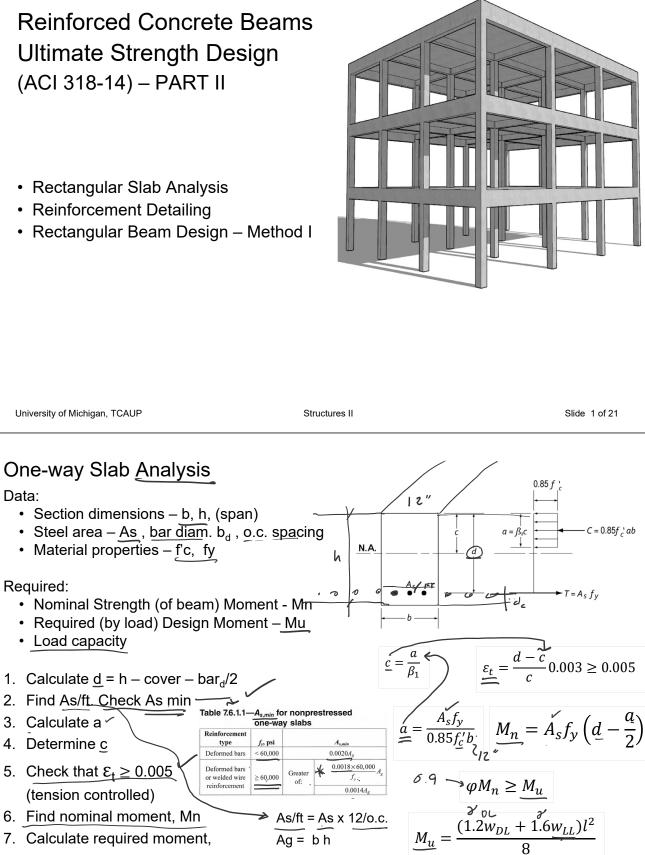
### Architecture 324 Structures II

Reinforced Concrete Beams Ultimate Strength Design (ACI 318-14) - PART II

- Rectangular Slab Analysis
- Reinforcement Detailing
- Rectangular Beam Design Method I

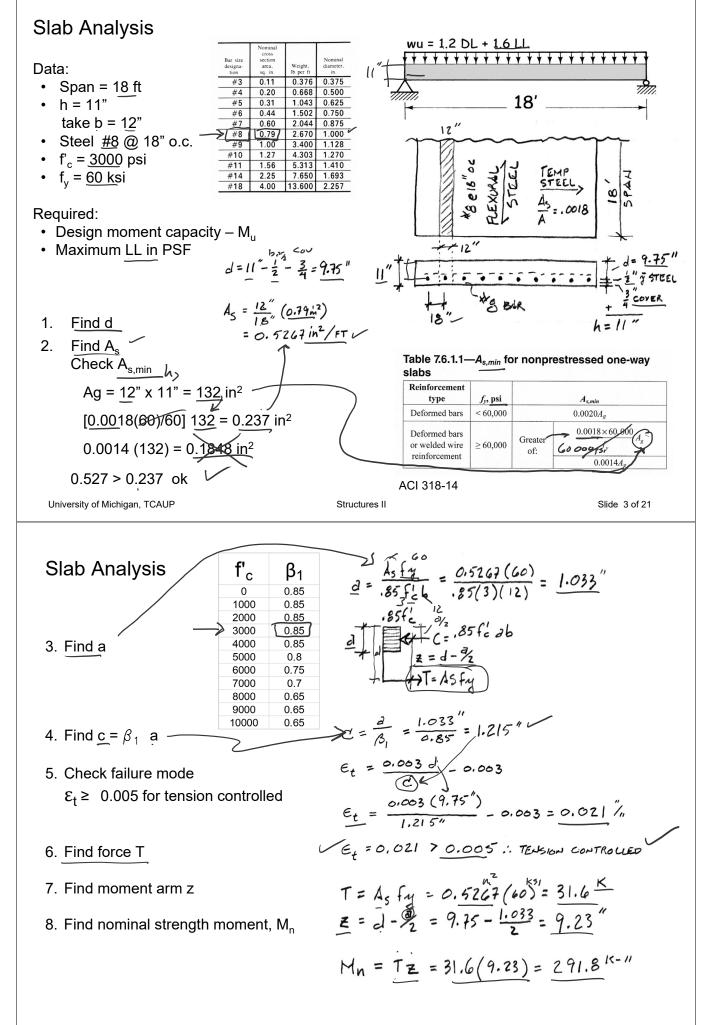


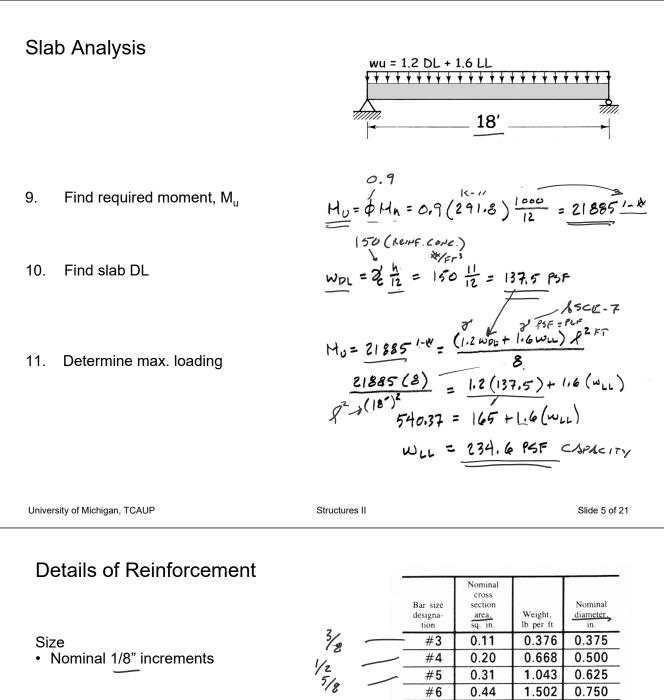
 $\phi$  Mn  $\geq$  Mu (if  $\varepsilon_t \geq 0.005$  then  $\phi = 0.9$ )

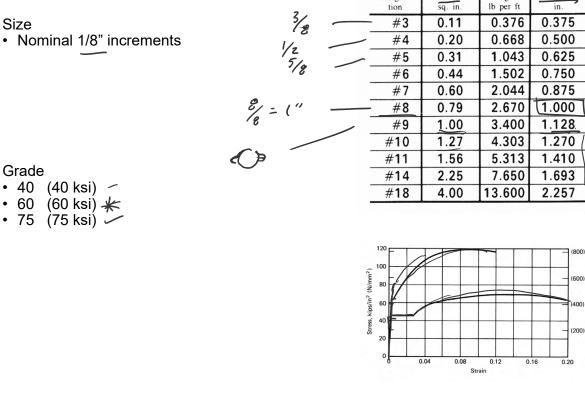
8. Determine max. loading (or span)

Data:

 $1.6w_{LL} = \frac{M_u 8}{l^2} - 1.2w_{DL}$ 







## **Details of Reinforcement**

ACI 318 Chapter 25.2 Placement of Reinforcement

- Cover (ACI 20.6.1)
- Horizontal spacing in beams, s<sub>h</sub> (ACI 25.2.1)
   <u>1 inch</u>

$$\frac{d_b}{4/3} d_{agg,max}$$

• Vertical spacing in beams (ACI 25.2.2) Min 1 inch

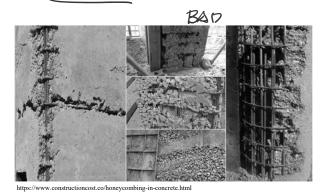
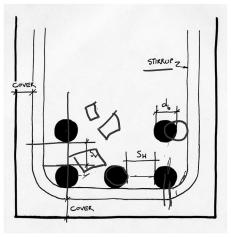


Table 20.6.1.3.1—Specified concrete cover for cast-in-place nonprestressed concrete members

Concrete exposure	Member	Reinforcement	Specified cover, in.
Cast against and permanently in contact with ground	All	All	3
Exposed to weather		No. 6 through No. 18 bars	2
or in contact with ground	All	No. 5 bar, W31 or D31 wire, and smaller	1-1/2
Not exposed to weather or in contact with ground	Slabs, joists,	No. 14 and No. 18 bars	1-1/2
	and walls	No. 11 bar and smaller	3/4
	Beams, columns, pedestals, and tension ties	Primary reinforce- ment, stirrups, ties, spirals, and hoops	1-1/2



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## **Details of Reinforcement**

ACI 318 Chapter 25 Placement of Reinforcement

- · Chairs
- Bolsters







http://contractorsupplymagazine.com





High Chai

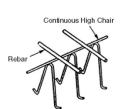
Reba



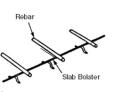




Continuous High Chair







## **Details of Reinforcement**

ACI 318 Chapter 25

### Minimum bend diameter

• factor x d<sub>b</sub>

### Hooks for bars in tension

- ACI Table 25.3.1
- · Inside diameter

### Bends for stirrups

• ACI Table 25.3.2

Table 25.3.1—Standard hook geometry for development of deformed bars in tension

Type of standard hook	Bar size	Minimum inside bend diameter, in.	Straight extension <sup>[1]</sup> ℓ <sub>ext</sub> in.	Type of standard hook	
	No. 3 through No. 8	6d <sub>b</sub> 3	63 9	Point at which bar is developed	
90-degree	No. 9 through No. 11	8 <i>d</i> <sub>b</sub>	<b>8 4 4</b> 12 <i>d</i>	4 90-degree bend	
hook	hook No. 14 and No. 18	10 <i>d</i> <sub>b</sub>	1246	Diameter	
	No. 3 through No. 8	$6d_b$		Point at which bar is developed	
180-degree	No. 9 through No. 11	8 <i>d</i> <sub>b</sub>	Greater of		
hook	No. 14 and No. 18	10 <i>d</i> <sub>b</sub>	$4d_b$ and 2.5 in.	Diameter bend	

<sup>10</sup>A standard hook for deformed bars in tension includes the specific inside bend diameter and straight extension length. It shall be permitted to use a longer straight extension at the end of a hook. A longer extension shall not be considered to increase the anchorage capacity of the hook.

Table 25.3.2—Minimum inside bend diameters and standard hook geometry for stirrups, ties, and hoops

Type of stan- dard hook	Bar size	Minimum inside bend diameter, in.	Straight extension <sup>[1]</sup> <i>l</i> <sub>exp</sub> in.	Type of standard hook
90-degree	No. 3 through No. 5	$4d_b$	Greater of $6d_b$ and 3 in.	d <sub>b</sub> 90-degree
hook	No. 6 through No. 8	6 <i>d</i> <sub>b</sub>	12 <i>d</i> <sub>b</sub>	Diameter
135-degree	No. 3 through No. 5	4 <i>d</i> <sub>b</sub>	Greater of 6 <i>d<sub>b</sub></i> and 3 in.	db 135-degree
hook	No. 6 through No. 8	6 <i>d</i> <sub>b</sub>		Diameter
180-degree	No. 3 through No. 5	4 <i>d</i> <sub>b</sub>	Greater of	d <sub>b</sub> 180-degre
hook No. 6 through No. 8	through	6 <i>d</i> <sub>b</sub>	4 <i>d<sub>b</sub></i> and 2.5 in.	Diameter bend

<sup>11</sup>A standard hook for stirrups, ties, and hoops includes the specific inside bend diameter and straight extension length. It shall be permitted to use a longer straight extension at the end of a hook. A longer extension shall not be considered to increase the anchorage capacity of the hook.

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## **Details of Reinforcement**

### ACI 318 Chapter 25



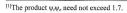
Development length of bars

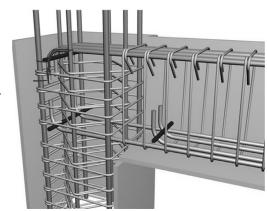
• 12" min

• Based on table 25.4.2.2

## Table 25.4.2.4—Modification factors for development of deformed bars and deformed wires in tension

Modification factor	Condition	Value of factor
	Lightweight concrete	0.75
Lightweight	Lightweight concrete, where $f_{ct}$ is specified	In accordance with 19.2.4.3
	Normalweight concrete	1.0
$\underbrace{\frac{\text{Epoxy}^{[1]}}{\psi_e}}_{\psi_e}$	Epoxy-coated or zinc and epoxy dual-coated reinforcement with clear cover less than $3d_b$ or clear spacing less than $6d_b$	1.5
	Epoxy-coated or zinc and epoxy dual- coated reinforcement for all other conditions	1.2
	Uncoated or zinc-coated (galvanized) reinforcement	1.0
Size	No. 7 and larger bars	1.0
$\Psi_s$	No. 6 and smaller bars and deformed wires	0.8
Casting position <sup>[1]</sup>	More than 12 in. of fresh con- crete placed below horizontal reinforcement	1.3
$\Psi_t$	Other	1.0





https://www.buildinghow.com

#### 

Spacing and cover	No. 6 and smaller bars and deformed wires	No. 7 and larger bars
Clear spacing of bars or wires being developed or lap spliced not less than $d_b$ , clear cover at least $d_b$ , and stirrups or ties throughout $\ell_d$ not less than the Code minimum or Clear spacing of bars or wires being developed or lap spliced at least $2d_b$ and clear cover at least $d_b$	$\underbrace{\left(\frac{f_{y}\boldsymbol{\psi},\boldsymbol{\psi}_{e}}{25\lambda\sqrt{f_{c}^{\prime}}}\right)}_{\boldsymbol{\psi}_{b}}d_{b}$	$\left(\frac{f_{y}\psi_{i}\psi_{e}}{20\lambda\sqrt{f_{c}'}}\right)d_{b}$
Other cases	$\left(\frac{3f_y\psi_i\psi_e}{50\lambda\sqrt{f_c'}}\right)d_b$	$\left(\frac{3f_y\psi_i\psi_e}{40\lambda\sqrt{f_c'}}\right)d_b$

## Other Useful Tables:

					C	ustomary Uni	ts		SI Units	
				Bar No.	Diameter (in.)	Cross- sectional Area (in. <sup>2</sup> )	Unit Weight (lb/ft)	Diameter (mm)	Cross- sectional Area (mm <sup>2</sup> )	Unit Weight (kg/m)
Table A	.1 Values of M	odulus of Ela	sticity for	1 3	0.375	0.11	0.376	9.52	71	0.560
	Normal-Wei	ght Concrete		4	0.500	0.20	0.668	12.70	129	0.994
Custo		CI I	Jnits	5	0.625	0.31	1.043	15.88	200	1.552
	mary Units			6	0.750	0.44	1.502	19.05	284	2.235
$f_c'$	$\frac{E_c}{(mai)}$	$f_c'$ (MPa)	E <sub>c</sub> (MPa)	7	0.875	0.60	2.044	22.22	387	3.042
(psi)	(psi)	. ,		8	1.000	0.79	2.670	25.40	510	3.973
3,000	3,140,000	20.7	21 650	9	1.128	1.00	3.400	28.65	645	5.060
3,500	3,390,000	24.1	23 373	10	1.270	1.27	4.303	32.26	819	6.404
4,000	3,620,000	27.6	24 959	11	1.410	1.56	5.313	35.81	1006	7.907
4,500	3,850,000	31.0	26 545	14	1.693	2.25	7.650	43.00	1452	11.384
5,000	4,050,000	34.5	27 924	18	2.257	4.00	13.600	57.33	2581	20.238

Table A.2 Designations, Areas, Perimeters, and Weights of Standard Bars

Jack C McCormac, 1978, Design of Reinforced Concrete,

#### Table A.4 Areas of Groups of StandardBars (in.<sup>2</sup>)

						Num	ber of Ba	rs					
Bar No.	2	3	4	5	6	7	8	9	10	11	12	13	1,4
- 4	0.39	0.58	0.78	0.98	1.18	1.37	1.57	1.77	1.96	2.16	2.36	2.55	2.75
5	0.61	0.91	1.23	1.53	1.84	2.15	2.45	2.76	3.07	3.37	3.68	3.99	4.30
6	0.88	1.32	1.77	2.21	2.65	3.09	3.53	3.98	4.42	4.86	5.30	5.74	6.19
7	1.20	1.80	2.41	3.01	3.61	4.21	4.81	5.41	6.01	6.61	7.22	7.82	8.42
8	1.57	2.35	3.14	3.93	4.71	5.50	6.28	7.07	7.85	8.64	9.43	10.21	11.00
9	2.00	3.00	4.00	5.00	6.00	7.00	8.00	9.00	10.00	11.00	12.00	13.00	14.00
10	2.53	3.79	5.06	6.33	7.59	8.86	10.12	11.39	12.66	13.92	15.19	16.45	17.72
11	3.12	4.68	6.25	7.81	9.37	10.94	12.50	14.06	15.62	17.19	18.75	20.31	21.87
14	4.50	6.75	9.00	11.25	13.50	15.75	18.00	20.25	22.50	24.75	27.00	29.25	31.50
18	8.00	12.00	16.00	20.00	24.00	28.00	32.00	36.00	40.00	44.00	48.00	52.00	56.00

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## Rectangular Beam Design

Two approaches:

### Method 1:

Data:

- Load and Span
- Material properties  $f'_c, f_v$
- All section dimensions: h and b

**Required:** 

Steel area – A<sub>s</sub>

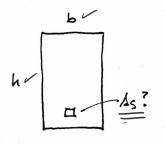
### Method 2:

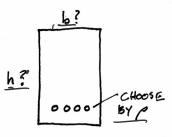
Data:

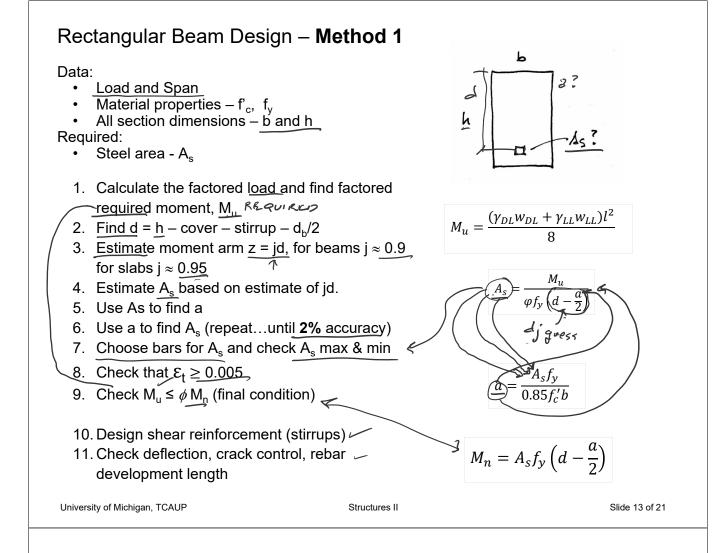
- Load and Span
- Some section dimensions h or b
- Material properties f'<sub>c</sub>, f<sub>v</sub>
- Choose  $\rho$

Required:

- Steel area <u>A</u>
- Beam dimensions b or h







### One-way Slab Design Method 1

#### Data:

- · Load and Span
- Material properties f<sup>'</sup><sub>c</sub>, f<sub>v</sub>
- All section dimensions:
- h (based on deflection limit)
- b = typical 12" width

#### **Required:**

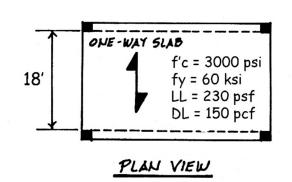
Steel area – A<sub>s</sub>

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First estimate the slab thickness, h.

Try first the recommended minimum.

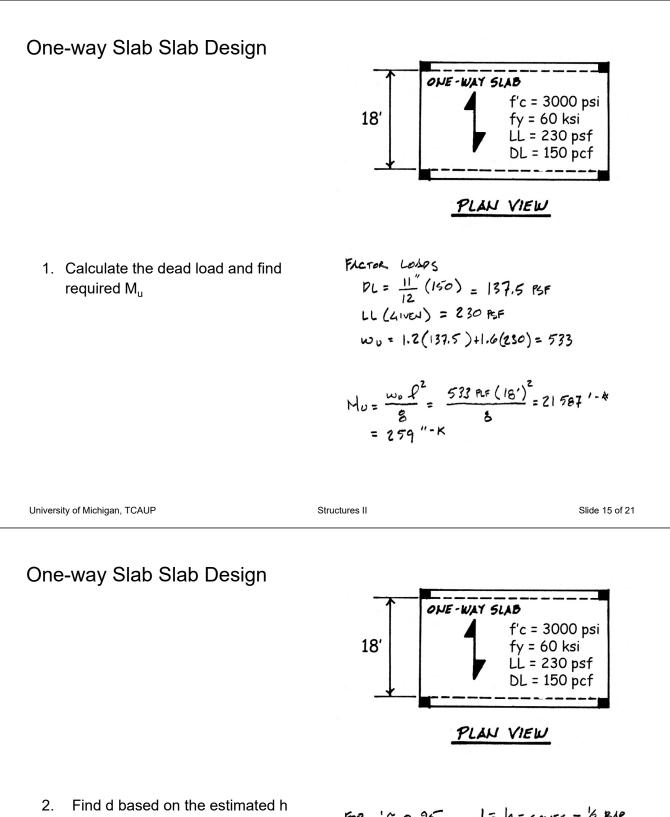
Deeper sections require less steel, but of course more concrete.



#### Table 7.3.1.1—Minimum thickness of solid nonprestressed one-way slabs

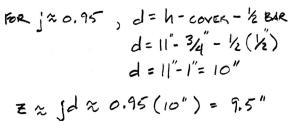
Support condition	Minimum h <sup>[1]</sup>
Simply supported	<i>ℓ</i> /20
One end continuous	<i>ℓ</i> /24
Both ends continuous	ℓ/28
Cantilever	<i>€</i> /10

THICKNESS, h, BASED ON DEFLECTION  $h = \frac{R_{10}}{20} = \frac{18 \times 12}{20} = 10.8"$  USE II"



3. Estimate moment arm  $z \approx 0.95 d$ 

and rebar size (guessing #4)



## One-way Slab Slab Design

4. Estimate  $A_s$  based on estimate of z

- 5. Use  $A_s$  to find a
- 6. Use a to find  $A_s$  (repeat...)

TRIAL I  $A_{5} = \frac{M_{U}}{\phi f_{y}(z)} = \frac{259''''}{0.9(60 \text{ KsI})(9.5)''} = 0.505 \text{ in}^{2}$   $a = \frac{A_{5} f_{y}}{.85 f_{c}} = \frac{0.505(c0)}{.85(3)(12)} = 0.99''$ 

$$\frac{1}{4} \frac{1}{4} \frac{1}{5} \frac{1}{4} \frac{1}{5} \frac{1}$$

## One-way Slab Slab Design

7. Choose bars for A<sub>s</sub> required:

either

choose bars and calculate spacing or

**choose spacing** and find bar size If the bar size changes, re-calculate to find new d. Then, re-calculate A<sub>s</sub>...

Check A<sub>s,min</sub>

(for slabs A<sub>s.min</sub> from ACI Table 7.6.1.1)

Table 7.6.1.1-	As,min for nonprestressed one-way
slabs	
DIC	

type	<i>f<sub>y</sub></i> , psi		A <sub>s,min</sub>
Deformed bars	< 60,000		$0.0020 A_{g}$
Deformed bars or welded wire	≥ 60,000	Greater of:	$\frac{0.0018 \times 60,000}{f_y} A_g$
reinforcement	1.1.1.1		$0.0014A_{g}$

$$\frac{0.505}{12''} : \frac{0.2}{s} = 4.75''$$
i. USE 4" o.c. (always round down)  
 $A_5 = 0.60 \text{ m}^2/\text{FT} > 0.505 \text{ //}$ 

ALTERNATE FOR MAX. S =18"

$$\frac{0.505}{12''} : \frac{A_b}{18''} \qquad A_b = 0.75 \text{ m}^2$$

$$\frac{A_b}{18''} \qquad \frac{A_b}{18''} = 0.79$$

$$\frac{1}{100} \text{ m}^2 \text{ m}^2$$

Check As,min

As min = 0.0018 bh = 0.0018(12)(11")  
= 0.24 
$$m^2 < 0.526m^2 = 0 \ K$$

## One-way Slab Slab Design

8. Check that  $\varepsilon_t \ge 0.005$ 

RE-CALC 2 FOR 
$$A_{5} = 0.6 \frac{m^{3}}{PT}$$
  
 $d = \frac{A_{5} f_{M}}{0.85 f_{c}} = \frac{0.6(60)}{0.85(3)(12)} = 1.176''$   
 $C = \frac{2}{B_{1}} = \frac{1.176}{0.85} = 1.384''$   
 $G_{4} = \frac{d-c}{c} 0.003 =$   
 $= \frac{9.5''-1.384''}{1.384''} 0.003 = 0.01759$   
 $0.01759 > 0.005$   
 $i. TENSION CONTROLLED /$ 

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# One-way Slab Slab Design

9. Check  $M_u \le \phi M_n$ (final condition)

> $A_s = A_{s,used}$  $M_n = Tz$

- 10. Add stirrups (no stirrups in slab)
- 11. Check deflection, crack control, and rebar development length

$$M_{n} = A_{3}F_{y}\left(d - \frac{z^{2}}{2}\right)$$

$$M_{n} = 0.6(60)\left(9.5^{n} - \frac{1.176}{2}\right)$$

$$M_{n} = 36\left(8.911^{n}\right) = 320.8^{K-11}$$

$$M_{n} = 0.9\left(320.8\right) = 288.7^{K-11}$$

$$M_{0} = 259^{K-11} < 288.7^{K-11}$$

$$M_{0} < d_{1}M_{1} \quad \checkmark = \times$$

### Rectangular Beam Design - Method 2

### Data:

- Load and Span
- Some section dimensions b or h
- Material properties  $f'_c$ ,  $f_y$

### **Required:**

- Steel area A<sub>s</sub>
- Beam dimensions b and h
- 1. Estimate the dead load (estimate h and b)  $(L/8 \le h \le L/21, h \approx L/12$  and b:h  $\approx$  1:2 to 2:3), find  $M_u$
- 2. Choose  $\rho$  (equation assumes  $\varepsilon_t = 0.0075$ ) 3. Calculate  $bd^2$
- Calculate bd<sup>2</sup>
   Change b and and
- 4. Choose b and solve for d (or d and solve b)
- 5. Revise h, weight,  $M_u$ , and  $bd^2$
- 6. Find  $A_s = \rho bd$
- 7. Choose bars for  ${\rm A}_{\rm s},$  determine spacing and cover, and revise d
- 8. Check that  $\epsilon_t \geq 0.005$  (if not, increase h and reduce  $A_s)$
- 9. Design shear reinforcement (stirrups)
- 10. Check deflection, crack control, steel development length

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$$M_u = \frac{(\gamma_{DL} w_{DL} + \gamma_{LL} w_{LL})l^2}{8}$$

$$\rho = \frac{\beta_1 f_c'}{4f_y}$$

$$bd^{2} = \frac{M_{u}}{\varphi \rho f_{y} \left(1 - 0.59 \rho (fy/f_{c}')\right)}$$

$$A_s = \rho b d$$

$$a = \frac{\rho f_{\mathcal{Y}} \, d}{0.85 f_c'}$$

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