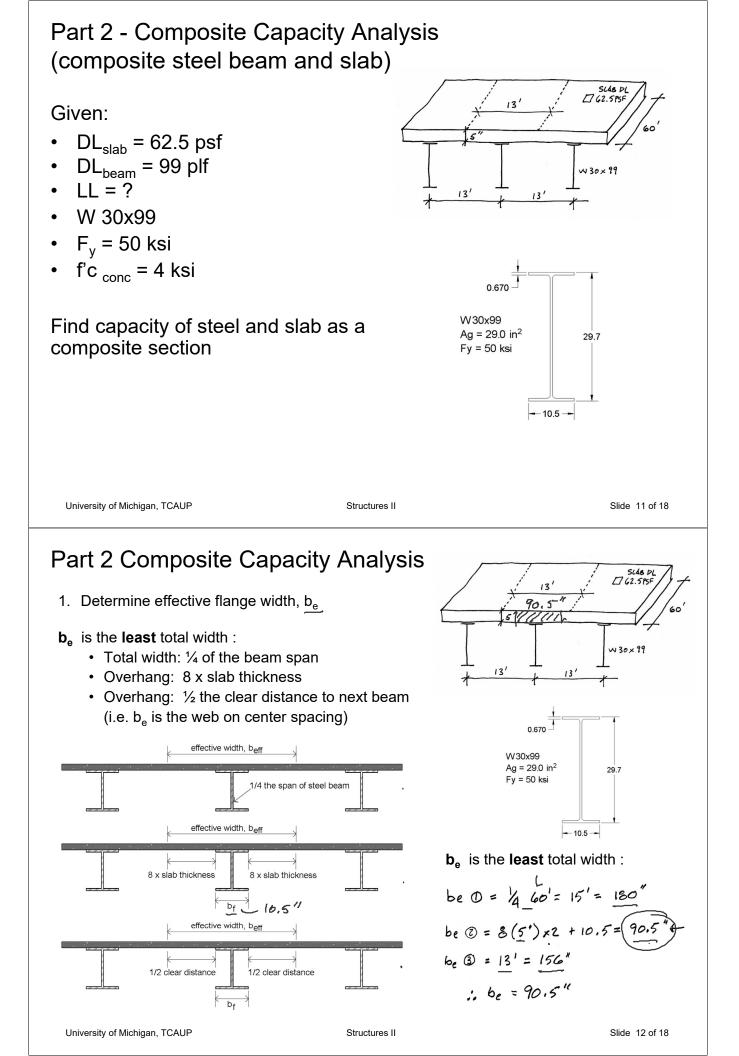
WEIGHT of SLAB <u>5</u>" 150 PCF = 62.5 PSF 12 13' × 62.5 PSF = 812.5 PLF



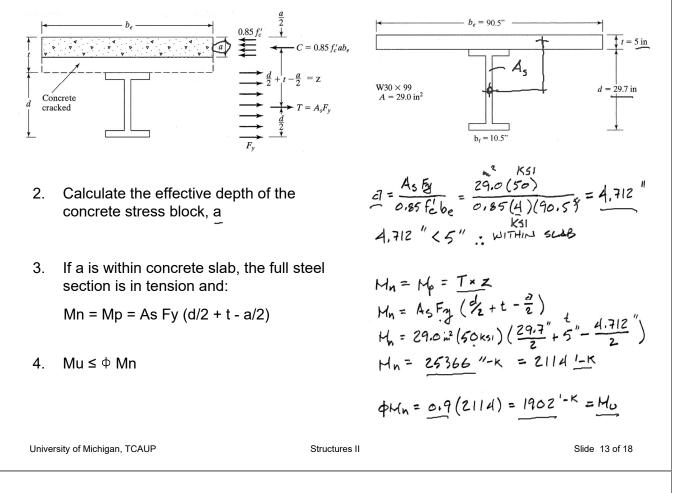
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Part 2 - Composite Capacity Analysis cont.



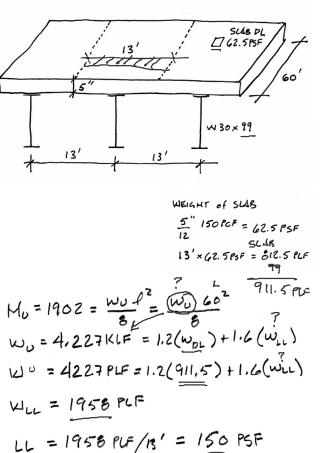
Composite Analysis cont.

- 5. Find total factored w_u .
- 6. Subtract the factored w_{DL} to find w_{LL}
- Calculate the LL in PSF based on the w_{LL}.

Conclusion:

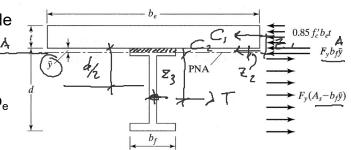
Non-composite LL = 72.4 PSF

Composite LL = 150 PSF



Composite Analysis Procedure (Case 2 – **PNA within W-section**)

- Find: pass/fail or capacities
- 1. Determine effective flange width, b_e
- 2. Calculate the effective depth of the concrete stress block, a.



3. If a is within steel section, the part below the Plastic Neutral Axis (PNA) is in tension and everything above the PNA is in compression (the steel and the concrete)

~?

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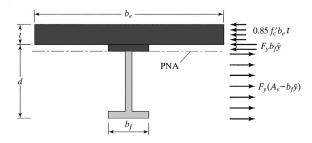
- 4. Check if PNA falls within flange or web of the W-section
- 5. Find \bar{y} by equating T = C

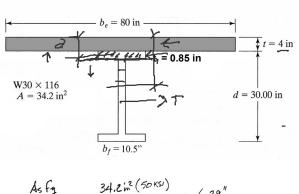
6. Mn = Mp =
$$C_1(z_1) + C_2(z_2) + T(z_3)$$

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Composite Analysis Procedure (Case 2 – PNA within W-section)

- **Given:** Slab and beam geometry W-section size and steel grade (floor loads)
- Find: pass/fail or capacities
- 1. Determine effective flange width, b_e
- 2. Calculate the effective depth of the concrete stress block, a.
- Check if PNA is within upper flange. Assume PNA is at top of web. Check C and T. If C is greater than T, then PNA is within the top flange.





$$\frac{\partial}{\partial e^{2}} = \frac{A_{s} F_{1}}{\partial e^{3}} = \frac{54.2 \text{ m}^{(1)}(20.27)}{\partial e^{3}} = \frac{6.27}{2},$$

$$\frac{6.29'' > 4}{2} :: Becon scale}{2}$$

$$C_{1} = 0.85 f'_{c} b_{c} t FULL SLAB$$

$$C_{1} = 0.85 (4 \text{ ks} \text{ i})(80'')(4'') = 1088 \text{ k} + 146.25^{\text{K}}$$

$$C_{2} = F_{N} b_{f} t_{f} = 50 \text{ ks} \text{ i} (10.5'')(0.85'') = 446.25^{\text{K}}$$

$$C = C_{1} + C_{2} = 1088^{\text{K}} + 446.25^{\text{K}} = (1534)^{\text{K}}$$

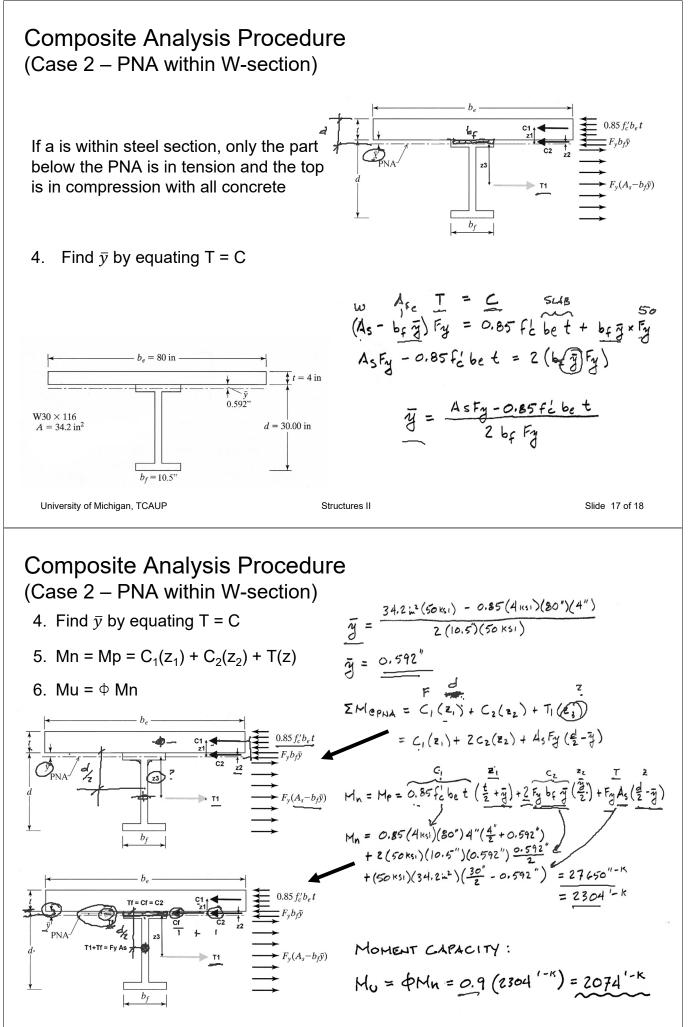
$$T = F_{N} (A_{5} - b_{f} t_{f}) = 50 (34.2 - 8.925) = 1263.7^{\text{K}}$$

$$\Sigma F_{u} = 0 = T - C \quad \text{;} T = C$$

Since horizontal forces should sum to zero, T should equal C. So C should be less than 1534 and T greater than 1263. Therefore, the PNA must be higher and within the flange.

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