Wood Columns

- Failure Modes
- Euler Equation
- End Conditions and Lateral Bracing
- Analysis of Wood Columns
- Design of Wood Columns

Solemar, Bad Dürrheim
Klaus Linkwitz, 1987

Failure Modes

FLEXURE

AXIAL

Strength

$$f_b = \frac{Mc}{I} \qquad f_v = \frac{VQ}{Ib}$$

$$f_c = \frac{P}{A}$$

Stability

$$C_L = \frac{1+\left(F_{bE}/F_b^*\right)}{1.9} - \sqrt{\left[\frac{1+\left(F_{bE}/F_b^*\right)}{1.9}\right]^2 - \frac{F_{bE}/F_b^*}{0.95}}$$

$$C_P = \frac{1+\left(F_{cE}/F_c^*\right)}{2c} - \sqrt{\left[\frac{1+\left(F_{cE}/F_c^*\right)}{2c}\right]^2 - \frac{F_{cE}/F_c^*}{c}}$$

Serviceability

Deflection

Bearing (crushing limit)

Leonhard Euler (1707 – 1783)

Euler Buckling (elastic buckling)

FORCE

$$P_{cr} = \frac{\pi^2 AE}{\left(\frac{KL}{r}\right)^2} = \frac{\pi^2 IE}{(KL)^2}$$

SLENDERNESS $\frac{d}{r}$

$$r = \sqrt{\frac{I}{A}}$$

$$I = Ar^2$$

- A = Cross sectional area (in²)
- E = Modulus of elasticity of the material (lb/in²)
- K = Stiffness (curvature mode) factor
- L = Column length between pinned ends (in.)
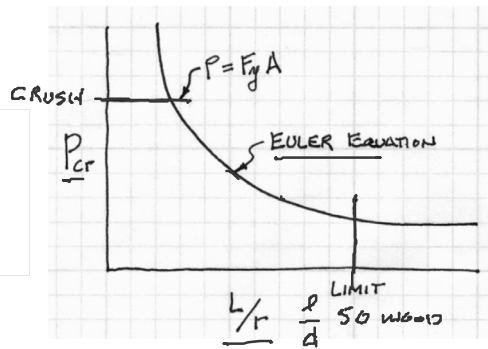- r = radius of gyration (in.)

portrait by Emanuel Handmann,1753

STRESS

$$f_{cr} = \frac{\pi^2 E}{\left(\frac{KL}{r}\right)^2}$$

$\frac{d}{\sqrt{12}}$

RECTANGLE

$$F_{cE} = \frac{0.822 \; E'_{min}}{\left(\frac{le}{d}\right)^2}$$

CRUSH $P = F_y A$

P_{cr} EULER EQUATION

L/r $\frac{\ell}{d}$ LIMIT 50 WOOD
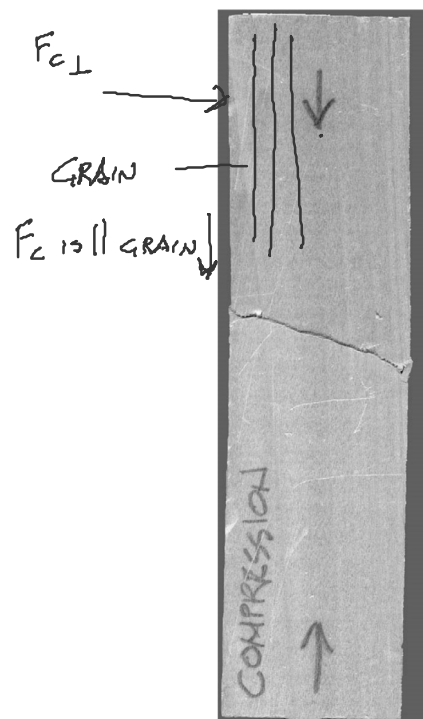

Failure Mode - Strength

Short Columns – fail by crushing

$$f_c = \frac{P}{A} \le F_c$$ NDS

$$A = \frac{P}{F_c}$$

- f_c = Actual compressive stress
- A = Cross-sectional area of column (in²)
- P = Load on the column
- F_c = Allowable compressive stress per codes

$F_{c\perp}$

GRAIN

F_c is || GRAIN

COMPRESSION

Failure Modes – Stability

Long Columns – fail by buckling

Traditional Euler

$$f_{cr} = \frac{\pi^2 E}{\left(\frac{KL}{r}\right)^2}$$

NDS Equation

$$F_{cE} = \frac{0.822 E'_{min}}{\left(\frac{l_e}{d}\right)^2}$$

- E = Modulus of elasticity of the column material (psi)
- K = Stiffness (curvature mode) factor
- L = Column length between ends (inches)
- r = radius of gyration = $\sqrt{I/A}$ (inches)

- E'min = reduced E modulus (psi)
- le = Ke l$_u$ (inches)
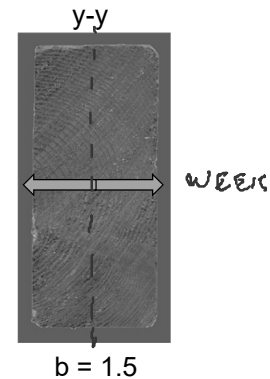- d (inches)
- 0.822 = $\pi^2/12$
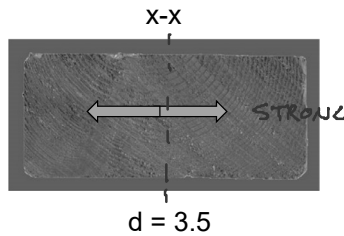
$$r = d/\sqrt{12}$$

Slenderness Ratio le/d

Slenderness Ratios:

The larger ratio will govern.
Try to balance for efficiency.

Slenderness Limited to < 50

y-y

x-x

STRONG

WEEK

d = 3.5

b = 1.5

X- X
Ke = 1.0
le = 1.0 (96)

$$\frac{le}{d} = \frac{96}{3.5} = 27.4$$

Y- Y
Ke = 1.0
le = 1.0 (96)

$$\frac{le}{b} = \frac{96}{1.5} = 64$$

48

$$\frac{48}{1.5} = 32$$

8'
96"

48"

48
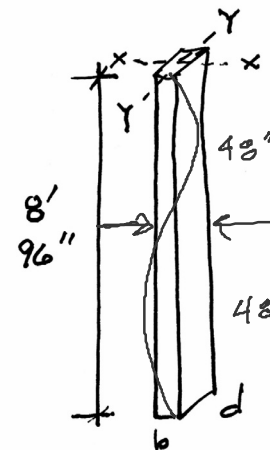
End Support Conditions

K_e is a constant based on the end conditions
ℓ is the actual length
ℓ_e is the effective length (curved part)

$$\ell_e = K_e \ell$$

use these ➡

Table G1   Buckling Length Coefficients, K_e

Buckling modes						
Theoretical K_e value	0.5	0.7	1.0	1.0	2.0	2.0
Recommended design K_e when ideal conditions approximated	0.65	0.80	1.2	1.0	2.10	2.4
End condition code		Rotation fixed, translation fixed				
		Rotation free, translation fixed				
		Rotation fixed, translation free				
		Rotation free, translation free				

Allowable Flexure Stress F_c'

F_c from tables determined by species and grade

$F_c' = F_c$ (adjustment factors)

Actual Flexure Stress f_b

$$f_c = P/A$$

$$\mathbf{F_c' \geq f_c}$$

Table 4A (Cont.)   Base Design Values for Visually Graded Dimension Lumber (2"-4" thick)[1,2]

(All species except Southern Pine — see Table 4B) (Tabulated design values are for normal load duration and dry service conditions. See NDS 4.3 for a comprehensive description of design value adjustment factors.)

USE WITH TABLE 4A ADJUSTMENT FACTORS

Species and commercial grade	Size classification	Design values in pounds per square inch (psi)						Grading Rules Agency
		Bending F_b	Tension parallel to grain F_t	Shear parallel to grain F_v	Compression perpendicular to grain $F_{c\perp}$	Compression parallel to grain F_c	Modulus of Elasticity E	
EASTERN HEMLOCK-BALSAM FIR								
Select Structural		1250	575	140	335	1200	1,200,000	
No.1		775	350	140	335	1000	1,100,000	
No.2	2" & wider	575	275	140	335	825	1,100,000	
No.3		350	150	140	335	475	900,000	NELMA
Stud	2" & wider	450	200	140	335	525	900,000	NSLB
Construction		675	300	140	335	1050	1,000,000	
Standard	2"-4" wide	375	175	140	335	850	900,000	
Utility		175	75	140	335	550	800,000	

Adjustment Factors

Table 4.3.1   Applicability of Adjustment Factors for Sawn Lumber

	ASD only	ASD and LRFD										LRFD only		
	Load Duration Factor	Wet Service Factor	Temperature Factor	Beam Stability Factor	Size Factor	Flat Use Factor	Incising Factor	Repetitive Member Factor	Column Stability Factor	Buckling Stiffness Factor	Bearing Area Factor	Format Conversion Factor K_F	Resistance Factor ϕ	Time Effect Factor
$F_b' = F_b$ x	C_D	C_M	C_t	C_L	C_F	C_{fu}	C_i	C_r	-	-	-	2.54	0.85	λ
$F_t' = F_t$ x	C_D	C_M	C_t	-	C_F	-	C_i	-	-	-	-	2.70	0.80	λ
$F_v' = F_v$ x	C_D	C_M	C_t	-	-	-	C_i	-	-	-	-	2.88	0.75	λ
$F_c' = F_c$ x	C_D	C_M	C_t	-	C_F	✗	C_i	✗	$\boxed{C_P}$	-	-	2.40	0.90	λ
$F_{c\perp}' = F_{c\perp}$ x	-	C_M	C_t	-	-	-	C_i	-	-	-	C_b	1.67	0.90	-
$E' = E$ x	-	C_M	C_t	-	-	-	C_i	-	-	-	-	-	-	-
$E_{min}' = E_{min}$ x	-	C_M	C_t	-	-	-	C_i	-	-	C_T	-	1.76	0.85	-

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Allowable Flexure Stress F_c'

F_c from tables determined by species and grade

$F_c' = F_c (C_D\ C_M\ C_t\ C_F\ C_i\ C_P)$

Adjustment factors for compression:
- C_D Load Duration Factor
- C_t Temperature Factor

Table 2.3.2 Frequently Used Load Duration Factors, C_D[1]

Load Duration	C_D	Typical Design Loads
Permanent	0.9	Dead Load
Ten years	1.0	Occupancy Live Load
Two months	1.15	Snow Load
Seven days	1.25	Construction Load
Ten minutes	1.6	Wind/Earthquake Load
Impact[2]	2.0	Impact Load

(1) Actual stress due to (DL) ≤ (0.9) (Design value)
(2) Actual stress due to (DL+LL) ≤ (1.0) (Design value)
(3) Actual stress due to (DL+WL) ≤ (1.6) (Design value)
(4) Actual stress due to (DL+LL+SL) ≤ (1.15) (Design value)
(5) Actual stress due to (DL+LL+WL) ≤ (1.6) (Design value)
(6) Actual stress due to (DL+SL+WL) ≤ (1.6) (Design value)
(7) Actual stress due to (DL+LL+SL+WL) ≤ (1.6) (Design value)

Table 2.3.3   Temperature Factor, C_t

Reference Design Values	In-Service Moisture Conditions[1]	C_t		
		T≤100°F	100°F<T≤125°F	125°F<T≤150°F
F_t, E, E_{min}	Wet or Dry	1.0	0.9	0.9
F_b, F_v, F_c, and $F_{c\perp}$	Dry	1.0	0.8	0.7
	Wet	1.0	0.7	0.5

1. Wet and dry service conditions for sawn lumber, structural glued laminated timber, prefabricated wood I-joists, structural composite lumber, wood structural panels and cross-laminated timber are specified in 4.1.4, 5.1.4, 7.1.4, 8.1.4, 9.3.3, and 10.1.5 respectively.

Allowable Flexure Stress F_c' (For **Dimensioned Lumber**)

F_c from tables determined by species and grade

$F_c' = F_c (C_D \ C_M \ C_t \ C_F \ C_i \ C_P)$

Adjustment factors for compression:
    C_M Moisture Factor
    C_F Size Factor

Wet Service Factor, C_M

When dimension lumber is used where moisture content will exceed 19% for an extended time period, design values shall be multiplied by the appropriate wet service factors from the following table:

Wet Service Factors, C_M

F_b	F_t	F_v	$F_{c\perp}$	F_c	E and E_{min}
0.85*	1.0	0.97	0.67	0.8**	0.9

* when $(F_b)(C_F) \leq 1{,}150$ psi, $C_M = 1.0$
** when $(F_c)(C_F) \leq 750$ psi, $C_M = 1.0$

Size Factors, C_F

Grades	Width (depth)	F_b Thickness (breadth) 2" & 3"	F_b Thickness (breadth) 4"	F_t	F_c
Select Structural, No.1 & Btr, No.1, No.2, No.3	2", 3", & 4"	1.5	1.5	1.5	1.15
	5"	1.4	1.4	1.4	1.1
	6"	1.3	1.3	1.3	1.1
	8"	1.2	1.3	1.2	1.05
	10"	1.1	1.2	1.1	1.0
	12"	1.0	1.1	1.0	1.0
	14" & wider	0.9	1.0	0.9	0.9
Stud	2", 3", & 4"	1.1	1.1	1.1	1.05
	5" & 6"	1.0	1.0	1.0	1.0
	8" & wider	Use No.3 Grade tabulated design values and size factors			
Construction, Standard	2", 3", & 4"	1.0	1.0	1.0	1.0
Utility	4"	1.0	1.0	1.0	1.0
	2" & 3"	0.4	—	0.4	0.6

Allowable Flexure Stress F_c' (For **Timbers**)

F_c from tables determined by species and grade

$F_c' = F_c (C_D \ C_M \ C_t \ C_F \ C_i \ C_P)$

Adjustment factors for compression:
    C_M Moisture Factor
    C_F Size Factor

Size Factor, C_F

When visually graded timbers are subjected to loads applied to the narrow face, tabulated design values shall be multiplied by the following size factors:

Size Factors, C_F

Depth	F_b	F_t	F_c
d > 12"	$(12/d)^{1/9}$	1.0	1.0
d ≤ 12"	1.0	1.0	1.0

Wet Service Factor, C_M

When timbers are used where moisture content will exceed 19% for an extended time period, design values shall be multiplied by the appropriate wet service factors from the following table (for Southern Pine and Mixed Southern Pine, use tabulated design values without further adjustment):

Wet Service Factors, C_M

F_b	F_t	F_v	$F_{c\perp}$	F_c	E and E_{min}
1.00	1.00	1.00	0.67	0.91	1.00

Allowable Flexure Stress F_c'

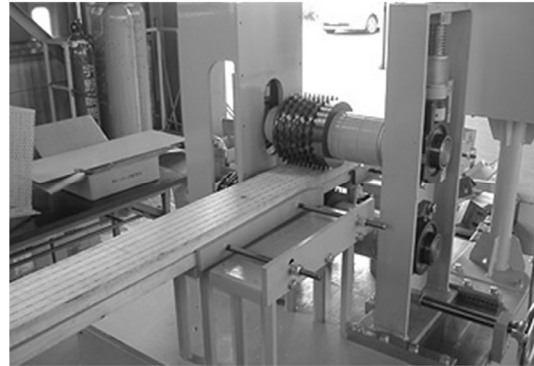F_c from tables determined by species and grade

$F_c' = F_c (C_D\ C_M\ C_t\ C_F\ C_i\ C_P\ )$

Adjustment factors for compression :
      C_i Incising Factor

Table 4.3.8 Incising Factors, C_i

Design Value	C_i
E, E_{min}	0.95
F_b, F_t, F_c, F_v	0.80
$F_{c\perp}$	1.00

Allowable Flexure Stress F_c'

F_c from tables determined by species and grade

$F_c' = F_c (C_D\ C_M\ C_t\ C_F\ C_i\ C_P\ )$

3.7 Solid Columns

## 3.7.1 Column Stability Factor, C_P

3.7.1.1 When a compression member is supported throughout its length to prevent lateral displacement in all directions, $C_P = 1.0$.

3.7.1.2 The effective column length, ℓ_e, for a solid column shall be determined in accordance with principles of engineering mechanics. One method for determining effective column length, when end-fixity conditions are known, is to multiply actual column length by the appropriate effective length factor specified in Appendix G, $\ell_e = (K_e)(\ell)$.

3.7.1.3 For solid columns with rectangular cross section, the slenderness ratio, ℓ_e/d, shall be taken as the larger of the ratios ℓ_{e1}/d_1 or ℓ_{e2}/d_2 (see Figure 3F) where each ratio has been adjusted by the appropriate buckling length coefficient, K_e, from Appendix G.

3.7.1.4 The slenderness ratio for solid columns, ℓ_e/d, shall not exceed 50, except that during construction ℓ_e/d shall not exceed 75.

3.7.1.5 The column stability factor shall be calculated as follows:
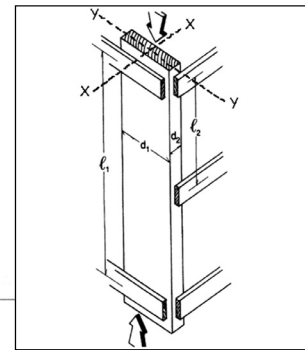
$$C_P = \frac{1 + (F_{cE}/F_c^*)}{2c} - \sqrt{\left[\frac{1 + (F_{cE}/F_c^*)}{2c}\right]^2 - \frac{F_{cE}/F_c^*}{c}} \quad (3.7\text{-}1)$$

where:

F_c^* = reference compression design value parallel to grain multiplied by all applicable adjustment factors except C_P (see 2.3), psi
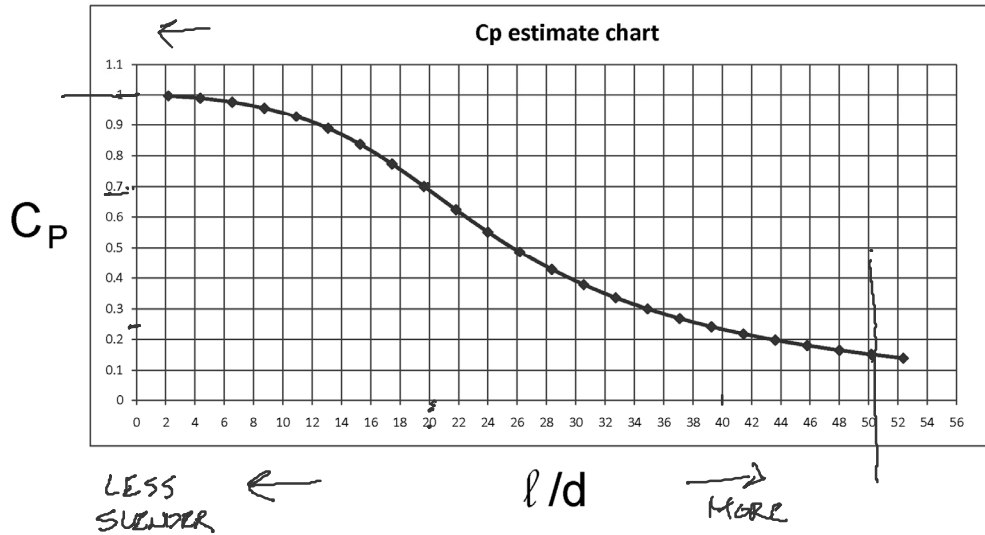
EULER $F_{cE} = \dfrac{0.822\ E_{min}'}{(\ell_e/d)^2}$

c = 0.8 for sawn lumber

c = 0.85 for round timber poles and piles

c = 0.9 for structural glued laminated timber or structural composite lumber

C$_P$

Cp estimate chart

C$_P$

ℓ /d

LESS SLENDER ←

MORE →

Analysis of Wood Columns

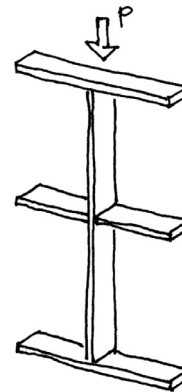## Data:
- Column – <u>size</u>, <u>length</u>
- Support conditions
- <u>Material</u> properties – F$_c$, E
- <u>Load</u>

Required:
- <u>Pass/Fail</u> or margin of safety

1. Calculate slenderness ratio l$_e$/d
   largest ratio governs. Must be < 50

2. Find <u>adjustment</u> factors
   C$_D$ C$_M$ C$_t$ C$_F$ C$_i$

3. Calculate C$_P$

4. Determine <u>F'c</u> by multiplying the tabulated Fc
   by all the above factors   ACTUAL

5. Calculate the actual stress: <u>fc</u> = P/A
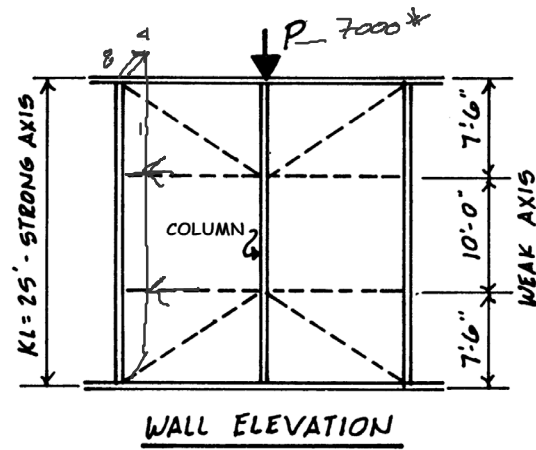6. Compare Allowable and Actual stress.
   <u>F'c > fc</u> passes

Analysis Example:

Data: section 4x8 (nominal)
Douglas Fir-Larch No1
M.C. 15%
P = 7000 LBS (Snow Load)

$C_D = 1.15$

Find: Pass/Fail

From NDS Supplement Table 4A
F_c = 1500 psi
E_{min} = 620000 psi

$C_D = 1.15$ (snow) ✓
$C_M = 1.0$
$C_t = 1.0$
$C_F = 1.05$ (4x8)
$C_i = 1.0$
$C_P = ?$

WALL ELEVATION

Size Factors, C_F

Grades	Width (depth)	F_c
Select Structural, No.1 & Btr, No.1, No.2, No.3	2", 3", & 4"	1.15
	5"	1.1
	6"	1.1
	8"	1.05
	10"	1.0
	12"	1.0
	14" & wider	0.9
Stud	2", 3", & 4"	1.05
	5" & 6"	1.0
	8" & wider	
Construction, Standard	2", 3", & 4"	1.0
Utility	4"	1.0
	2" & 3"	0.6

Allowable Flexure Stress F_c'

F_c from tables determined by species and grade

$$F_c' = F_c (C_D\ C_M\ C_t\ C_F\ C_i\ C_P)$$

Adjustment factors for compression:
C_M Moisture Factor
C_F Size Factor

Wet Service Factor, C_M

When dimension lumber is used where moisture content will exceed 19% for an extended time period, design values shall be multiplied by the appropriate wet service factors from the following table:

Wet Service Factors, C_M

F_b	F_t	F_v	$F_{c\perp}$	F_c	E and E_{min}
0.85*	1.0	0.97	0.67	0.8**	0.9

* when $(F_b)(C_F) \leq 1{,}150$ psi, $C_M = 1.0$
** when $(F_c)(C_F) \leq 750$ psi, $C_M = 1.0$

Size Factors, C_F

Grades	Width (depth)	F_b Thickness (breadth) 2" & 3"	F_b Thickness (breadth) 4"	F_t	F_c
Select Structural, No.1 & Btr, No.1, No.2, No.3	2", 3", & 4"	1.5	1.5	1.5	1.15
	5"	1.4	1.4	1.4	1.1
	6"	1.3	1.3	1.3	1.1
	8"	1.2	1.3	1.2	1.05
	10"	1.1	1.2	1.1	1.0
	12"	1.0	1.1	1.0	1.0
	14" & wider	0.9	1.0	0.9	0.9
Stud	2", 3", & 4"	1.1	1.1	1.1	1.05
	5" & 6"	1.0	1.0	1.0	1.0
	8" & wider	Use No.3 Grade tabulated design values and size factors			
Construction, Standard	2", 3", & 4"	1.0	1.0	1.0	1.0
Utility	4"	1.0	1.0	1.0	1.0
	2" & 3"	0.4	—	0.4	0.6

Analysis Example:

Calculate C_P

$$C_p = \frac{1+\left(F_{cE}/F_c^*\right)}{2c} - \sqrt{\left[\frac{1+\left(F_{cE}/F_c^*\right)}{2c}\right]^2 - \frac{F_{cE}/F_c^*}{c}} \quad (3.7\text{-}1)$$

where:

F_c^* = reference compression design value paral-
lel to grain multiplied by all applicable ad-
justment factors except C_p (see 2.3), psi

$$F_{cE} = \frac{0.822\, E_{min}'}{\left(\ell_e/d\right)^2}$$

c = 0.8 for sawn lumber

c = 0.85 for round timber poles and piles

c = 0.9 for structural glued laminated timber or
structural composite lumber

WALL ELEVATION

$$x-x$$
$$\ell e_x = 25' = 300''$$
$$\ell ex/d_1 = \frac{300''}{7.25''}$$
$$= 41.4$$

$$Y-Y$$
$$\ell e_y = 10' = 120''$$
$$\ell ey/d_2 = \frac{120}{3.5''}$$
$$= 34.3$$

$$\ell e/d = 41.4 < 50 \checkmark$$

Analysis Example:

Calculate C_P

$$C_p = \frac{1+\left(F_{cE}/F_c^*\right)}{2c} - \sqrt{\left[\frac{1+\left(F_{cE}/F_c^*\right)}{2c}\right]^2 - \frac{F_{cE}/F_c^*}{c}} \quad (3.7\text{-}1)$$

where:

F_c^* = reference compression design value paral-
lel to grain multiplied by all applicable ad-
justment factors except C_p (see 2.3), psi

$$F_{cE} = \frac{0.822\, E_{min}'}{\left(\ell_e/d\right)^2}$$

c = 0.8 for sawn lumber

c = 0.85 for round timber poles and piles

c = 0.9 for structural glued laminated timber or
structural composite lumber

$$F_{cE} = \frac{0.822\, E'_{min}}{(\ell e/d)^2}$$

$$= \frac{0.822(620000)}{(41.4)^2}$$

$$= 297.6 \text{ psi}$$

$$F_c^* = 1500\left(\overset{C_D}{1.15}\ \overset{C_F}{1.05}\right)$$

$$= 1811.25 \text{ psi}$$

$$F_{cE}/F_c^* = \frac{297.6}{1811.25} = 0.164$$

$$c = 0.8$$

Analysis Example:

Calculate C_P

$$C_p = \frac{1+\left(F_{cE}/F_c^*\right)}{2c} - \sqrt{\left[\frac{1+\left(F_{cE}/F_c^*\right)}{2c}\right]^2 - \frac{F_{cE}/F_c^*}{c}} \quad (3.7\text{-}1)$$

where:

F_c^* = reference compression design value parallel to grain multiplied by all applicable adjustment factors except C_p (see 2.3), psi

$$F_{cE} = \frac{0.822\,E_{min}'}{(\ell_e/d)^2}$$

$c = 0.8$ for sawn lumber

$c = 0.85$ for round timber poles and piles

$c = 0.9$ for structural glued laminated timber or structural composite lumber

Compare Allowable and Actual stress
    F'c > fc passes

$$C_p = \frac{1+0.164}{2(0.8)} - \sqrt{\left[\frac{1+0.164}{2(0.8)}\right]^2 - \frac{0.164}{.8}}$$

$$C_p = 0.1584$$

$$F_c' = 1500 \overset{C_D \quad\quad C_F \quad\quad C_p}{(1.15 \quad 1.05 \quad 0.1584\,)}$$

ALLOW.

$$= 286.9 \text{ psi} \quad \longleftarrow$$

OK

$$f_c = \frac{P}{A} = \frac{7000^\#}{25.38\,in^2} = \underset{\text{ACTUAL}}{275.8\,psi}$$

$$F_c' > f_c \quad \checkmark \text{ OK}$$

Capacity Analysis of Columns

Data:
- Column – <u>size</u>, length
- Support conditions
- Material properties – F_c , E

Required:
- Maximum Load Capacity, <u>Pmax</u>

1. Calculate slenderness ratio l_e/d
   largest ratio governs. Must be < 50

2. Find adjustment factors
   $C_D\ C_M\ C_t\ C_F\ C_i$

3. Calculate C_P

4. Determine F'c by multiplying the tabulated Fc
   by all the above factors

5. Set actual stress = allowable, fc = F'c
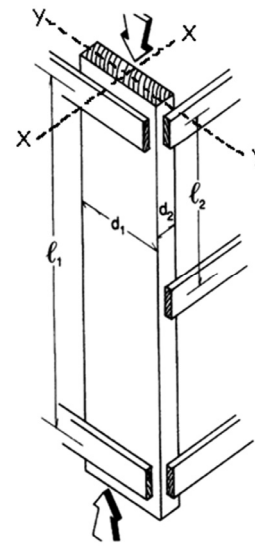6. Find the maximum allowable load
       Pmax = F'c A
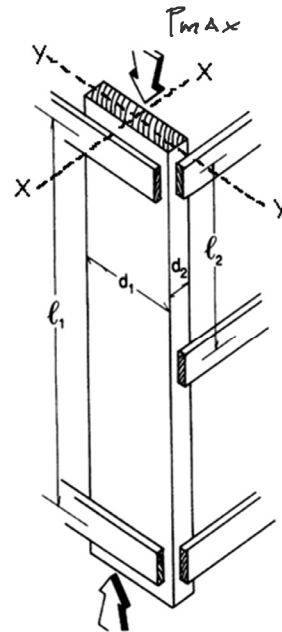
Capacity Example

Data:
- 4x10
- Hem – Fir, No 2   M.C. = 20%
- Wind Load
- L1 = 8'   L2 = 4' K_e=1.0

Required:
- Maximum Load Capacity, Pmax

From NDS Supplement Table 4A
  Fc = 1300 psi
  Emin = 470000 psi

  C_D = 1.6   (Table 2.3.2.)
  C_{Mc} = 0.8 C_{ME} = 0.9
  C_t = 1.0
  C_F = 1.0   (chart in Supplement)
  C_i = 1.0
  C_P = ?

$x - x$

$l_{ex} = 8' = 96"$

$\dfrac{l_{er}}{d_1} = \dfrac{96}{9.25} = 10.4$

$y - y$

$l_{ey} = 4' = 48"$

$\dfrac{l_{ey}}{d_2} = \dfrac{48}{3.5} = 13.7$

$\dfrac{l_e}{d} = 13.7 < 50$ ✓

Allowable Flexure Stress F_c'

4 x 10

F_c from tables determined by species and grade

$F_c' = F_c (C_D\ C_M\ C_t\ C_F\ C_i\ C_P)$

Adjustment factors for compression:
  C_M Moisture Factor
  C_F Size Factor

Wet Service Factor, C_M

When dimension lumber is used where moisture content will exceed 19% for an extended time period, design values shall be multiplied by the appropriate wet service factors from the following table:

Wet Service Factors, C_M

| F_b	F_t	F_v	$F_{c\perp}$	F_c	E and E_{min}
0.85*	1.0	0.97	0.67	0.8**	0.9

* when $(F_b)(C_F) \le 1{,}150$ psi, $C_M = 1.0$
** when $(F_c)(C_F) \le 750$ psi, $C_M = 1.0$

Size Factors, C_F

Grades	Width (depth)	F_b 2" & 3"	F_b 4"	F_t	F_c
		Thickness (breadth)			
Select Structural, No.1 & Btr, No.1, No.2, No.3	2", 3", & 4"	1.5	1.5	1.5	1.15
	5"	1.4	1.4	1.4	1.1
	6"	1.3	1.3	1.3	1.1
	8"	1.2	1.3	1.2	1.05
	10"	1.1	1.2	1.1	1.0
	12"	1.0	1.1	1.0	1.0
	14" & wider	0.9	1.0	0.9	0.9
Stud	2", 3", & 4"	1.1	1.1	1.1	1.05
	5" & 6"	1.0	1.0	1.0	1.0
	8" & wider	Use No.3 Grade tabulated design values and size factors			
Construction, Standard	2", 3", & 4"	1.0	1.0	1.0	1.0
Utility	4"	1.0	1.0	1.0	1.0
	2" & 3"	0.4	—	0.4	0.6

Capacity Example
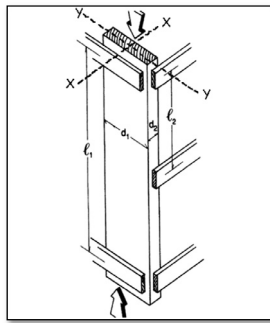
Find C_P

$$F_{CE} = \frac{0.822 \, E'_{min}}{(\ell_e/d)^2}$$

$$= \frac{0.822(470000(0.9))}{13.7^2}$$

$$= 1848.7 \text{ psi}$$

$$F_c^* = 1300(1.6 \quad 0.8)$$

$$= 1664. \text{ psi}$$

$$F_{CE}/F_c^* = \frac{1848.7}{1664.} = 1.111$$

$$C_P = 0.7261$$

$$C_P = \frac{1+\left(F_{cE}/F_c^*\right)}{2c} - \sqrt{\left[\frac{1+\left(F_{cE}/F_c^*\right)}{2c}\right]^2 - \frac{F_{cE}/F_c^*}{c}} \quad (3.7\text{-}1)$$

where:

F_c^* = reference compression design value parallel to grain multiplied by all applicable adjustment factors except C_p (see 2.3), psi

$$F_{cE} = \frac{0.822 \, E_{min}'}{(\ell_e/d)^2}$$

c = 0.8 for sawn lumber

c = 0.85 for round timber poles and piles

c = 0.9 for structural glued laminated timber or structural composite lumber

Find the maximum load, Pmax

$$F_c' = 1300(1.6 \quad 0.8 \quad 0.7261)$$

$$= 1208 \text{ psi}$$

$$P_{max} = F_c' \, A = 1208(32.38) = 39\,115 \, \#$$
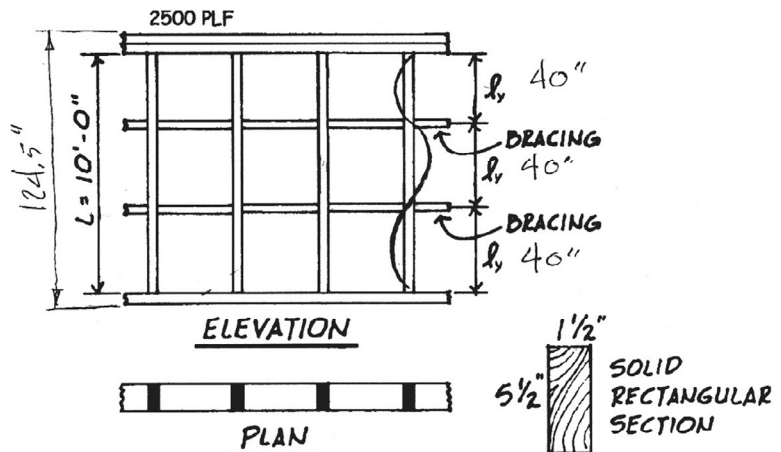

Stud Wall Example

Data:
- 2x6
- S-P-F, Stud   M.C. = 12%
- D+L Load = 2500 PLF
- Braced as shown K_e=1.0

Required:
- o.c. spacing

From NDS Supplement Table 4A
    Fc = 725 psi
    Emin = 440000 psi

    C_D = 1.0 (LL)
    C_{Mc} = 1.0 C_{ME} = 1.0
    C_t = 1.0
    C_F = 1.0 (stud)
    C_i = 1.0
    C_P = ?

Stud Wall Example

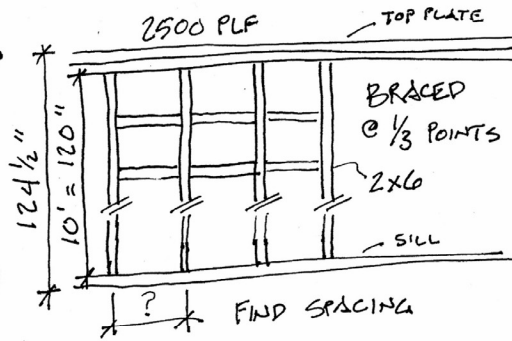

STUD WALL

S-P-F STUD GRADE

$F_c = 725 \text{ psi}$

$E_{min} = 440,000 \text{ psi}$

$C_D = 1 \quad C_M = 1 \quad C_p = 1.0$

2500 PLF — TOP PLATE

$124\frac{1}{2}''$ $10' = 120''$

BRACED @ $\frac{1}{3}$ POINTS

2x6

SILL

? FIND SPACING

X-X
$\ell_{e_x} = 124.5''$

$\ell_e/d = \dfrac{124.5}{5.5} = 22.6$

124.5*

Y-Y
$\ell_{e_y} = 40''$

$\ell_e/d = \dfrac{40}{1.5} = 26.7$

40"

CONTROLLING $\ell_e/d = \underline{26.7}$

Stud Wall Example

C_p

X-X
$\ell_{e_x} = 124.5''$

$\ell_e/d = \dfrac{124.5}{5.5} = 22.6$

124.5*

Y-Y
$\ell_{e_y} = 40''$

$\ell_e/d = \dfrac{40}{1.5} = 26.7$

40"

CONTROLLING $\ell_e/d = \underline{26.7}$

$$F_{CE} = \frac{0.822\, E_{min}'}{\left(\ell_e/d\right)^2} = \frac{0.822(440\,000)}{26.7^2} = 508.6$$

$$F_c^* = 725(1 \times 1 \times 1) = 725 \text{ psi}$$

$$\frac{F_{CE}}{F_c^*} = \frac{508.6}{725} = 0.702$$

NDS eq. 3.7-1 $\rightarrow$ $C_p = \underline{0.559}$

Stud Wall Example

Find max allowable stress, F'c

$$F'_c = 725 \, (0.559) = \boxed{405.6 \text{ psi}}$$
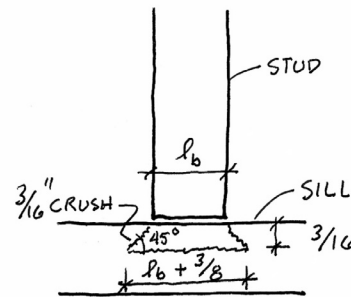
Calculate max load per stud

$$P = F'_c \, A = 405.6 \text{ psi} \times 8.25 \text{ in}^2$$
$$= 3345 \, \# $$

Determine max stud spacing

$$\frac{2500 \text{ PLF}}{3345 \text{ LBS/STUD}} \; : \; \frac{12}{S}$$
$$16.06'' \qquad S = 16'' \text{ O.C.}$$
$$(\text{ROUND DOWN})$$

Stud Wall Example

Check bearing on sill plate

3.10.4 Bearing Area Factor, C_b

Reference compression design values perpendicular to grain, $F_{c\perp}$, apply to bearings of any length at the ends of a member, and to all bearings 6" or more in length at any other location. For bearings less than 6" in length and not nearer than 3" to the end of a member, the reference compression design value perpendicular to grain, $F_{c\perp}$, shall be permitted to be multiplied by the following bearing area factor, C_b:

$$C_b = \frac{\ell_b + 0.375}{\ell_b} \qquad (3.10\text{-}2)$$

where:

ℓ_b = bearing length measured parallel to grain, in.

Equation 3.10-2 gives the following bearing area factors, C_b, for the indicated bearing length on such small areas as plates and washers:
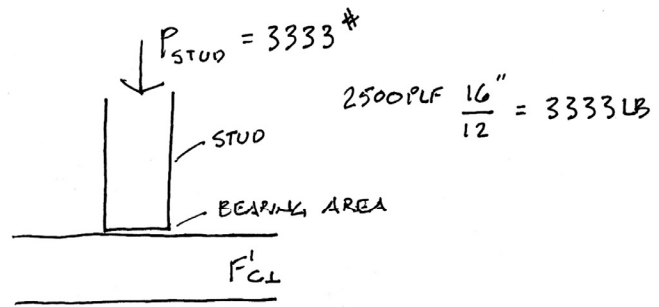
Table 3.10.4   Bearing Area Factors, C_b

ℓ_b	0.5"	1"	1.5"	2"	3"	4"	6" or more
C_b	1.75	1.38	1.25	1.19	1.13	1.10	1.00

For round bearing areas such as washers, the bearing length, ℓ_b, shall be equal to the diameter.

Stud Wall Example

Check bearing on sill plate
- determine Cb
- calculate $F'_{c\perp}$
- calculate $f_{c\perp}$
- check stress

$P_{STUD} = 3333^{\#}$

$2500 PLF \dfrac{16''}{12} = 3333 LB$

STUD

BEARING AREA

$F'_{c\perp}$

$b = 1.5''$

$C_b = 1.25$

$F_{c\perp} = 425 \, psi$ $\qquad F'_{c\perp} = 425(1.25) = 531 \, psi$

$f_{c\perp} = \dfrac{P}{A} = \dfrac{3333^{\#}}{8.25 \, in^2} = 404 \, psi$

$f_{c\perp} = 404 < 531 = F'_{c\perp} \quad \checkmark oK$