

# Architecture 324 Structures II

## Wood Beam Analysis

- ASD approach
- NDS criteria
- Wood Beam Analysis



## Allowable Stresses

From the NDS Supplement

**DESIGN VALUES FOR WOOD CONSTRUCTION – NDS SUPPLEMENT** **35**

**Table 4A (Cont.) Reference Design Values for Visually Graded Dimension Lumber (2" - 4" thick)<sup>1,2,3</sup>**

(All species except Southern Pine— see Table 4B) (Tabulated design values are for normal load duration and dry service conditions. See NDS 4.3 for a comprehensive description of design value adjustment factors.)

**USE WITH TABLE 4A ADJUSTMENT FACTORS**

Species and commercial grade	Size classification	Design values in pounds per square inch (psi)						Modulus of Elasticity		Specific Gravity <sup>4</sup>	Grading Rules Agency
		Bending	Tension parallel to grain	Shear parallel to grain	Compression perpendicular to grain	Compression parallel to grain	E				
		F <sub>b</sub>	F <sub>t</sub>	F <sub>v</sub>	F <sub>c⊥</sub>	F <sub>c</sub>					
<b>HEM-FIR</b>											
Select Structural		1,400	925	150	405	1,500	1,600,000	580,000			
No. 1 & Btr		1,100	725	150	405	1,350	1,500,000	550,000			
No. 1	2" & wider	975	625	150	405	1,350	1,500,000	550,000	0.43	WCLIB WWPA	
No. 2		850	525	150	405	1,300	1,300,000	470,000			
No. 3		500	300	150	405	725	1,200,000	440,000			
Stud	2" & wider	675	400	150	405	800	1,200,000	440,000			
Construction		975	600	150	405	1,550	1,300,000	470,000			
Standard	2" - 4" wide	550	325	150	405	1,300	1,200,000	440,000			
Utility		250	150	150	405	850	1,100,000	400,000			

# Allowable Stress Design by NDS

## Flexure

$$F_b'$$

$$\geq$$

$$f_b$$

### Allowable Flexure Stress $F_b'$

$F_b$  from NDS Supplement tables determined by species and grade

$$F_b' = F_b \text{ (usage factors)}$$

usage factors for flexure:

- $C_D$  Load Duration Factor
- $C_M$  Moisture Factor
- $C_t$  Temperature Factor
- $C_L$  Beam Stability Factor
- $C_F$  Size Factor
- $C_{fu}$  Flat Use
- $C_i$  Incising Factor
- $C_r$  Repetitive Member Factor

$$\geq$$

### Actual Flexure Stress $f_b$

$$f_b = Mc/I = M/S$$

$$S = I/c = bd^2/6$$

# Allowable Stress Design by NDS

## Shear

$$F_v'$$

$$\geq$$

$$f_v$$

### Allowable Shear Stress $F_v'$

$F_v$  from tables determined by species and grade

$$F_v' = F_v \text{ (usage factors)}$$

usage factors for shear:

- $C_D$  Load Duration Factor
- $C_M$  Moisture Factor
- $C_t$  Temperature Factor
- $C_i$  Incising Factor

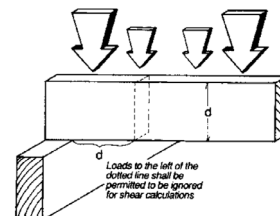
$$\geq$$

### Actual Shear Stress $f_v$

$$f_v = VQ / I b = 1.5 V/A$$

Can use  $V$  at  $d$  from support as maximum

#### Shear at Supports



# Adjustment Factors

**Table 4.3.1 Applicability of Adjustment Factors for Sawn Lumber**

	ASD only	ASD and LRFD											LRFD only		
		Load Duration Factor	Wet Service Factor	Temperature Factor	Beam Stability Factor	Size Factor	Flat Use Factor	Incising Factor	Repetitive Member Factor	Column Stability Factor	Buckling Stiffness Factor	Bearing Area Factor	Format Conversion Factor	Resistance Factor	Time Effect Factor
$F_b' = F_b$	x	$C_D$	$C_M$	$C_t$	$C_L$	$C_F$	$C_{fu}$	$C_i$	$C_r$	-	-	-	$K_F$	$\phi_b$	$\lambda$
$F_t' = F_t$	x	$C_D$	$C_M$	$C_t$	-	$C_F$	-	$C_i$	-	-	-	-	$K_F$	$\phi_t$	$\lambda$
$F_v' = F_v$	x	$C_D$	$C_M$	$C_t$	-	-	-	$C_i$	-	-	-	-	$K_F$	$\phi_v$	$\lambda$
$F_{c\perp}' = F_{c\perp}$	x	-	$C_M$	$C_t$	-	-	-	$C_i$	-	-	-	$C_b$	$K_F$	$\phi_c$	$\lambda$
$F_c' = F_c$	x	$C_D$	$C_M$	$C_t$	-	$C_F$	-	$C_i$	-	$C_p$	-	-	$K_F$	$\phi_c$	$\lambda$
$E' = E$	x	-	$C_M$	$C_t$	-	-	-	$C_i$	-	-	-	-	-	-	-
$E_{min}' = E_{min}$	x	-	$C_M$	$C_t$	-	-	-	$C_i$	-	-	$C_T$	-	$K_F$	$\phi_s$	-

# Adjustment Factors

## Allowable Flexure Stress $F_b'$

$F_b$  from tables determined by species and grade

$$F_b' = F_b (C_D C_M C_t C_L C_F C_{fu} C_i C_r)$$

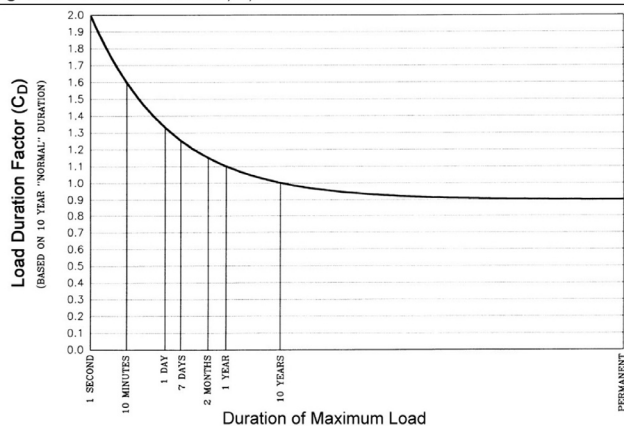
Usage factors for flexure:

$C_D$  Load Duration Factor

**Table 2.3.2 Frequently Used Load Duration Factors,  $C_D$**

Load Duration	$C_D$	Typical Design Loads
Permanent	0.9	Dead Load
Ten years	1.0	Occupancy Live Load
Two months	1.15	Snow Load
Seven days	1.25	Construction Load
Ten minutes	1.6	Wind/Earthquake Load
Impact <sup>2</sup>	2.0	Impact Load

**Figure B1 Load Duration Factors,  $C_D$ , for Various Load Durations**



- (1) Actual stress due to (DL)  $\leq (0.9)$  (Design value)
- (2) Actual stress due to (DL+LL)  $\leq (1.0)$  (Design value)
- (3) Actual stress due to (DL+WL)  $\leq (1.6)$  (Design value)
- (4) Actual stress due to (DL+LL+SL)  $\leq (1.15)$  (Design value)
- (5) Actual stress due to (DL+LL+WL)  $\leq (1.6)$  (Design value)
- (6) Actual stress due to (DL+SL+WL)  $\leq (1.6)$  (Design value)
- (7) Actual stress due to (DL+LL+SL+WL)  $\leq (1.6)$  (Design value)

# Adjustment Factors

## Allowable Flexure Stress $F_b'$

$F_b$  from tables determined by species and grade

$$F_b' = F_b (C_D C_M C_t C_L C_F C_{fu} C_i C_r)$$

Usage factors for flexure:

$C_t$  Temperature Factor

**Table 2.3.3 Temperature Factor,  $C_t$**

Reference Design Values	In-Service Moisture Conditions <sup>1</sup>	$C_t$		
		$T \leq 100^\circ\text{F}$	$100^\circ\text{F} < T \leq 125^\circ\text{F}$	$125^\circ\text{F} < T \leq 150^\circ\text{F}$
$F_t, E, E_{min}$	Wet or Dry	1.0	0.9	0.9
	Dry	1.0	0.8	0.7
$F_b, F_v, F_c,$ and $F_{c\perp}$	Wet	1.0	0.7	0.5

1. Wet and dry service conditions for sawn lumber, structural glued laminated timber, prefabricated wood I-joists, structural composite lumber, wood structural panels and cross-laminated timber are specified in 4.1.4, 5.1.4, 7.1.4, 8.1.4, 9.3.3, and 10.1.5 respectively.

# Adjustment Factors

## Allowable Flexure Stress $F_b'$

$F_b$  from NDS tables

$$F_b' = F_b (C_D C_M C_t C_L C_F C_{fu} C_i C_r)$$

Usage factors for flexure:

$C_M$  Moisture Factor

$C_F$  Size Factor

## Wet Service Factor, $C_M$

When dimension lumber is used where moisture content will exceed 19% for an extended time period, design values shall be multiplied by the appropriate wet service factors from the following table:

Wet Service Factors, $C_M$					
$F_b$	$F_t$	$F_v$	$F_{c\perp}$	$F_c$	E and $E_{min}$
0.85*	1.0	0.97	0.67	0.8**	0.9

\* when  $(F_b)(C_F) \leq 1,150$  psi,  $C_M = 1.0$

\*\* when  $(F_c)(C_F) \leq 750$  psi,  $C_M = 1.0$

## Size Factors, $C_F$

Grades	Width (depth)	$F_b$		$F_t$	$F_c$
		Thickness (breadth)			
		2" & 3"	4"		
Select Structural, No.1 & Btr, No.1, No.2, No.3	2", 3", & 4"	1.5	1.5	1.5	1.15
	5"	1.4	1.4	1.4	1.1
	6"	1.3	1.3	1.3	1.1
	8"	1.2	1.3	1.2	1.05
	10"	1.1	1.2	1.1	1.0
	12"	1.0	1.1	1.0	1.0
Stud	14" & wider	0.9	1.0	0.9	0.9
	2", 3", & 4"	1.1	1.1	1.1	1.05
	5" & 6"	1.0	1.0	1.0	1.0
Construction, Standard	8" & wider	Use No.3 Grade tabulated design values and size factors			
	2", 3", & 4"	1.0	1.0	1.0	1.0
Utility	4"	1.0	1.0	1.0	1.0
	2" & 3"	0.4	—	0.4	0.6

# Adjustment Factors

## Allowable Flexure Stress $F_b'$

$F_b$  from NDS tables

$$F_b' = F_b (C_D C_M C_t C_L C_F C_{fu} C_i C_r)$$

Usage factors for flexure:

- $C_{fu}$  Flat Use
- $C_r$  Repetitive Member Factor

## Flat Use Factor, $C_{fu}$

Bending design values adjusted by size factors are based on edgewise use (load applied to narrow face). When dimension lumber is used flatwise (load applied to wide face), the bending design value,  $F_b$ , shall also be permitted to be multiplied by the following flat use factors:

Flat Use Factors, $C_{fu}$		
Width (depth)	Thickness (breadth)	
	2" & 3"	4"
2" & 3"	1.0	—
4"	1.1	1.0
5"	1.1	1.05
6"	1.15	1.05
8"	1.15	1.05
10" & wider	1.2	1.1

## Repetitive Member Factor, $C_r$

Bending design values,  $F_b$ , for dimension lumber 2" to 4" thick shall be multiplied by the repetitive member factor,  $C_r = 1.15$ , when such members are used as joists, truss chords, rafters, studs, planks, decking, or similar members which are in contact or spaced not more than 24" on center, are not less than 3 in number and are joined by floor, roof, or other load distributing elements adequate to support the design load.

# Adjustment Factors

## Allowable Flexure Stress $F_b'$

$F_b$  from tables determined by species and grade

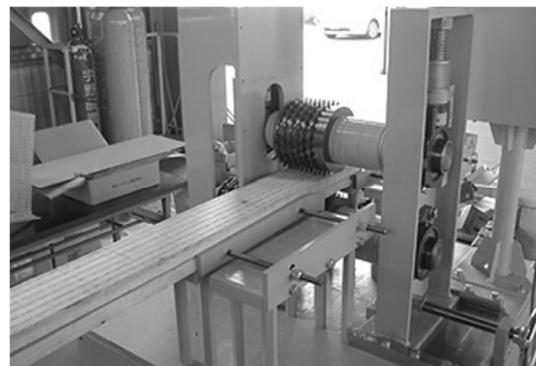
$$F_b' = F_b (C_D C_M C_t C_L C_F C_{fu} C_i C_r)$$

Usage factors for flexure:

- $C_i$  Incising Factor

**Table 4.3.8 Incising Factors,  $C_i$**

Design Value	$C_i$
$E_s, E_{min}$	0.95
$F_b, F_t, F_c, F_v$	0.80
$F_{cL}$	1.00



# Adjustment Factors

## Allowable Flexure Stress $F_b'$

$F_b$  from tables determined by species and grade

$$F_b' = F_b (C_D C_M C_t C_L C_F C_{fu} C_i C_r)$$

Usage factors for flexure:

$C_L$  Beam Stability Factor

### 3.3.3 Beam Stability Factor, $C_L$

3.3.3.1 When the depth of a bending member does not exceed its breadth,  $d \leq b$ , no lateral support is required and  $C_L = 1.0$ .

3.3.3.2 When rectangular sawn lumber bending members are laterally supported in accordance with 4.4.1,  $C_L = 1.0$ .

3.3.3.3 When the compression edge of a bending member is supported throughout its length to prevent lateral displacement, and the ends at points of bearing have lateral support to prevent rotation,  $C_L = 1.0$ .

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### 4.4.1 Stability of Bending Members

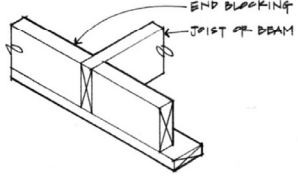
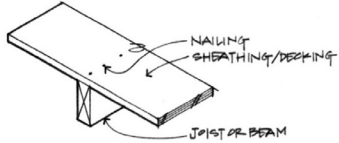
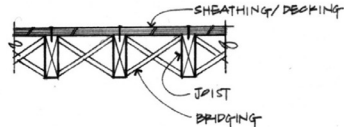
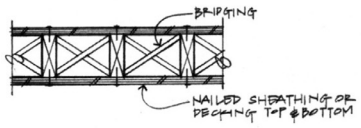
- 2x4 (a)  $d/b \leq 2$ ; no lateral support shall be required.
- 2x6-8 (b)  $2 < d/b \leq 4$ ; the ends shall be held in position, as by full depth solid blocking, bridging, hangers, nailing, or bolting to other framing members, or other acceptable means.
- 2x10 (c)  $4 < d/b \leq 5$ ; the compression edge of the member shall be held in line for its entire length to prevent lateral displacement, as by adequate sheathing or subflooring, and ends at point of bearing shall be held in position to prevent rotation and/or lateral displacement.
- 2x12 (d)  $5 < d/b \leq 6$ ; bridging, full depth solid blocking or diagonal cross bracing shall be installed at intervals not exceeding 8 feet, the compression edge of the member shall be held in line as by adequate sheathing or subflooring, and the ends at points of bearing shall be held in position to prevent rotation and/or lateral displacement.
- 2x14 (e)  $6 < d/b \leq 7$ ; both edges of the member should be held in line for their entire length and ends at points of bearing shall be held in position to prevent rotation and/or lateral displacement.

## $C_L$

$C_L = 1.0$   
when bracing meets 4.4.1  
for the depth/width ratio

Otherwise

$C_L < 1.0$   
calculate factor using  
section 3.3.3

Beam Depth/ Width Ratio	Type of Lateral Bracing Required	Example
2 to 1	None	
3 to 1 <b>2x6</b> <b>2x8</b>	The ends of the beam should be held in position	
5 to 1 <b>2x10</b>	Hold compression edge in line (continuously)	
6 to 1 <b>2x12</b>	Diagonal bridging should be used	
7 to 1 <b>2x14</b>	Both edges of the beam should be held in line	

# C<sub>L</sub> Beam Stability Factor

In the case bracing provisions of 4.4.1 cannot be met, C<sub>L</sub> is calculated using equation 3.3-6

The maximum allowable slenderness, R<sub>B</sub> is 50

**Table 3.3.3 Effective Length, ℓ<sub>e</sub>, for Bending Members**

Cantilever <sup>1</sup>	when ℓ <sub>e</sub> /d < 7	when ℓ <sub>e</sub> /d ≥ 7
Uniformly distributed load	ℓ <sub>e</sub> =1.33 ℓ <sub>u</sub>	ℓ <sub>e</sub> =0.90 ℓ <sub>u</sub> + 3d
Concentrated load at unsupported end	ℓ <sub>e</sub> =1.87 ℓ <sub>u</sub>	ℓ <sub>e</sub> =1.44 ℓ <sub>u</sub> + 3d
Single Span Beam <sup>1,2</sup>	when ℓ <sub>e</sub> /d < 7	when ℓ <sub>e</sub> /d ≥ 7
Uniformly distributed load	ℓ <sub>e</sub> =2.06 ℓ <sub>u</sub>	ℓ <sub>e</sub> =1.63 ℓ <sub>u</sub> + 3d
Concentrated load at center with no intermediate lateral support	ℓ <sub>e</sub> =1.80 ℓ <sub>u</sub>	ℓ <sub>e</sub> =1.37 ℓ <sub>u</sub> + 3d
Concentrated load at center with lateral support at center	ℓ <sub>e</sub> =1.11 ℓ <sub>u</sub>	
Two equal concentrated loads at 1/3 points with lateral support at 1/3 points	ℓ <sub>e</sub> =1.68 ℓ <sub>u</sub>	
Three equal concentrated loads at 1/4 points with lateral support at 1/4 points	ℓ <sub>e</sub> =1.54 ℓ <sub>u</sub>	
Four equal concentrated loads at 1/5 points with lateral support at 1/5 points	ℓ <sub>e</sub> =1.68 ℓ <sub>u</sub>	
Five equal concentrated loads at 1/6 points with lateral support at 1/6 points	ℓ <sub>e</sub> =1.73 ℓ <sub>u</sub>	
Six equal concentrated loads at 1/7 points with lateral support at 1/7 points	ℓ <sub>e</sub> =1.78 ℓ <sub>u</sub>	
Seven or more equal concentrated loads, evenly spaced, with lateral support at points of load application	ℓ <sub>e</sub> =1.84 ℓ <sub>u</sub>	
Equal end moments	ℓ <sub>e</sub> =1.84 ℓ <sub>u</sub>	

1. For single span or cantilever bending members with loading conditions not specified in Table 3.3.3:  
 ℓ<sub>e</sub> = 2.06 ℓ<sub>u</sub> when ℓ<sub>e</sub>/d < 7  
 ℓ<sub>e</sub> = 1.63 ℓ<sub>u</sub> + 3d when 7 ≤ ℓ<sub>e</sub>/d ≤ 14.3  
 ℓ<sub>e</sub> = 1.84 ℓ<sub>u</sub> when ℓ<sub>e</sub>/d > 14.3  
 2. Multiple span applications shall be based on table values or engineering analysis.

3.3.3.6 The slenderness ratio, R<sub>B</sub>, for bending members shall be calculated as follows:

$$R_B = \sqrt{\frac{\ell_e d}{b^2}} \quad (3.3-5)$$

3.3.3.7 The slenderness ratio for bending members, R<sub>B</sub>, shall not exceed 50.

3.3.3.8 The beam stability factor shall be calculated as follows:

$$C_L = \frac{1 + (F_{BE}/F_b^*)}{1.9} - \sqrt{\left[ \frac{1 + (F_{BE}/F_b^*)}{1.9} \right]^2 - \frac{F_{BE}/F_b^*}{0.95}} \quad (3.3-6)$$

where:

F<sub>b</sub>\* = reference bending design value multiplied by all applicable adjustment factors except C<sub>tu</sub>, C<sub>v</sub> (when C<sub>v</sub> ≤ 1.0), and C<sub>L</sub> (see 2.3), psi

$$F_{BE} = \frac{1.20 E_{min}'}{R_B^2}$$

# Adjustment Factors for Shear

## Allowable Flexure Stress F<sub>v</sub>'

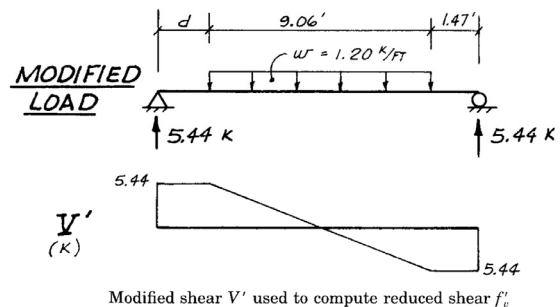
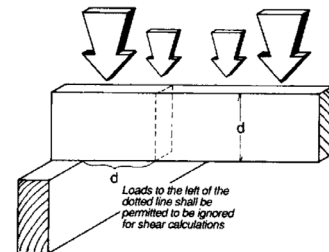
F<sub>v</sub> from tables determined by species and grade

$$F_v' = F_v \text{ (usage factors)}$$

Usage factors for shear:

- C<sub>D</sub> Load Duration Factor
- C<sub>M</sub> Moisture Factor
- C<sub>t</sub> Temperature Factor
- C<sub>i</sub> Incising Factor

### Shear at Supports



# Analysis Procedure

Given: loading, member size, material and span.

Req'd: Safe or Unsafe (Pass/Fail)

## 1. Find Max Shear & Moment

- Simple case – equations
- Complex case - diagrams

## 2. Determine actual stresses

- $f_b = M/S$
- $f_v = 1.5 V/A$

## 3. Determine allowable stresses

- $F_b$  and  $F_v$  (from NDS)
- $F_b' = F_b$  (usage factors)
- $F_v' = F_v$  (usage factors)

## 4. Check that actual $\leq$ factored allowable

- $f_b \leq F_b'$
- $f_v \leq F_v'$

## 5. Check deflection < building code max.

## 6. Check bearing ( $F_{cL} \geq \text{Reaction}/A_{\text{bearing}}$ )

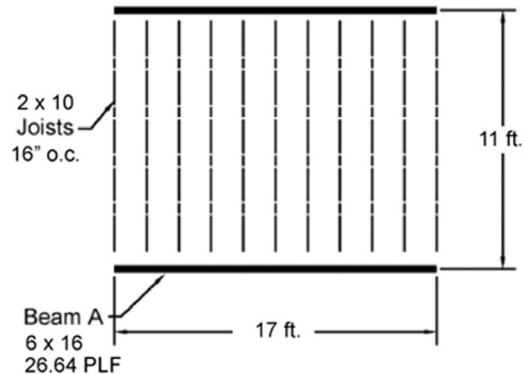
Nominal Size b x d	Standard Dressed Size (S4S) b x d in. x in.	Area of Section A in. <sup>2</sup>	X-X AXIS		Y-Y AXIS	
			Section Modulus $S_{xx}$ in. <sup>3</sup>	Moment of Inertia $I_{xx}$ in. <sup>4</sup>	Section Modulus $S_{yy}$ in. <sup>3</sup>	Moment of Inertia $I_{yy}$ in. <sup>4</sup>
<b>Boards<sup>1</sup></b>						
1 x 3	3/4 x 2-1/2	1.875	0.781	0.977	0.234	0.088
1 x 4	3/4 x 3-1/2	2.625	1.531	2.680	0.328	0.123
1 x 6	3/4 x 5-1/2	4.125	3.781	10.40	0.516	0.193
1 x 8	3/4 x 7-1/4	5.438	6.570	23.82	0.680	0.255
1 x 10	3/4 x 9-1/4	6.938	10.70	49.47	0.867	0.325
1 x 12	3/4 x 11-1/4	8.438	15.82	88.99	1.055	0.396
<b>Dimension Lumber (see NDS 4.1.3.2) and Decking (see NDS 4.1.3.5)</b>						
2 x 3	1-1/2 x 2-1/2	3.750	1.56	1.953	0.938	0.703
2 x 4	1-1/2 x 3-1/2	5.250	3.06	5.359	1.313	0.984
2 x 5	1-1/2 x 4-1/2	6.750	5.06	11.39	1.688	1.266
2 x 6	1-1/2 x 5-1/2	8.250	7.56	20.80	2.063	1.547
2 x 8	1-1/2 x 7-1/4	10.88	13.14	47.63	2.719	2.039
2 x 10	1-1/2 x 9-1/4	13.88	21.39	98.93	3.469	2.602
2 x 12	1-1/2 x 11-1/4	16.88	31.64	178.0	4.219	3.164
2 x 14	1-1/2 x 13-1/4	19.88	43.89	290.8	4.969	3.727
3 x 4	2-1/2 x 3-1/2	8.75	5.10	8.932	3.646	4.557
3 x 5	2-1/2 x 4-1/2	11.25	8.44	18.98	4.688	5.859
3 x 6	2-1/2 x 5-1/2	13.75	12.60	34.66	5.729	7.161
3 x 8	2-1/2 x 7-1/4	18.13	21.90	79.39	7.552	9.440
3 x 10	2-1/2 x 9-1/4	23.13	35.65	164.9	9.635	12.04
3 x 12	2-1/2 x 11-1/4	28.13	52.73	296.6	11.72	14.65
3 x 14	2-1/2 x 13-1/4	33.13	73.15	484.6	13.80	17.25
3 x 16	2-1/2 x 15-1/4	38.13	96.90	738.9	15.89	19.86
4 x 4	3-1/2 x 3-1/2	12.25	7.15	12.51	7.146	12.51
4 x 5	3-1/2 x 4-1/2	15.75	11.81	26.58	9.188	16.08
4 x 6	3-1/2 x 5-1/2	19.25	17.65	48.53	11.23	19.65
4 x 8	3-1/2 x 7-1/4	25.38	30.66	111.1	14.80	25.90
4 x 10	3-1/2 x 9-1/4	32.38	49.91	230.8	18.89	33.05
4 x 12	3-1/2 x 11-1/4	39.38	73.83	415.3	22.97	40.20
4 x 14	3-1/2 x 13-1/4	46.38	102.41	678.5	27.05	47.34
4 x 16	3-1/2 x 15-1/4	53.38	135.66	1034	31.14	54.49

from NDS 2012

# Analysis Example (pass/fail)

Given:

DATASET: 1 -2-	
Span A	17 FT
Span B	11 FT
Joist O.C. Spacing	16 IN
Wood Density	45 PCF
Joist Size	2x10 NOMINAL
Beam Size	6x16 NOMINAL
Floor DL (not including joist)	3 PSF
Occupancy or Use	assembly area - fixed seats



Req'd: pass or fail for floor joist



ASCE-7 Table 4.3-1: Live Load = 60 PSF

ASCE-7 2.4.1 ASD load case: D + L

2x10 Joist + floor load:

$$\begin{aligned}
 & D + L \\
 & \left( \text{SELF WEIGHT} + D \frac{\text{o.c.}}{12} \right) + \left( L \frac{\text{o.c.}}{12} \right) \\
 & \left( 4.336 \text{ PLF} + 3 \text{ PSF} \frac{16''}{12} \right) + \left( 60 \text{ PSF} \frac{16''}{12} \right) \\
 & 8.336 \text{ PLF} + 80 \text{ PLF} = 88.336 \text{ PLF}
 \end{aligned}$$



# Analysis Example (pass/fail)

ASCE-7 Table 4.3-1: Live Load = 60 PSF

ASCE-7 2.4.1 ASD load case: D + L

2x10 Joist + floor load:

Given:

DATASET: 1 -2-	
Span A	17 FT
Span B	11 FT
Joist O.C. Spacing	16 IN
Wood Density	45 PCF
Joist Size	2x10 NOMINAL
Beam Size	6x16 NOMINAL
Floor DL (not including joist)	3 PSF
Occupancy or Use	assembly area - fixed seats

$$D + L$$

$$\left( \text{SELF WEIGHT} + D \frac{O.C.}{12} \right) + \left( L \frac{O.C.}{12} \right)$$

$$\left( 4.336 \text{ PLF} + 3 \text{ PSF} \frac{16''}{12} \right) + \left( 60 \text{ PSF} \frac{16''}{12} \right)$$

$$8.336 \text{ PLF} + 80 \text{ PLF} = 88.336 \text{ PLF}$$

**Table 1B Section Properties of Standard Dressed (S4S) Sawn Lumber**

Nominal Size b x d	Standard Dressed Size (S4S) b x d in. x in.	Area of Section A in. <sup>2</sup>	X-X AXIS		Y-Y AXIS		Approximate weight in pounds per linear foot (lbs/ft) of piece when density of wood equals:					
			Section Modulus S <sub>xx</sub> in. <sup>3</sup>	Moment of Inertia I <sub>xx</sub> in. <sup>4</sup>	Section Modulus S <sub>yy</sub> in. <sup>3</sup>	Moment of Inertia I <sub>yy</sub> in. <sup>4</sup>	25 lbs/ft <sup>3</sup>	30 lbs/ft <sup>3</sup>	35 lbs/ft <sup>3</sup>	40 lbs/ft <sup>3</sup>	45 lbs/ft <sup>3</sup>	50 lbs/ft <sup>3</sup>
							Dimension Lumber (see NDS 4.1.3.2) and Decking (see NDS 4.1.3.5)					
2 x 3	1-1/2 x 2-1/2	3.750	1.56	1.953	0.938	0.703	0.651	0.781	0.911	1.042	1.172	1.302
2 x 4	1-1/2 x 3-1/2	5.250	3.06	5.359	1.313	0.984	0.911	1.094	1.276	1.458	1.641	1.823
2 x 5	1-1/2 x 4-1/2	6.750	5.06	11.39	1.688	1.266	1.172	1.406	1.641	1.875	2.109	2.344
2 x 6	1-1/2 x 5-1/2	8.250	7.56	20.80	2.063	1.547	1.432	1.719	2.005	2.292	2.578	2.865
2 x 8	1-1/2 x 7-1/4	10.88	13.14	47.63	2.719	2.039	1.888	2.266	2.643	3.021	3.398	3.776
2 x 10	1-1/2 x 9-1/4	13.88	21.39	98.93	3.469	2.602	2.409	2.891	3.372	3.854	4.336	4.818
2 x 12	1-1/2 x 11-1/4	16.88	31.64	178.0	4.219	3.164	2.930	3.516	4.102	4.688	5.273	5.859
2 x 14	1-1/2 x 13-1/4	19.88	43.89	290.8	4.969	3.727	3.451	4.141	4.831	5.521	6.211	6.901

# Analysis Example (pass/fail)

1. Find Max Shear & Moment on Joist

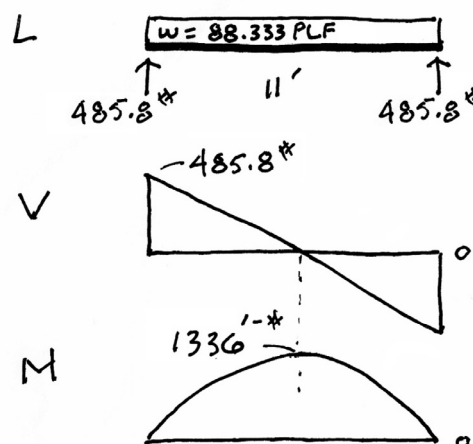
By equations:

Shear:

$$\frac{wl}{2} = \frac{88.336 (11)}{2} = 485.848 \text{ lbs}$$

Moment:

$$\frac{wl^2}{8} = \frac{88.336 (11^2)}{8} = 1336.08 \text{ ft-lbs}$$



# Analysis Example (pass/fail)

2. Determine actual stresses in joists

- $f_b = M/S$
- $f_v = 1.5 V/A$

$$f_b = \frac{M}{S_x} = \frac{1336 \text{ ft} \cdot \text{lb} (12)}{21.39 \text{ in}^3} = 749.5 \text{ psi}$$

$$f_v = \frac{3}{2} \frac{V}{A} = \frac{1.5 (485.8) \text{ lb}}{13.88 \text{ in}^2} = 52.5 \text{ psi}$$

**Table 1B Section Properties of Standard Dressed (S4S) Sawn Lumber**

Nominal Size b x d	Standard Dressed Size (S4S) b x d in. x in.	Area of Section A in. <sup>2</sup>	X-X AXIS		Y-Y AXIS		Approximate weight in pounds per linear foot (lbs/ft) of piece when density of wood equals:					
			Section Modulus S <sub>xx</sub> in. <sup>3</sup>	Moment of Inertia I <sub>xx</sub> in. <sup>4</sup>	Section Modulus S <sub>yy</sub> in. <sup>3</sup>	Moment of Inertia I <sub>yy</sub> in. <sup>4</sup>	25 lbs/ft <sup>3</sup>	30 lbs/ft <sup>3</sup>	35 lbs/ft <sup>3</sup>	40 lbs/ft <sup>3</sup>	45 lbs/ft <sup>3</sup>	50 lbs/ft <sup>3</sup>
<b>Dimension Lumber (see NDS 4.1.3.2) and Decking (see NDS 4.1.3.5)</b>												
2 x 3	1-1/2 x 2-1/2	3.750	1.56	1.953	0.938	0.703	0.651	0.781	0.911	1.042	1.172	1.302
2 x 4	1-1/2 x 3-1/2	5.250	3.06	5.359	1.313	0.984	0.911	1.094	1.276	1.458	1.641	1.823
2 x 5	1-1/2 x 4-1/2	6.750	5.06	11.39	1.688	1.266	1.172	1.406	1.641	1.875	2.109	2.344
2 x 6	1-1/2 x 5-1/2	8.250	7.56	20.80	2.063	1.547	1.432	1.719	2.005	2.292	2.578	2.865
2 x 8	1-1/2 x 7-1/4	10.88	13.14	47.63	2.719	2.039	1.888	2.266	2.643	3.021	3.398	3.776
2 x 10	1-1/2 x 9-1/4	13.88	21.39	98.93	3.469	2.602	2.409	2.891	3.372	3.854	4.336	4.818
2 x 12	1-1/2 x 11-1/4	16.88	31.64	178.0	4.219	3.164	2.930	3.516	4.102	4.688	5.273	5.859
2 x 14	1-1/2 x 13-1/4	19.88	43.89	290.8	4.969	3.727	3.451	4.141	4.831	5.521	6.211	6.901

# Analysis Example (pass/fail)

3. Determine allowable stresses – NDS Supplement

- $F_b = 875 \text{ psi}$
- $F_v = 135 \text{ psi}$



Species and Grade

**Table 4A Reference Design Values for Visually Graded Dimension Lumber (Cont.) (2" - 4" thick)<sup>1,2,3</sup>**

(All species except Southern Pine— see Table 4B) (Tabulated design values are for normal load duration and dry service conditions. See NDS 4.3 for a comprehensive description of design value adjustment factors.)

**USE WITH TABLE 4A ADJUSTMENT FACTORS**

Species and commercial grade	Size classification	Design values in pounds per square inch (psi)						Modulus of Elasticity	Specific Gravity <sup>4</sup>	Grading Rules Agency	
		Bending F <sub>b</sub>	Tension parallel to grain F <sub>t</sub>	Shear parallel to grain F <sub>v</sub>	Compression perpendicular to grain F <sub>c⊥</sub>	Compression parallel to grain F <sub>c</sub>	Modulus of Elasticity				
							E				E <sub>min</sub>
<b>SPRUCE-PINE-FIR</b>											
Select Structural		1,250	700	135	425	1,400	1,500,000	550,000			
No. 1/ No. 2	2" & wider	875	450	135	425	1,150	1,400,000	510,000			
No. 3		500	250	135	425	650	1,200,000	440,000			
Stud	2" & wider	675	350	135	425	725	1,200,000	440,000	0.42	NLGA	
Construction		1,000	500	135	425	1,400	1,300,000	470,000			
Standard	2" - 4" wide	550	275	135	425	1,150	1,200,000	440,000			
Utility		275	125	135	425	750	1,100,000	400,000			

# Analysis Example (pass/fail)



- Determine allowable stresses – NDS Supplement
  - Adjustment Factors

Determine factors:

- CD = ?
- CM = 1
- Ct = 1
- CL = ?
- CF = ?
- Cfu = 1
- Ci = 1
- Cr = ?

**Table 4.3.1 Applicability of Adjustment Factors for Sawn Lumber**

		ASD only	ASD and LRFD										LRFD only		
		Load Duration Factor	Wet Service Factor	Temperature Factor	Beam Stability Factor	Size Factor	Flat Use Factor	Incising Factor	Repetitive Member Factor	Column Stability Factor	Buckling Stiffness Factor	Bearing Area Factor	Format Conversion Factor	Resistance Factor	Time Effect Factor
$F_b' = F_b$	x	C <sub>D</sub>	C <sub>M</sub>	C <sub>t</sub>	C <sub>L</sub>	C <sub>F</sub>	C <sub>fu</sub>	C <sub>i</sub>	C <sub>r</sub>	-	-	-	K <sub>F</sub>	φ <sub>b</sub>	λ
$F_v' = F_v$	x	C <sub>D</sub>	C <sub>M</sub>	C <sub>t</sub>	-	-	-	C <sub>i</sub>	-	-	-	-	K <sub>F</sub>	φ <sub>v</sub>	λ

# Analysis Example (pass/fail)

**Table 2.3.2 Frequently Used Load Duration Factors, C<sub>D</sub><sup>1</sup>**

C<sub>D</sub> Load duration factor

Occupancy LL (10 years) = 1.0

Load Duration	C <sub>D</sub>	Typical Design Loads
Permanent	0.9	Dead Load
Ten years	1.0	Occupancy Live Load
Two months	1.15	Snow Load
Seven days	1.25	Construction Load
Ten minutes	1.6	Wind/Earthquake Load
Impact <sup>2</sup>	2.0	Impact Load

C<sub>F</sub> Size factor

2 x 10  
use 1.1

Size Factors, C<sub>F</sub>

Grades	Width (depth)	F <sub>b</sub>		F <sub>t</sub>	F <sub>c</sub>
		Thickness (breadth)			
		2" & 3"	4"		
Select Structural, No.1 & Btr, No.1, No.2, No.3	2", 3", & 4"	1.5	1.5	1.5	1.15
	5"	1.4	1.4	1.4	1.1
	6"	1.3	1.3	1.3	1.1
	8"	1.2	1.3	1.2	1.05
	10"	1.1	1.2	1.1	1.0
	12"	1.0	1.1	1.0	1.0
Stud	14" & wider	0.9	1.0	0.9	0.9
	2", 3", & 4"	1.1	1.1	1.1	1.05
	5" & 6"	1.0	1.0	1.0	1.0
Use No.3 Grade tabulated design values and size factors					
Construction, Standard	2", 3", & 4"	1.0	1.0	1.0	1.0
Utility	4"	1.0	1.0	1.0	1.0
	2" & 3"	0.4	—	0.4	0.6

# Analysis Example (pass/fail)

## $C_r$ Repetitive Member Factor

16" o.c. :  $C_r = 1.15$

### Repetitive Member Factor, $C_r$

Bending design values,  $F_b$ , for dimension lumber 2" to 4" thick shall be multiplied by the repetitive member factor,  $C_r = 1.15$ , when such members are used as joists, truss chords, rafters, studs, planks, decking, or similar members which are in contact or spaced not more than 24" on center, are not less than 3 in number and are joined by floor, roof, or other load distributing elements adequate to support the design load.

# Analysis Example (pass/fail)

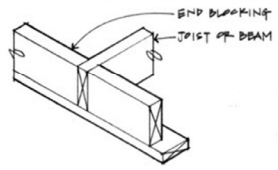
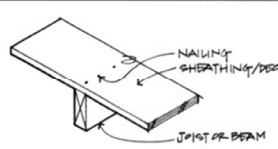
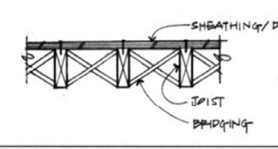
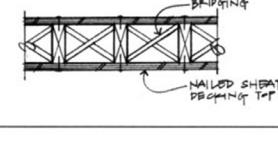
## $C_L$ Beam Stability Factor

2x10 w/ flooring:  $C_L = 1.0$

$C_L = 1.0$   
if depth/width ratio meets criteria  
in 4.4.1  $C_L = 1.0$

Otherwise:

$C_L < 1.0$   
calculate factor using section 3.3.3

Beam Depth/ Width Ratio	Type of Lateral Bracing Required	Example
2 to 1	None	
3 to 1 2x6 2x8	The ends of the beam should be held in position	
5 to 1 2x10	Hold compression edge in line (continuously)	
6 to 1 2x12	Diagonal bridging should be used	
7 to 1 2x14	Both edges of the beam should be held in line	

## Analysis Example (pass/fail)

### 3. Determine factored allowable stresses

- $F_b' = F_b (C_D)(C_L)(C_F)(C_r)$
- $F_b' = 875 (1.0) (1.0) (1.1) (1.0) (1.15) = 1107 \text{ psi}$
- $F_v' = F_v (C_D)$
- $F_v' = 135 (1.0) = 135 \text{ psi}$

### 4. Check that actual $\leq$ factored allowable

- $f_b < F_b'$
- $f_v < F_v'$

$$f_b = \frac{M}{S_x} = \frac{1336' \cdot (12)}{21.39 \text{ in}^3} = 749.5 \text{ psi}$$

$$f_v = \frac{3}{2} \frac{V}{A} = \frac{1.5 (485.8)'}{13.88 \text{ in}^2} = 52.5 \text{ psi}$$

### 5. Check deflection

### 6. Check bearing ( $F_{cp} = R/A_b$ )

## Analysis Example (pass/fail)

### 5. Check deflection < Code limits

- NDS 3.5
- $\Delta_{LT}$  - Long term
- $\Delta_{ST}$  - Short term
- $K_{cr}$  - creep factor

$$\Delta_T = K_{cr} \Delta_{LT} + \Delta_{ST} \quad (\text{NDS 3.5-1})$$

$K_{cr}$

- 1.5 dry, seasoned lumber
- 2.0 wet service conditions
- 2.0 wood panels
- 2.0 CLT (dry)

TABLE 1604.3 DEFLECTION LIMITS<sup>a, b, c, h, i</sup>

CONSTRUCTION	L	S or W <sup>f</sup>	D + L <sup>d, g</sup>
Roof members: <sup>e</sup>			
Supporting plaster or stucco ceiling	//360	//360	//240
Supporting nonplaster ceiling	//240	//240	//180
Not supporting ceiling	//180	//180	//120
Floor members	//360	—	//240
Exterior walls:			
With plaster or stucco finishes	—	//360	—
With other brittle finishes	—	//240	—
With flexible finishes	—	//120	—
Interior partitions: <sup>b</sup>			
With plaster or stucco finishes	//360	—	—
With other brittle finishes	//240	—	—
With flexible finishes	//120	—	—
Farm buildings	—	—	//180
Greenhouses	—	—	//120

$\Delta_{ST}$

$$\Delta_L = \frac{5wL^4}{384EI} = \frac{5(80 \text{ PLF})(11 \text{ FT})^4 (1728)}{384(1400000 \text{ PSI})(98.93 \text{ in}^4)}$$

$$\Delta_L = 0.19''$$

$$\frac{P}{360} = \frac{11 \text{ FT}(12)}{360} = 0.367''$$

$\Delta_{LT}$

$$\Delta_D = \frac{5wL^4}{384EI} = \frac{5(8.34 \text{ PLF})(11 \text{ FT})^4 (1728)}{384(1400000 \text{ PSI})(98.93 \text{ in}^4)}$$

$$\Delta_D = 0.02''$$

$$K_{cr} = 1.5$$

$$\Delta_T = K_{cr} \Delta_{LT} + \Delta_{ST}$$

$$= 1.5(0.02) + 0.19 = 0.22''$$

$$\frac{P}{240} = \frac{11 \text{ FT}(12)}{240} = 0.55''$$

## Analysis Example (pass/fail)

6. Check bearing :  $F_{c\perp} < P/A_b$

$$F_{c\perp} = 425 \text{ psi}$$

$$P = R = 485.8 \text{ lbs}$$

$$A_b = 1.5'' (1'') = 1.5 \text{ in}^2$$

$$f_b = \frac{485.8}{1.5} = 323.8 \text{ psi} < 425 \text{ psi} \quad \text{ok}$$

### 3.10.4 Bearing Area Factor, $C_b$

Reference compression design values perpendicular to grain,  $F_{c\perp}$ , apply to bearings of any length at the ends of a member, and to all bearings 6" or more in length at any other location. For bearings less than 6" in length and not nearer than 3" to the end of a member, the reference compression design value perpendicular to grain,  $F_{c\perp}$ , shall be permitted to be multiplied by the following bearing area factor,  $C_b$ :

$$C_b = \frac{\ell_b + 0.375}{\ell_b} \quad (3.10-2)$$

where:

$\ell_b$  = bearing length measured parallel to grain, in.

Equation 3.10-2 gives the following bearing area factors,  $C_b$ , for the indicated bearing length on such small areas as plates and washers:

**Table 3.10.4 Bearing Area Factors,  $C_b$**

$\ell_b$	0.5"	1"	1.5"	2"	3"	4"	6" or more
$C_b$	1.75	1.38	1.25	1.19	1.13	1.10	1.00

For round bearing areas such as washers, the bearing length,  $\ell_b$ , shall be equal to the diameter.