Structure II Recitation 2/9

Steel Beam Analysis

Before we start ...

Today's Tasks

- 1. Homework Example (Steel Beam Analysis) (17 Questions)
- 2. Lab (Steel Beams)

<u>Reminder</u>

- 1. Don't forget to start your report!
- 2. Scale besides Peter's office if needed.



Videos of Old Tower Tests



Go to Structure Website >> Tower 1

Architecture 324 Structures II

Prof. Peter von Buelow Winter 2024

Tower Project

Description

This project gives students the chance to apply concepts learned in column analysis to the design of a structural system that carries primarily a compression load – a tower. Work is to be done in groups of up to four people. The project is divided into 3 parts: 1) initial conceptual design, 2) design development and testing, 3) final analysis and documentation.

Goals

- to explore design parameters of geometry and material under compression.
- to develop a design of a compression member to meet the criteria below.
- to make some rough hand calculation to estimate the expected performance.
- to test the compression member and record the results.
- to document the results in a well organized and clear report format.

Criteria

- The tower is to be made of wood. Either linear wood (sticks) or wood panels (sheets) can be used. Glue can be used to connect the elements. Gusset plates at the joints are allowed and can also be glued. But no steel pins or fasteners may be used.
- · Wood: any species. maximum cross-sectional dimension = 1/4".
- NO paper, mylar or plastic or string or dental floss.
- If a member is made by laminating multiple pieces together, the maximum cross-sectional dimension or thickness still cannot exceed 1/4*.
- The height of the tower = 48".
- The tower must hold at least 50 lbs.
- · The entire tower can weigh no more than 4 oz.
- The top of the tower must be loadable. The weights will be stacked on top of the tower, but you
 may optionally use a loose piece of MDF or plywood as a tray under the weights. (It will not be
 counted in either weight or load)
- Towers will be graded on their low weight, high load-carrying capacity, and the load/weight ratio. The evaluation formula is:

(4/weight in OZ) + (load in LBS/50) + (load LBS/weight OZ)x1.5

The score will be normalized to a range of 50 to 100. It is used together with report scores to
assess your project (a detailed evaluation form is given separately).

Procedure

- 1. Develop a structural concept for a tower meeting the above criteria.
- 2. Analyze the design concept with either hand calculations or a computer program (e.g. Dr. Frame)
- 3. Determine the capacity of the major members and of the overall tower (total capacity in LBS)
- 4. Estimate your expected score using the formula above.
- 5. Write the preliminary report.
- 6. Construct the structural model.
- Test the model. 5-pound steel bars will be placed on top of the model, until the model fails. (bar size: 1 ½" x 2" x 5 13/16").
- 8. Produce final report documenting requirements and process. See also score sheet.

Due Dates	Scoring	
See Course Schedule	Preliminary Report	40 pts
	Testing	60 pts
	Final Report	150 pts

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Tower Project – Preliminary Report Requirements

- Explanation describe how the design was developed, the basis of the structural concept, and how the principles of column behavior influenced the design decisions.
- Illustration include diagrams/drawings that describe the structure in its entirety. At least a horizontal crosssection and an elevation of the tower are required. Dimensions are to be included and the member sizes labeled.

Analysis - the report should include the following:

- Choose wood type and stress properties. Either use values below for typical model grade Basswood
 or use values in the NDS or find test values online. Indicate in the report which values you choose.
- Determine the cross-sectional area of each member. Find the axial force P and the allowable stress
 F'c. The force P can be determined either by a hand calculated truss analysis or as a second order
 analysis in Dr. Frame or STAAD.Pro. The stress F'c should be found using the NDS equations for CP
 and F'c. Other NDS stress adjustment factors (Co, Cu, C, C, and Ci) can be taken equal to 1.0. Size
 members based on the predicted load, P and the allowable stress F'c. Target (or predict) some total
 capacity load for the tower. A minimum of 50 LBS is required. Then size the members based on the
 force in each member.
- Predict the total weight of the tower. Provide a table with each member type showing, length, section
 and weight for each. Make an estimate of the weight added by glue joints and/or gusset plates. The total
 weight should be under 4 OZ.
- Predict Capacity. Predict the ultimate capacity in pounds that the entire tower can carry based on the
 actual cross-sections chosen. Produce a ultilization table to show for each member type (e.g. main
 vertical, horizontal tie, diagonal brace) the utilization ratio fc/F'c based on the predicted total capacity
 load. This ratio should be below 1.0 for all members.
- Calculate the buckling capacity of the tower as a whole. This is done by treating the tower as one
 column loaded at the top, made up in cross section of multiple columns. Show the moment of inertia of
 the tower cross-section, and use it to calculate the critical buckling load using the Euler equation. An
 example of this calculation is given in the slides from the class lecture. The ultimate capacity is the lower
 of the two capacities (critical member or tower as a whole).

Note: If an excel spreadsheet is used to make calculations, show the equations being used for each cell or column in the table. If STAAD.Pro or Dr. Frame is used to do any of the above, include print-outs showing the applied loads and resulting member forces.

Format - Reports should be formatted for 8½ X 11 paper. 11X17 format reports will not be accepted. Once returned to you graded, save the original copy of the preliminary report for submission together with the Final Report.

The report is a professional document. Text should be clear, grammatically correct, and language should be appropriate and professional. All calculations should be legible and clearly described – not just numbers or results, but with a clear description of what is being calculated included.

Properties of Basswood: (like	in the Media Center)
Density (oven dry)	20 pcf *
E (buckling)	1,650,000 psi **
F (Compression to grain)	4745 psi *
F (Compression 1 to grain)	377 psi *
F (Tension to grain)	4500 psi (estimate)
F (Tension ⊥ to grain)	348 psi *
F (Shear to grain)	986 psi *
F (Flexure)	5900 psi *
* from http://www.matweb.com/	** tested by PvB (small pieces in compression)

Winter 2024	ARCH 324 001 WN 2024 > Files	> Steel
Home Modules Ø	Search for files Q (
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4. Steel Beam Analysis

Analyze the given W-section for beam B1, to determine the maximum live load capacity the floor can carry. Determine the shear and bending forces and check the maximum deflection against an allowable of L/180. Assume the beam is fully braced, Lb < Lp (zone 1).

DATASET: 1	-23-	
W-section		W12X45
Fy		50 KSI
Span A		25 FT
Span B		12 FT
Floor DL		18 PSF



1. Find out LL, 2. Compare Shear, 3. Compare Deflection

Example - Analysis of Steel Beam - Capacity

Find applied live load capacity, w_{LL} in KLF $w_u = 1.2w_{DL} + 1.6w_{LL}$ $w_{DL} = beam + floor = 44plf + 1500plf$ Fy = 50 ksi, Fully Braced

 Find the Plastic Modulus (Z_x) for the given section from the AISC table 1-1

2. Check that $L_b < L_p$ (fully braced – ok)

3. Determine $M_n = M_p = F_y Z_x$

4. Set
$$M_u = \phi_b M_n$$

 $\phi_b = 0.90$



Example – Analysis of Steel Beam - Capacity

 Using the maximum moment equation, solve for the factored distributed loading, w_u

$$M_{u}: \frac{\omega_{u}}{8} \stackrel{l^{2}}{\Rightarrow} \omega_{u}: \frac{\mathcal{B}M_{u}}{l^{2}}$$

$$\omega_{u}: \frac{\mathcal{B} \times 357.75}{20} \frac{\mathcal{E}T}{r}$$

$$\omega_{u}: 7.155 \frac{\mathcal{E}T}{r}$$

7. The applied (unfactored) load $w = w_u / (\gamma \text{ factors})$ $w_u = 1.2 \text{wDL} + 1.6 \text{wLL}$

$$w_{0L} = 7.155 \text{ KLF} = 1.2(0.044 + 1.5) + 1.6(w_{LL})$$
$$w_{0} = 1.853 + 1.6 w_{LL} = 7.155 \text{ KLF}$$
$$w_{LL} = 3.31 \text{ KLF}$$

Q1: Plastic Modulus of the Section (Zx) Check AISC 14, Table 1-1, for me p.8(PDF): For W12 x 45, $Zx = \underline{64.2 \text{ in}}^3$

Q2: Nominal Bending Moment (Mn) Since its full bracing (Zone 1): Mn = (Zx) x (Fy) = 64.2 x 50 = 3210 k-in







Q3: The Factored Bending Resistance (Φ Mn) $\Phi = 0.9$ Φ Mn = Mn x 0.9 = 3210 x 0.9 = <u>2889 k-in</u>

Q4: The Factored Design Moment (Mu) We assume $Mu = \Phi$ Mn in order to find our LL: $Mu = (\Phi Mn) = 2889 / 12 = 240.75$ k-ft

Convert Unit

Q5: The Total Factored Design Load (wu) Moment for uniformly distributed load = (w x $L^2 / 8$) wu = Mu x 8 / L^2 = 240.75 x 8 / 25² = <u>3.0816 klf</u>



 $\phi M_n = 0.90 M_n$

1. SIMPLE BEAM—UNIFORMLY DISTRIBUTED LOAD



Given from Question

Q6: The Total Unfactored Dead Load (w_DL) <u>Consider: Beam Self Weight + Dead Load</u> For Beam Self Weight: Check AISC 14, Table 1-1 for Nominal Weight, For my situation, self weight = 45 lb/ft

For Dead Load: Floor DL x Tributary Area / Beam Length (Span A) = Floor DL x Span B = 18 x 12 = 216 lb/ft

Convert Unit (pounds to kips) Total: (45 + 216) / 1000 = <u>0.261 klf</u>

Q7: The Total Factored Dead Load (wu_DL) wu_DL = w_DL x 1.2 = 0.261 x 1.2 = <u>0.3132 klf</u>

					Web			Fla	ange			[Distanc	e	
Area, Shape A		Area, Depth,		Thickness,		tw	Width,		Thick	iess,		k	ŀ	-	Work-
Suape	A	'	u	tv	v	2		bf	t		k des	k _{det}	K 1	'	Gage
	in. ²	i	n.	in		in.	i	n.	in		in.	in.	in.	in.	in.
W12×58	17.0	12.2	121/4	0.360	3/8	3/16	10.0	10	0.640	5/8	1.24	11/2	15/16	91/4	5 ¹ /2
×53	15.6	12.1	12	0.345	3/8	³ /16	10.0	10	0.575	⁹ /16	1.18	1 ³ /8	15/16	91/4	51/2
W12×50	14.6	12.2	121/4	0.370	3/8	³ /16	8.08	8 ¹ /8	0.640	5/8	1.14	11/2	15/16	9 ¹ /4	5 ¹ /2
×45	13.1	12.1	12	0.335	5/16	³ /16	8.05	8	0.575	⁹ /16	1.08	13/8	15/16		
×40	11.7	11.9	12	0.295	⁹ /16	3/16	8.01	8	0.515	1/2	1.02	13/8	⁷ /8	Ť	Ť
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Nom- inal	Com Sec	pact tion	Axis X-X					Axis	5 Y-Y		rts	ho	Torsional Properties	
Wt.	4	h	1	S	r	Z	1	S	r	Z			J	Cw
lb/it	2t _f	tw	in.4	in. ³	in.	in. ³	in.4	in. ³	in.	in. ³	in.	in.	in.4	in.6
58	7.82	27.0	475	78.0	5.28	86.4	107	21.4	2.51	32.5	2.81	11.6	2.10	3570
53	8.69	28.1	425	70.6	5.23	77.9	95.8	19.2	2.48	29.1	2.79	11.5	1.58	3160
50	6.31	26.8	391	64.2	5.18	71.9	56.3	13.9	1.96	21.3	2.25	11.6	1.71	1880
45	7.00	29.6	348	57.7	5.15	64.2	50.0	12.4	1.95	19.0	2.23	11.5	1.26	1650
40	7.77	33.6	307	51.5	5.13	57.0	44.1	11.0	1.94	16.8	2.21	11.4	0.906	1440

Q8: The Factored Live Load (wu_LL) wu_LL = wu - wu_DL = 3.0816 - 0.03132 = 2.7684 klf From Q5 From Q7 Q9: The Actual Beam Live Load (w_LL) w_LL = wu_LL / 1.6 = 2.7684 / 1.6 = 1.73025 klf

Q10: The Actual Floor Live Load (LL) LL = w_LL / Span B = (1.73025 / 12) x 1000 = <u>144.1875 psf</u>

Convert Unit (kips to pounds)

W-section	W12X45
Fy	50 KSI
Span A	25 FT
Span B	12 FT
Floor DL	18 PSF

Given from Question





Q11: The Maximum Factored Design Beam Shear Force (Vu_max):

Formula: Aw = d x tw

Check AISC 14, Table 1-1 for d & tw:

 $Aw = 12.1 \ge 0.335 = 4.0535 \text{ in}^2$





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	Area,	De	pth,	Thie	Wet			F Width.	lange Thick	ness.		k	Distan	ce	Work-	Nominal	Co	mpact ection	t	A	xis)	(-X			Axis	s Y-Y		I ts	ha	Tors Prop	ional erties
Shape	A		d		tw	2		b _f	1	t _f	k _{des}	k _{det}	- <i>k</i> ₁	T	able Gage	Wt.		h	1		S	r	Z	1	S	r	Z	-		J	Cw
	in. ²	i	n.		in.	in.		in.	i	n.	in.	in.	in.	in.	in.	lb/ft	t 21,	tw	in.	4 ir	1.3	in.	in. ³	in.4	in.3	in.	in. ³	in.	in.	in.4	in.6
W12×58	17.0	12.2	121/4	0.3	i0 ³ /8	3/1	3 10.	0 10	0.640	5/8	1.24	11/2	15/16	91/4	51/2	58	7.8	2 27.0	0 47	5 7	8.0	5.28	86.4	107	21.4	2.51	32.5	2.81	11.6	2.10	357
×53	15.6	12.1	12	0.34	5 3/8	3/1	3 10.	.0 10	0.575	9/16	1.18	13/8	15/16	91/4	51/2	53	8.6	9 28.1	1 42	5 7	0.6	5.23	77.9	95.8	19.2	2.48	29.1	2.79	11.5	1.58	316
W12×50	14.6	12.2	121/4	0.3	0 3/8	3/1	6 8.	08 81/8	0.640	5/8	1.14	11/2	15/16	91/4	51/2	50	6.3	1 26.8	3 39	1 6	4.2	5.18	71.9	56.3	13.9	1.96	21.3	2.25	11.6	1.71	188
×45	13.1	12.1	12	0.33	5/16	3/1	6 8.	.05 8	0.575	9/16	1.08	13/8	15/16	1		45	7.0	0 29.6	6 34	8 5	7.7	5.15	64.2	50.0	12.4	1.95	19.0	2.23	11.5	1.26	165
×40	11.7	11.9	12	0.29	15 9/16	3/1	6 8.	.01 8	0.515	1/2	1.02	13/8	1/8			40	7.7	7 33.6	6 30	7 5	1.5	5.13	57.0	44.1	11.0	1.94	16.8	2.21	11.4	0.906	144

Q13: The Factored Shear Resistance (phi Vn) Check my h/tw, Since my h/tw = 29.6 < 59, phi Vn = 0.6 x Fy x Aw = 0.6 x 50 x 4.0535 = 121.605 k

Q14: Is the section safe for shear? From Q12

For my situation: 121.605 (phi Vn) > 38.52 (Vu_max), **It's a Pass!**

Given from Question

W-section	W12X45
Fy	50 KSI
Span A	25 FT
Span B	12 FT
Floor DL	18 PSF

AISC 14, Table 1-1

Nom- inal	Com Sec	pact tion		Axis 2	(-X			Axis	Y-Y		r _{ts}	h _o	Tors Prop	ional erties
Wt.	b	h	1	S	r	Z	1	S	r	Z			J	Cw
lb/ft	2tr	tw	in.4	in. ³	in.	in. ³	in.4	in. ³	in.	in. ³	in.	in.	in.4	in.6
58	7.82	27.0	475	78.0	5.28	86.4	107	21.4	2.51	32.5	2.81	11.6	2.10	3570
53	8.69	28.1	425	70.6	5.23	77.9	95.8	19.2	2.48	29.1	2.79	11.5	1.58	3160
50	6.31	26 8	391	64.2	5.18	71.9	56.3	13.9	1.96	21.3	2.25	11.6	1.71	1880
45	7.00	29.6	348	57.7	5.15	64.2	50.0	12.4	1.95	19.0	2.23	11.5	1.26	1650
40	7.77	33.6	307	51.5	5.13	57.0	44.1	11.0	1.94	16.8	2.21	11.4	0.906	1440



then: $V_n = 0.6 F_y A_w (2.45 \sqrt{E/F}) / \frac{h}{1}$

Zone 3: ELASTIC WEB BUCKLING

if $3.07 \sqrt{E/F_{\gamma}} < \frac{h}{t_{w}} \le 260$ then: $V_n = A_w \left[\frac{\frac{4.25 E}{(\frac{h}{t_w})^2}}{\frac{h}{(\frac{h}{t_w})^2}} \right]$

Course Slides p.5

Q15: The Actual (Unfactored) Deflection Due to Total DL+LL

Deflection =
$$(5 \times x \times L^4) / (384 \times E \times I)$$

(E = 29000 ksi)

(I: Check AISC 14, Table 1-1, I = 348)

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(L: Given from question (Span A))
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(w = w LL + w DL = 1.73025 + 0.261 = 1.991)

Actual Deflection Actual Deflection Unfactored Loads $(Q^{9}+Q^{6})$ = $(5 \times 1.991 \times 25^{4}) / (384 \times 29000 \times 348) \times (12)^{3}$ =<u>1.734 in</u>

Convert Unit

Q16: The Deflection Limit (L/180) $L/180 = 25(Span A) \times 12/180 = 1.667 in$

Convert Unit

Q17: Maximum Allowable Axial Load Capacity (Pmax)

Check if the actual deflection (Q15) is smaller than the deflection limit (Q16), If yes = Pass, If no = Fail,

AISC 9, Beam Equations, p.2 (PDF)

E = Modulus of Elasticity of steel at 29,000 ksi.



Nom- inal	Com Sec	pact tion		Axis X-X					Y-Y		r _{ts}	ha	Tors Prop	ional erties
Wt.	b,	h	1	S	r	Z	1	S	r	Z	-		J	Cw
lb/ft	2tf	tw	in 4	in. ³	in.	in. ³	in.4	in. ³	in.	in. ³	in.	in.	in.4	in.6
58	7.82	27.0	475	78.0	5.28	86.4	107	21.4	2.51	32.5	2.81	11.6	2.10	3570
53	8.69	28.1	4 <mark>2</mark> 5	70.6	5.23	77.9	95.8	19.2	2.48	29.1	2.79	11.5	1.58	3160
50	6.31	26.8	391	64.2	5.18	71.9	56.3	13.9	1.96	21.3	2.25	11.6	1.71	1880
45	7.00	29.6	348	57.7	5.15	64.2	50.0	12.4	1.95	19.0	2.23	11.5	1.26	1650
40	7.77	33.6	307	51.5	5.13	57.0	44.1	11.0	1.94	16.8	2.21	11.4	0.906	1440

AISC 14, Table 1-1

For my situation: 1.734 > 1.667, **It's a Fail!**

Questions?

We're Done Here

RUUUM

Lab Session:

Goals:

Compare the load capacity of a free edge member in different orientations.

Steps:

1. Record the total number of washers each orientation holds when it fails.

2. Compare which one carries more load.

Structures II

Arch 324

Name 1	
Name 2	
Name 3	

Steel Beams

Description

This project uses observation to understand how unbraced compression edges and lateral torsional buckling reduce the ultimate load capacity of steel beams.

Goals

To observe the behavior of unbraced section edges in compression vs tension. To measure capacity loss due to lateral torsional buckling.

Procedure

- 1. Position the U shaped section with the free edges on the upper side of the span.
- Test how many washers the section can support at mid span. Use a wood block to position the load. Observe the mode (how) it fails.
- 3. Repeat the procedure with the section inverted and the free edges downward.
- Compare the load level carried by each orientation of the paper beam and describe the behavior under load.

