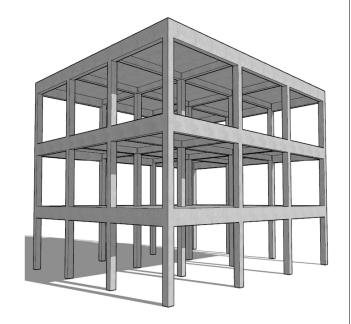
# Architecture 324 Structures II

# Reinforced Concrete Beams Ultimate Strength Design (ACI 318-14) – PART II

- Rectangular Slab Analysis
- · Reinforcement Detailing
- Rectangular Beam Design Method I



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# One-way Slab Analysis

#### Data:

- Section dimensions b, h, (span)
- Steel area As , bar diam. b<sub>d</sub> , o.c. spacing
- Material properties f'c, fy

#### Required:

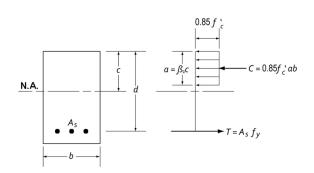
- · Nominal Strength (of beam) Moment Mn
- Required (by load) Design Moment Mu
- · Load capacity
- 1. Calculate  $d = h cover bar_d/2$
- 2. Find As/ft. Check As min
- 3. Calculate a
- 4. Determine c
- 5. Check that  $\varepsilon_t \ge 0.005$  (tension controlled)

Table 7.6.1.1—A<sub>s,min</sub> for nonprestressed

- 6. Find nominal moment, Mn
- $As/ft = As \times 12/o.c.$

Ag = bh

- 7. Calculate required moment,
   φ Mn ≥ Mu (if ε<sub>t</sub> ≥ 0.005 then φ = 0.9)
- 8. Determine max. loading (or span)



$$\varepsilon = \frac{a}{\beta_1} \qquad \varepsilon_t = \frac{d-c}{c} \quad 0.003 \ge 0.005$$

$$a = \frac{A_s f_y}{0.85 f_c' b} \qquad M_n = A_s f_y \left( d - \frac{a}{2} \right)$$

$$\varphi M_n \ge M_u$$

$$M_u = \frac{(1.2w_{DL} + 1.6w_{LL})l^2}{8}$$
$$1.6w_{LL} = \frac{M_u 8}{l^2} - 1.2w_{DL}$$

# Slab Analysis

#### Data:

- Span = 18 ft
- h = 11" take b = 12"
- Steel #8 @ 18" o.c.
- $f'_c = 3000 \text{ psi}$
- $f_v = 60 \text{ ksi}$

Bar size designa- tion	Nominal cross section area, sq. in.	Weight, lb per ft	Nominal diameter in.
#3	0.11	0.376	0.375
#4	0.20	0.668	0.500
#5	0.31	1.043	0.625
#6	0.44	1.502	0.750
#7	0.60	2.044	0.875
#8	0.79	2.670	1.000
#9	1.00	3.400	1.128
#10	1.27	4.303	1.270
#11	1.56	5.313	1.410
#14	2.25	7.650	1.693
#18	4.00	13.600	2.257

#### Required:

- Design moment capacity M<sub>...</sub>
- Maximum LL in PSF

- 1. Find d
- $A_{S} = \frac{12''}{18''} (0.79 in^{2})$   $= 0.5267 in^{2}/FT$
- 2. Find A<sub>s</sub> Check A<sub>s.min</sub>

[0.0018(60)/60] 132 = 0.237 in<sup>2</sup>

 $0.0014 (132) = 0.1848 in^2$ 

0.527 > 0.237 ok

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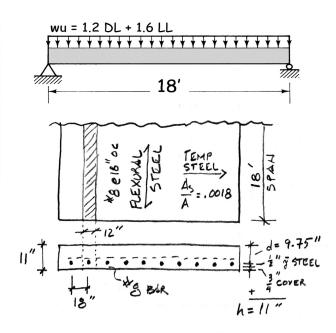


Table 7.6.1.1— $A_{s,min}$  for nonprestressed one-way slabs

Reinforcement type	$f_y$ , psi		$A_{s,min}$
Deformed bars	< 60,000		$0.0020A_g$
Deformed bars or welded wire reinforcement	≥ 60,000	Greater of:	$\frac{0.0018\times60,000}{f_y}A_{\xi}$
reinforcement			$0.0014A_{g}$

\_\_\_\_\_

# Slab Analysis

t' <sub>c</sub>	$\beta_1$
0	0.85
1000	0.85
2000	0.85
3000	0.85
4000	0.85
5000	8.0
6000	0.75
7000	0.7
8000	0.65
9000	0.65
10000	0.65

4. Find 
$$c = \beta_1$$
 a

3. Find a

- 5. Check failure mode  $\varepsilon_t \ge 0.005$  for tension controlled
- 6. Find force T
- 7. Find moment arm z
- 8. Find nominal strength moment, M<sub>n</sub>

$$d = \frac{A_5 fy}{.85 f_c'b} = \frac{0.5267(60)}{.85(3)(12)} = 1.033''$$

$$\frac{.85 f_c'b}{.85 f_c'b} = \frac{0.5267(60)}{.85(3)(12)} = 1.033''$$

$$\frac{.85 f_c'b}{.85 f_c'b} = \frac{0.5267(60)}{.85(3)(12)} = 1.033''$$

$$\frac{.85 f_c'b}{.85 f_c'b} = \frac{0.5267(60)}{.85(3)(12)} = 1.033''$$

$$C = \frac{\partial}{\beta_1} = \frac{1.033}{0.85} = 1.215$$

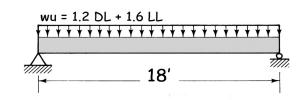
ACI 318-14

$$\epsilon_t = \frac{0.003 \, d}{c} - 0.003$$

$$\epsilon_t = \frac{0.003 (9.75'')}{1.215''} - 0.003 = 0.021 ''$$

$$T = A_s fy = 0.5267(60) = 31.6 K$$
  
 $E = d - \frac{9}{2} = 9.75 - \frac{1.033}{2} = 9.23$ 

## Slab Analysis



- 9. Find required moment, M<sub>II</sub>
- Ho= ΦHn = 0,9 (291.8) 1000 = 218851-4

10. Find slab DL

WPL = 2 1/2 = 150 1/2 = 137.5 PSF

- 11. Determine max. loading
- $M_0 = 21885 \frac{1.4}{8} = \frac{(1.2 \, \omega_{DL} + 1.6 \, \omega_{LL}) \, A^2}{8}$   $\frac{21885 \, (8)}{(18^7)^2} = 1.2 \, (137.5) + 1.6 \, (\omega_{LL})$   $540.37 = 165 + 1.6 \, (\omega_{LL})$   $W_{LL} = 234.6 \, PSF$

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# **Details of Reinforcement**

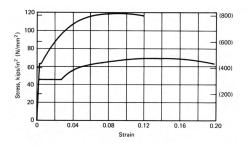
#### Size

· Nominal 1/8" increments

#### Grade

- 40 (40 ksi)
- 60 (60 ksi)
- 75 (75 ksi)

Bar size designa- tion	Nominal cross section area, sq. in.	Weight, lb per ft	Nominal diameter, in.
#3	0.11	0.376	0.375
#4	0.20	0.668	0.500
#5	0.31	1.043	0.625
#6	0.44	1.502	0.750
#7	0.60	2.044	0.875
#8	0.79	2.670	1.000
#9	1.00	3.400	1.128
#10	1.27	4.303	1.270
#11	1.56	5.313	1.410
#14	2.25	7.650	1.693
#18	4.00	13.600	2.257



#### **Details of Reinforcement**

# ACI 318 Chapter 25.2 Placement of Reinforcement

- Cover (ACI 20.6.1)
- Horizontal spacing in beams, s<sub>h</sub> (ACI 25.2.1)
   1 inch
   d<sub>b</sub>
   4/3 d<sub>agg,max</sub>
- Vertical spacing in beams (ACI 25.2.2) Min 1 inch



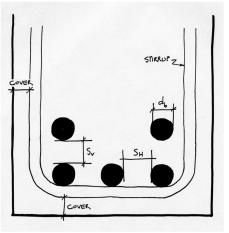
https://www.constructioncost.co/honeycombing-in-concrete.htm

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# Table 20.6.1.3.1—Specified concrete cover for cast-in-place nonprestressed concrete members

Concrete exposure	Member	Reinforcement	Specified cover, in.
Cast against and permanently in contact with ground	All	All	3
Exposed to weather		No. 6 through No. 18 bars	2
or in contact with ground	All	No. 5 bar, W31 or D31 wire, and smaller	1-1/2
	Slabs, joists,	No. 14 and No. 18 bars	1-1/2
Not exposed to weather or in	and walls	No. 11 bar and smaller	3/4
contact with ground	Beams, columns, pedestals, and tension ties	Primary reinforce- ment, stirrups, ties, spirals, and hoops	1-1/2

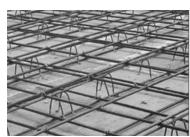


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### **Details of Reinforcement**

# ACI 318 Chapter 25 Placement of Reinforcement

- Chairs
- Bolsters

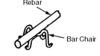


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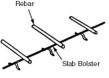






Slab Bolster





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#### **Details of Reinforcement**

ACI 318 Chapter 25

#### Minimum bend diameter

factor x d<sub>b</sub>

#### Hooks for bars in tension

- ACI Table 25.3.1
- · Inside diameter

#### Bends for stirrups

• ACI Table 25.3.2

Table 25.3.1—Standard hook geometry for development of deformed bars in tension

Type of standard hook	Bar size	Minimum inside bend diameter, in.	Straight extension <sup>[1]</sup> $\ell_{ext}$ in.	Type of standard hook
	No. 3 through No. 8	$6d_b$		Point at which bar is developed
90-degree	No. 9 through No. 11	8 <i>d</i> <sub>b</sub>	124	90-degree bend
hook	No. 14 and No. 18	10 <i>d<sub>b</sub></i>	1246	Diameter
	No. 3 through No. 8	6 <i>d</i> <sub>b</sub>		Point at which bar is developed
180-degree	No. 9 through No. 11	8 <i>d</i> <sub>b</sub>	Greater of	180-degree
hook	No. 14 and No. 18	10 <i>d<sub>b</sub></i>	bar is d  d  Diameter—  Lan  Point as dw  d  d  Can	laxt

<sup>&</sup>quot;A standard hook for deformed bars in tension includes the specific inside bend diameter and straight extension length. It shall be permitted to use a longer straight extension at the end of a hook. A longer extension shall not be considered to increase the anchorage capacity of the hook.

Table 25.3.2—Minimum inside bend diameters and standard hook geometry for stirrups, ties, and hoops

Type of stan- dard hook	Bar size	Minimum inside bend diameter, in.	Straight extension <sup>[1]</sup> $\ell_{ext}$ in.	Type of standard hook
90-degree	No. 3 through No. 5	4d <sub>b</sub>	Greater of $6d_b$ and 3 in.	d <sub>b</sub> 90-degree bend
hook	No. 6 through No. 8	6 <i>d</i> <sub>b</sub>	12 <i>d</i> <sub>b</sub>	Diameter \\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\
135-degree	No. 3 through No. 5	4d <sub>b</sub>	Greater of 6d <sub>b</sub> and	135-degree bend
hook	No. 6 through No. 8	6 <i>d</i> <sub>b</sub>	3 in.	Diameter
180-degree	No. 3 through No. 5	4d <sub>b</sub>	Greater of	d <sub>b</sub> 180-degree
hook	No. 6 through No. 8	6 <i>d</i> <sub>b</sub>	4 <i>d<sub>b</sub></i> and 2.5 in.	Diameter bend

<sup>11/</sup>A standard hook for stirrups, tics, and hoops includes the specific inside bend diameter and straight extension length. It shall be permitted to use a longer straight extension at the end of a hook. A longer extension shall not be considered to increase the anchorage capacity of the hook.

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#### **Details of Reinforcement**

ACI 318 Chapter 25

#### Development length of bars

- 12" min
- Based on table 25.4.2.2

Table 25.4.2.4—Modification factors for development of deformed bars and deformed wires in tension

Modification factor	Condition	Value of factor
	Lightweight concrete	0.75
Lightweight λ	Lightweight concrete, where $f_{ct}$ is specified	In accordance with 19.2.4.3
	Normalweight concrete	1.0
F(II)	Epoxy-coated or zinc and epoxy dual-coated reinforcement with clear cover less than $3d_b$ or clear spacing less than $6d_b$	1.5
Epoxy <sup>[1]</sup> $\Psi_e$	Epoxy-coated or zinc and epoxy dual- coated reinforcement for all other conditions	1.2
	Uncoated or zinc-coated (galvanized) reinforcement	1.0
Size	No. 7 and larger bars	1.0
$\psi_s$	No. 6 and smaller bars and deformed wires	0.8
Casting position <sup>[1]</sup>	position <sup>[1]</sup> reinforcement	
Ψι	Other	1.0

<sup>[1]</sup> The product  $\psi_t \psi_e$  need not exceed 1.7.

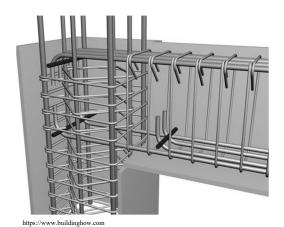


Table 25.4.2.2—Development length for deformed bars and deformed wires in tension

Spacing and cover	No. 6 and smaller bars and deformed wires	No. 7 and larger bars
Clear spacing of bars or wires being developed or lap spliced not less than $d_b$ , clear cover at least $d_b$ , and stirrups or ties throughout $\ell_d$ not less than the Code minimum or Clear spacing of bars or wires being developed or lap spliced at least $2d_b$ and clear cover at least $d_b$	$\left(\frac{f_{y}\Psi_{t}\Psi_{e}}{25\lambda\sqrt{f_{c}^{\prime}}}\right)d_{b}$	$\left(\frac{f_y \psi_i \psi_e}{20 \lambda \sqrt{f_c'}}\right) d_b$
Other cases	$\left(\frac{3f_{y}\psi_{i}\psi_{e}}{50\lambda\sqrt{f_{c}'}}\right)d_{b}$	$\left(\frac{3f_y\psi_i\psi_e}{40\lambda\sqrt{f_c'}}\right)d_b$

#### Other Useful Tables:

**Table A.1** Values of Modulus of Elasticity for Normal-Weight Concrete

Custo	mary Units	SIU	Jnits
f' (psi)	E <sub>c</sub> (psi)	f' <sub>c</sub> (MPa)	E <sub>c</sub> (MPa)
3,000	3,140,000	20.7	21 650
3,500	3,390,000	24.1	23 373
4,000	3,620,000	27.6	24 959
4,500	3,850,000	31.0	26 545
5,000	4,050,000	34.5	27 924

Jack C McCormac, 1978, Design of Reinforced Concrete,

Table A.2 Designations, Areas, Perimeters, and Weights of Standard Bars

	C	ustomary Uni	ts	SI Units				
Bar No.	Diameter (in.)	Cross- sectional Area (in.2)	Unit Weight (lb/ft)	Diameter (mm)	Cross- sectional Area (mm²)	Unit Weight (kg/m)		
3	0.375	0.11	0.376	9.52	71	0.560		
4	0.500	0.20	0.668	12.70	129	0.994		
5	0.625	0.31	1.043	15.88	200	1.552		
6	0.750	0.44	1.502	19.05	284	2.235		
7	0.875	0.60	2.044	22.22	387	3.042		
8	1.000	0.79	2.670	25.40	510	3.973		
9	1.128	1.00	3.400	28.65	645	5.060		
10	1.270	1.27	4.303	32.26	819	6.404		
11	1.410	1.56	5.313	35.81	1006	7.907		
14	1.693	2.25	7.650	43.00	1452	11.384		
18	2.257	4.00	13.600	57.33	2581	20.238		

Table A.4 Areas of Groups of StandardBars (in.2)

						Num	ber of Ba	ırs					
Bar No.	2	3	4	5	6	7	8	9	10	11	12	13	1,4
4	0.39	0.58	0.78	0.98	1.18	1.37	1.57	1.77	1.96	2.16	2.36	2.55	2.75
5	0.61	0.91	1.23	1.53	1.84	2.15	2.45	2.76	3.07	3.37	3.68	3.99	4.30
6	0.88	1.32	1.77	2.21	2.65	3.09	3.53	3.98	4.42	4.86	5.30	5.74	6.19
7	1.20	1.80	2.41	3.01	3.61	4.21	4.81	5.41	6.01	6.61	7.22	7.82	8.42
8	1.57	2.35	3.14	3.93	4.71	5.50	6.28	7.07	7.85	8.64	9.43	10.21	11.00
9	2.00	3.00	4.00	5.00	6.00	7.00	8.00	9.00	10.00	11.00	12.00	13.00	14.00
10	2.53	3.79	5.06	6.33	7.59	8.86	10.12	11.39	12.66	13.92	15.19	16.45	17.72
11	3.12	4.68	6.25	7.81	9.37	10.94	12.50	14.06	15.62	17.19	18.75	20.31	21.87
14	4.50	6.75	9.00	11.25	13.50	15.75	18.00	20.25	22.50	24.75	27.00	29.25	31.50
18	8.00	12.00	16.00	20.00	24.00	28.00	32.00	36.00	40.00	44.00	48.00	52.00	56.00

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# Rectangular Beam Design

Two approaches:

#### Method 1:

#### Data:

- Load and Span
- Material properties f'<sub>c</sub>, f<sub>y</sub>
- All section dimensions: h and b

#### Required:

Steel area – A<sub>s</sub>

# h As?

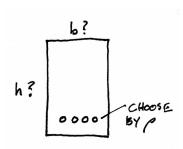
#### Method 2:

#### Data:

- Load and Span
- Some section dimensions h or b
- Material properties f'c, fv
- Choose  $\rho$

#### Required:

- Steel area A<sub>s</sub>
- Beam dimensions b or h



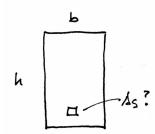
# Rectangular Beam Design - Method 1

#### Data:

- Load and Span
- Material properties f'c, fy
- All section dimensions b and h

#### Required:

- Steel area A<sub>s</sub>
- 1. Calculate the factored load and find factored required moment, M<sub>II</sub>
- 2. Find  $d = h cover stirrup d_h/2$
- 3. Estimate moment arm z = jd, for beams  $j \approx 0.9$  for slabs  $j \approx 0.95$
- 4. Estimate A<sub>s</sub> based on estimate of jd.
- 5. Use As to find a
- 6. Use a to find A<sub>s</sub> (repeat...until **2%** accuracy)
- 7. Choose bars for A<sub>s</sub> and check A<sub>s</sub> max & min
- 8. Check that  $\varepsilon_t \ge 0.005$
- 9. Check  $M_u \le \phi M_n$  (final condition)
- 10. Design shear reinforcement (stirrups)
- 11. Check deflection, crack control, rebar development length



$$M_u = \frac{(\gamma_{DL} w_{DL} + \gamma_{LL} w_{LL})l^2}{8}$$

$$A_{S} = \frac{M_{u}}{\varphi f_{y} \left( d - \frac{a}{2} \right)}$$

$$a = \frac{A_s f_y}{0.85 f_c' b}$$

$$M_n = A_s f_y \left( d - \frac{a}{2} \right)$$

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# One-way Slab Design Method 1

#### Data:

- Load and Span
- Material properties f'<sub>c</sub>, f<sub>y</sub>
- · All section dimensions:
- h (based on deflection limit)
- b = typical 12" width

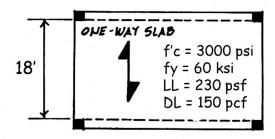
## Required:

Steel area – A<sub>s</sub>

First estimate the slab thickness, h.

Try first the recommended minimum.

Deeper sections require less steel, but of course more concrete.



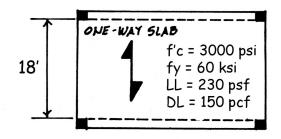
PLAN VIEW

Table 7.3.1.1—Minimum thickness of solid nonprestressed one-way slabs

Support condition	Minimum $h^{[1]}$
Simply supported	ℓ/20
One end continuous	ℓ/24
Both ends continuous	ℓ/28
Cantilever	€/10

THICKNESS, h, BASED ON DEFLECTION
$$h = \frac{1}{20} = \frac{18 \times 12}{20} = 10.8" \text{ USE II"}$$

# One-way Slab Slab Design



#### PLAN VIEW

1. Calculate the dead load and find required  $\rm M_{\rm u}$ 

FACTOR LOAPS
$$DL = \frac{11''}{12}(150) = 137.5 \text{ PSF}$$

$$LL (41VEN) = 230 \text{ PSF}$$

$$W_{D} = 1.2(137.5) + 1.6(230) = 533$$

$$M_{0} = \frac{\omega_{0} \, \ell^{2}}{8} = \frac{533 \, RF (18')^{2}}{8} = 21 \, 587' - *$$

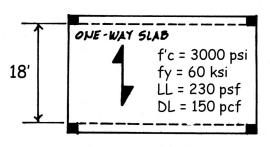
$$= 259'' - K$$

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# One-way Slab Slab Design



## PLAN VIEW

- Find d based on the estimated h and rebar size (guessing #4)
- 3. Estimate moment arm  $z \approx 0.95 d$

# One-way Slab Slab Design

- 4. Estimate  $A_s$  based on estimate of z
- 5. Use A<sub>s</sub> to find a
- 6. Use a to find A<sub>s</sub> (repeat...)

TRIAL I
$$A_{S} = \frac{M u}{\phi f_{y}(z)} = \frac{259''^{-15}}{0.9(60 \text{ Ksi})(9.5)''} = 0.505 \text{ in}^{2}$$

$$A = \frac{A_{S} f_{y}}{.85 f_{c}' b} = \frac{0.505(60)}{.85(3)(12)} = 0.99''$$

TRIAL 2
$$A_{5} = \frac{H_{0}}{\phi f_{3}(d - \frac{e_{1}^{2}}{2})} = \frac{259}{0.9(60)(10 - \frac{.99}{2})}$$

$$A_{5} = 0.5046h^{2} \quad \text{WITHIN 2\%}$$

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# One-way Slab Slab Design

7. Choose bars for A<sub>s</sub> required:

either

**choose bars** and calculate spacing or

**choose spacing** and find bar size If the bar size changes, re-calculate to find new d. Then, re-calculate  $A_s$ ...

Check  $A_{s,min}$ 

(for slabs  $A_{s,min}$  from ACI Table 7.6.1.1)

Table 7.6.1.1— $A_{s,min}$  for nonprestressed one-way slabs

Reinforcement type	$f_y$ , psi		$A_{s,min}$
Deformed bars	< 60,000	$0.0020A_{g}$	
Deformed bars or welded wire reinforcement	≥ 60,000	Greater of:	$\frac{0.0018\times60,000}{f_y}A_{\xi}$
			$0.0014A_{g}$

#### CHOOSE BARS

i, use 
$$4''o.c.$$
 (always round down)  
 $4s = 0.60 \text{ m}^2/\text{FT} > 0.505 \text{ }$ 

ALTERNATE FOR MAX. 
$$S = 18''$$

$$\frac{0.505}{12''} : \frac{A_b}{18''} \qquad A_b = 0.75 \text{ in}^2$$

$$\frac{A_b}{12''} : \frac{A_b}{18''} \qquad \frac{A_b}{8} = 0.79$$

$$i. USE \qquad \frac{48}{8} e 18'' \text{ o.c.}$$

$$A_5 = 0.526 \text{ in}^2/\text{FT} > 0.505 \text{ V}$$

#### Check As, min

# One-way Slab Slab Design

8. Check that  $\varepsilon_t \ge 0.005$ 

RE-CALC 2 FOR 
$$A_5 = 0.6 \frac{m^3}{67}$$

$$a = \frac{A_5 f_{yy}}{0.85 f_2'} = \frac{0.6(60)}{0.85(3)(12)} = 1.176''$$

$$C = \frac{2}{B_1} = \frac{1.176}{0.85} = 1.384''$$

$$G_1 = \frac{d-c}{c} 0.003 = \frac{1.384''}{0.003} = 0.01759$$

$$1.384'''$$

$$0.01759 > 0.005$$

$$1.764510A CONTROLLED V$$

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# One-way Slab Slab Design

9. Check  $M_u \le \phi M_n$  (final condition)

$$A_s = A_{s,used}$$
  
 $M_n = Tz$ 

- 10. Add stirrups (no stirrups in slab)
- 11. Check deflection, crack control, and rebar development length

$$M_n = A_3 f_y \left(d - \frac{27}{2}\right)$$
 $M_n = 0.6(60)\left(9.5^{n} - \frac{1.176}{2}\right)$ 
 $M_n = 36\left(8.911^{n}\right) = 320.8^{n}$ 
 $M_n = 0.9\left(320.8\right) = 288.7^{n}$ 
 $M_0 = 259^{n}$ 
 $M_0 < 4M_0$ 
 $M_0 < 4M_0$ 

# Rectangular Beam Design - Method 2

#### Data:

- Load and Span
- Some section dimensions b or h
- Material properties f'<sub>c</sub>, f<sub>y</sub>

#### Required:

- Steel area A<sub>s</sub>
- Beam dimensions b and h
- 1. Estimate the dead load (estimate h and b) (L/8  $\leq$  h  $\leq$  L/21, h  $\approx$  L/12 and b:h  $\approx$  1:2 to 2:3), find M<sub>II</sub>
- 2. Choose  $\rho$  (equation assumes  $\varepsilon_t = 0.0075$ )
- 3. Calculate bd<sup>2</sup>
- 4. Choose b and solve for d (or d and solve b)
- 5. Revise h, weight, M<sub>u</sub>, and bd<sup>2</sup>
- 6. Find  $A_s = \rho bd$
- 7. Choose bars for A<sub>s</sub>, determine spacing and cover, and revise d
- 8. Check that  $\varepsilon_t \ge 0.005$  (if not, increase h and reduce  $A_s$ )
- 9. Design shear reinforcement (stirrups)
- 10. Check deflection, crack control, steel development length

$$M_u = \frac{(\gamma_{DL} w_{DL} + \gamma_{LL} w_{LL})l^2}{8}$$

$$\rho = \frac{\beta_1 f_c'}{4 f_y}$$

$$bd^{2} = \frac{M_{u}}{\varphi \rho f_{y} \left(1 - 0.59 \rho (f y/f_{c}^{\prime})\right)}$$

$$A_s = \rho b d$$

$$a = \frac{\rho f_y d}{0.85 f_c'}$$

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