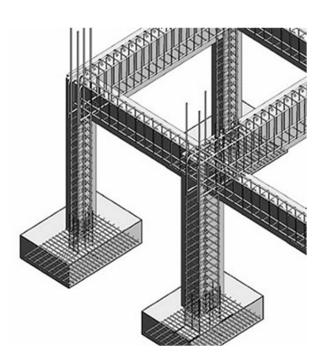
Architecture 324 Structures II

Reinforced Concrete Beams Ultimate Strength Design (ACI 318-14) – PART III

- Rectangular Beam Design Method 2
- Non-Rectangular Beam Analysis
- Reinforced Concrete Examples
- 3D-Print Evolution (Video)



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Details of Reinforcement

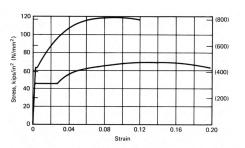
Size

• Nominal 1/8" increments

Grade

- 40 (40 ksi)
- 60 (60 ksi)
- 75 (75 ksi)

Bar size designa- tion	Nominal cross section area, sq. in.	Weight, lb per ft	Nominal diameter, in.
#3	0.11	0.376	0.375
#4	0.20	0.668	0.500
#5	0.31	1.043	0.625
#6	0.44	1.502	0.750
#7	0.60	2.044	0.875
#8	0.79	2.670	1.000
#9	1.00	3.400	1.128
#10	1.27	4.303	1.270
#11	1.56	5.313	1.410
#14	2.25	7.650	1.693
#18	4.00	13.600	2.257



Details of Reinforcement

ACI 318 Chapter 25.2 Placement of Reinforcement

- Cover (ACI 20.6.1)
- Horizontal spacing in beams, s_h (ACI 25.2.1)
 1 inch
 d_b
 4/3 d_{agg,max}
- Vertical spacing in beams (ACI 25.2.2)
 Min 1 inch



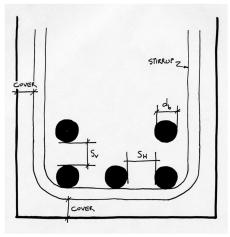
https://www.constructioncost.co/honeycombing-in-concrete.html

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Table 20.6.1.3.1—Specified concrete cover for cast-in-place nonprestressed concrete members

Concrete exposure	Member	Reinforcement	Specified cover, in.
Cast against and permanently in contact with ground	All	All	3
Exposed to weather		No. 6 through No. 18 bars	2
or in contact with ground	All	All 3 No. 6 through No. 18 bars No. 5 bar, W31 or D31 wire, and smaller No. 14 and No. 18 bars No. 14 and No. 18 bars No. 11 bar and smaller No. 11	
	Slabs, joists,		1-1/2
Not exposed to weather or in	and walls		3/4
contact with ground	Beams, columns, pedestals, and tension ties	ment, stirrups, ties,	1-1/2

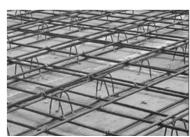


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Details of Reinforcement

ACI 318 Chapter 25 Placement of Reinforcement

- Chairs
- Bolsters



https://catalog.formtechinc.com

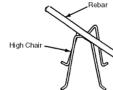


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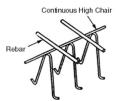




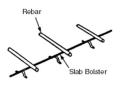




Continuous High Chair







Details of Reinforcement

ACI 318 Chapter 25

Minimum bend diameter

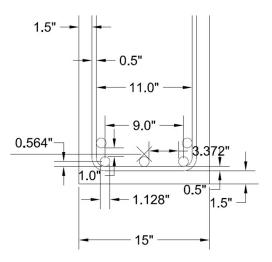
factor x d_b

Hooks for bars in tension

- ACI Table 25.3.1
- · Inside diameter

Bends for stirrups

ACI Table 25.3.2



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Table 25.3.1—Standard hook geometry for development of deformed bars in tension

Type of standard hook	Bar size	Minimum inside bend diameter, in.	Straight extension ^[1] ℓ_{ext} , in.	Type of standard hook		
No. 3 through No. 8		$6d_b$		Point at which bar is developed		
90-degree	No. 9 through No. 11	8 <i>d</i> _b	12 <i>d</i> s	d _b 90-degree bend		
hook	No. 14 and No. 18	10 <i>d_b</i>	12a _b	Diameter		
	No. 3 through No. 8	6 <i>d</i> _b		Point at which bar is developed		
180-degree	No. 9 through No. 11	8 <i>d</i> _b	Greater of	180-degree		
hook	No. 14 and No. 18	10 <i>d_b</i>	4d _b and 2.5 in.	Diameter bend		

[&]quot;In A standard hook for deformed bars in tension includes the specific inside bend diameter and straight extension length. It shall be permitted to use a longer straight extension at the end of a hook. A longer extension shall not be considered to increase the anchorage capacity of the hook.

Table 25.3.2—Minimum inside bend diameters and standard hook geometry for stirrups, ties, and hoops

Type of stan- dard hook	Bar size	Minimum inside bend diameter, in.	Straight extension ^[1] ℓ_{ext} , in.	Type of standard hook
90-degree	No. 3 through No. 5	4d _b	Greater of $6d_b$ and 3 in.	d _b 90-degree
hook	No. 6 through No. 8	$6d_b$	12 <i>d_b</i>	Diameter \\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\
135-degree	No. 3 through No. 5	4 <i>d</i> _b	Greater of 6dh and	135-degre
hook	No. 6 through No. 8	6 <i>d</i> _b	3 in.	Diameter
180-degree	No. 3 through No. 5	4 <i>d</i> _b	Greater of	d _b 180-degre
hook	No. 6 through No. 8	$6d_b$	4d_b and 2.5 in.	Diameter bend

^{11/}A standard hook for stirrups, tics, and hoops includes the specific inside bend diameter and straight extension length. It shall be permitted to use a longer straight extension at the end of a hook. A longer extension shall not be considered to increase the anchorage capacity of the hook.

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Details of Reinforcement

ACI 318 Chapter 25

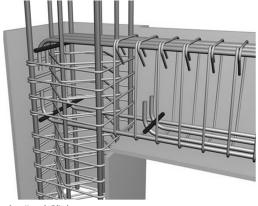
Development length of bars

- 12" min
- Based on table 25.4.2.2

Table 25.4.2.4—Modification factors for development of deformed bars and deformed wires in tension

Modification factor	Condition	Value of factor
	Lightweight concrete	0.75
Lightweight λ	Lightweight concrete, where f_{ct} is specified	In accordance with 19.2.4.3
	Normalweight concrete	1.0
F(11)	Epoxy-coated or zinc and epoxy dual-coated reinforcement with clear cover less than $3d_b$ or clear spacing less than $6d_b$	1.5
Epoxy ^[1] Ψ_e	Epoxy-coated or zinc and epoxy dual- coated reinforcement for all other conditions	1.2
	Uncoated or zinc-coated (galvanized) reinforcement	1.0
Size	No. 7 and larger bars	1.0
ψ_s	No. 6 and smaller hars and deformed	
Casting position ^[1]	More than 12 in. of fresh con- crete placed below horizontal reinforcement	1.3
Ψt	Other	1.0

^[1]The product $\psi_i \psi_e$ need not exceed 1.7.



https://www.buildinghow.com

Table 25.4.2.2—Development length for deformed bars and deformed wires in tension

Spacing and cover	No. 6 and smaller bars and deformed wires	No. 7 and larger bars
Clear spacing of bars or wires being developed or lap spliced not less than d_b , clear cover at least d_b , and stirrups or ties throughout ℓ_d not less than the Code minimum or Clear spacing of bars or wires being developed or lap spliced at least $2d_b$ and clear cover at least d_b	$\left(\frac{f_{j}\Psi_{t}\Psi_{e}}{25\lambda\sqrt{f_{c}^{\prime}}}\right)d_{b}$	$\left(rac{f_{y}\psi_{i}\psi_{e}}{20\lambda\sqrt{f_{c}^{\prime}}} ight)d_{b}$
Other cases	$\left(\frac{3f_{y}\psi_{t}\psi_{\epsilon}}{50\lambda\sqrt{f_{c}'}}\right)d_{b}$	$\left(\frac{3f_y\psi_i\psi_e}{40\lambda\sqrt{f_c'}}\right)d_b$

Other Useful Tables:

Table A.2 Designations, Areas, Perimeters, and Weights of Standard Bars

Table A	.1 Values of M Normal-Wei	odulus of Ela ght Concrete	sticity for
Custo	mary Units	SI U	Jnits
f_{c}^{\prime}	E _c	f_{c}^{\prime}	E_c

Custo	mary Units	SIC	nits
f' (psi)	E _c (psi)	fc' (MPa)	E _c (MPa)
3,000	3,140,000	20.7	21 650
3,500	3,390,000	24.1	23 373
4,000	3,620,000	27.6	24 959
4,500	3,850,000	31.0	26 545
5,000	4,050,000	34.5	27 924
3,000	4,030,000	34.3	2192

Jack C McCormac	1978	Design of Reinforced Concrete

_ ¬	C	ustomary Uni	ts	SI Units				
Bar No.	Diameter (in.)	Cross- sectional Area (in.2)	Unit Weight (lb/ft)	Diameter (mm)	Cross- sectional Area (mm²)	Unit Weight (kg/m)		
3	0.375	0.11	0.376	9.52	71	0.560		
4	0.500	0.20	0.668	12.70	129	0.994		
5	0.625	0.31	1.043	15.88	200	1.552		
6	0.750	0.44	1.502	19.05	284	2.235		
7	0.875	0.60	2.044	22.22	387	3.042		
8	1.000	0.79	2.670	25.40	510	3.973		
9	1.128	1.00	3.400	28.65	645	5.060		
10	1.270	1.27	4.303	32.26	819	6.404		
11	1.410	1.56	5.313	35.81	1006	7.907		
14	1.693	2.25	7.650	43.00	1452	11.384		
18	2.257	4.00	13.600	57.33	2581	20.238		

Table A.4 Areas of Groups of StandardBars (in.2)

						Num	ber of Ba	.rs					
Bar No.	2	3	4	5	6	7	8	9	10	11	12	13	1,4
4	0.39	0.58	0.78	0.98	1.18	1.37	1.57	1.77	1.96	2.16	2.36	2.55	2.75
5	0.61	0.91	1.23	1.53	1.84	2.15	2.45	2.76	3.07	3.37	3.68	3.99	4.30
6	0.88	1.32	1.77	2.21	2.65	3.09	3.53	3.98	4.42	4.86	5.30	5.74	6.19
7	1.20	1.80	2.41	3.01	3.61	4.21	4.81	5.41	6.01	6.61	7.22	7.82	8.42
8	1.57	2.35	3.14	3.93	4.71	5.50	6.28	7.07	7.85	8.64	9.43	10.21	11.00
9	2.00	3.00	4.00	5.00	6.00	7.00	8.00	9.00	10.00	11.00	12.00	13.00	14.00
10	2.53	3.79	5.06	6.33	7.59	8.86	10.12	11.39	12.66	13.92	15.19	16.45	17.72
11	3.12	4.68	6.25	7.81	9.37	10.94	12.50	14.06	15.62	17.19	18.75	20.31	21.87
14	4.50	6.75	9.00	11.25	13.50	15.75	18.00	20.25	22.50	24.75	27.00	29.25	31.50
18	8.00	12.00	16.00	20.00	24.00	28.00	32.00	36.00	40.00	44.00	48.00	52.00	56.00

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Structures II

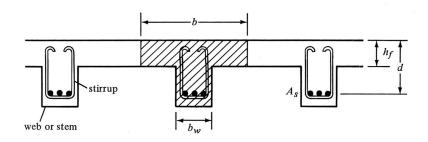
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T Beams

Dimensional limits

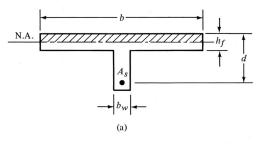
Nomenclature

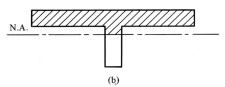


Possible locations of the N.A.:

Within flange – rectangular

Within stem – non-rectangular





T Beams - Effective Flange Width, be

Slab on one side:

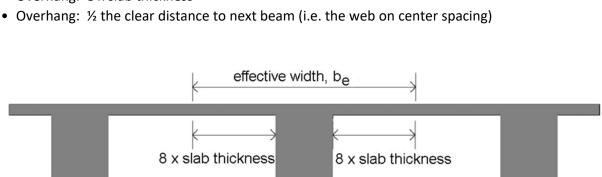
be least of either (total width) or (overhang + stem)

- Total width: 1/12 of the beam span
- Overhang: 6 x slab thickness
- Overhang: ½ the clear distance to next beam

Slab on both sides:

b_e least of either (total width) or (2 x overhang + stem)

- Total width: ¼ of the beam span
- Overhang: 8 x slab thickness



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Structures II

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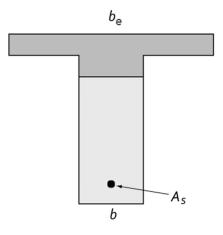
Non-Rectangular Beam Analysis

Data:

- Section dimensions b, b_e, h, (span)
- Steel area A_s
- Material properties f'_c, f_v

Required:

- Required Moment M_{II} (or load, or span)
- 1. Find T = $A_s f_y$ and C = $0.85 f_c^{\circ} A_c$
- 2. Set T = C and solve for $A_c = T/(0.85 \text{ f'c})$
- 3. Draw and label diagrams for section and stress
 - 1. Determine b effective (for T-beams)
 - 2. Locate T and C (or C₁ and C₂)
- 4. Determine the location of a Working from the top down, add up area to make A_c
- 5. Find the moment arms (z) for each block of area
- 6. Find $M_n = \sum C_i z_i$
- 7. Find $M_u = \phi M_n$
- 8. Check $A_{s,min} < A_s < A_{s,max}$
- 9. Check that $\varepsilon_t \ge 0.005$



1/12 of span

6 x slab depth

1/2 clear span

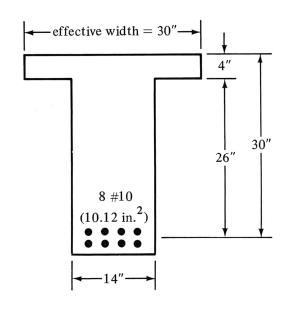
T Beam Analysis

Given: $f_c = 3000 \text{ psi}$

 $f_{v} = 50 \text{ ksi}$

dimensions. Use $b_{eff} = 30$ "

Req'd: Moment capacity, Mu



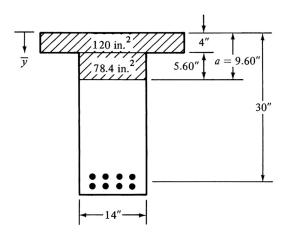
- 1. Find T = $A_s f_y$ and C = $0.85 f_c A_c$
- 2. Set T = C and solve for $A_c = T/(0.85 \text{ f'c})$

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T Beam Analysis (cont.)



- 3. Draw and label diagrams for section & stress
 - 1. Determine b effective (for T-beams)
 - 2. Locate T and C (or C₁ and C₂)
- Determine the location of a Working from the top down, add up area to make A_c
- 5. Find the moment arms (z) for each block of area
- 6. Find $M_n = \sum_i C_i z_i$
- 7. Find $M_u = \phi M_n$

FLANCE = 30"×4" = 120 < 198.4 : NA IN WEB 198.4-120 = 78.4 in² = 14"×5.60" a = 4" + 5.60" = 9.60" BY PARTS (FOR EACH AREA)

$$Z_1 = 30'' - \frac{4''}{2} = 28''$$

$$Z_2 = 30'' - 4'' - 5.6/z'' = 23.2''$$

$$C_1 = A_{c1} 0.85 f'_{c} = 120(0.85)(3) = 306^{K}$$

 $C_2 = A_{c2} 0.85 f'_{c} = 78.4(0.85)(3) = 199.9^{K}$

$$M_{\rm H} = \sum (iZ_i = 306(28) + 199.9(23.2) = 8568 + 4638 = 13206^{\rm K-IN}$$

T Beam Analysis (cont.)

$$\rho_{\rm max}$$
 = 0.75 $\rho_{\rm bal}$

$$a_{bal}$$
 = beta c_{bal} = 0.85 (19.07") = 16.21"

$$Ac_{bal} = (4")(30") + (12.21")(14") = 291 in^2$$

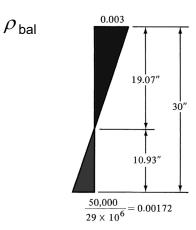
$$C_{bal} = (0.85)(3)(291) = 742^{k}$$

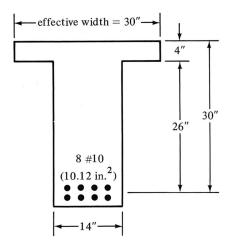
$$T_{\text{max}} = 0.75 C_{\text{bal}} = (0.75) (742) = 556^{\text{k}}$$

$$T_{used} = A_s f_v = (10.12) (50) = 506^k < 556^k \text{ ok}$$

$$As_{min} = 200 (b_w d) / f_v = 200 (14) (30) / 50 000$$

$$As_{min} = 1.68 \text{ in}^2 < 10.12 \text{ in}^2 \text{ ok}$$





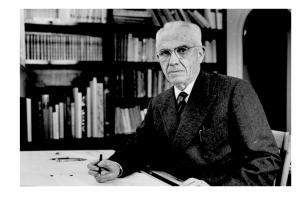
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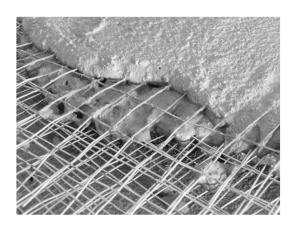
Structures II

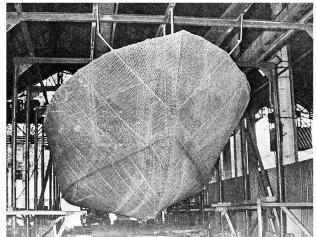
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Ferrocement

- Pioneered by Pier Luigi Nervi
- Dense, small gage reinforcement
- More flexible shapes no formwork
- · Well suited for thin shells
- · Less cracking



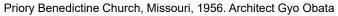




Ferrocement

- Pioneered by Nervi
- Dense, small gage reinforcement
- More flexible shapes no formwork
- · Well suited for thin shells
- Less cracking
- · Low-tech applications









Palazetto dello Sport, Rome, 1957. P.L. Nervi

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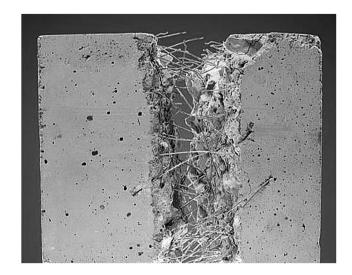
Fiber Reinforced Concrete

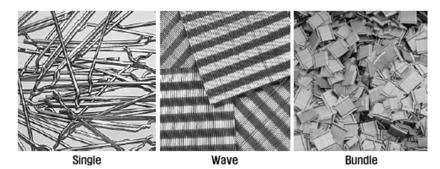
Several different fiber types:

- Steel (SFRC)
- Glass (GFRC)
- Plastic e.g. polypropylene
- Carbon
- Organic e.g. bamboo

Better crack control Secondary reinforcement





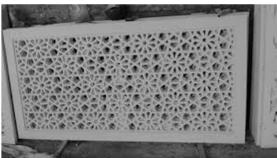


Glass Fiber Reinforced Concrete - GFRC









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Carbon Fiber





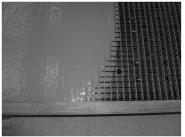
Bamboo





Textile Reinforced Concrete (TRC)





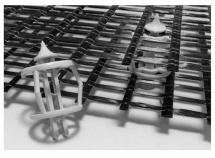


Figure 12: distTEX: special spacers for textile grids [photo: Frank Schladitz, TU Dresden]



Figure 13: Manufacturing of the TRC hypar-shell layer by layer by shotcrete [photo: © RWTH Aachen], [38]



Figure 10: Demolding of a hardened shell element in the concrete yard in Kahla/Saxony [photo: Daniel Ehlig, TU Dresden]

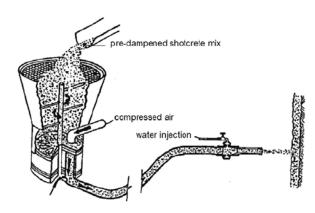
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Shotcrete

- Pneumatically applied
- High velocity
- Can include fiber
- Applied to backing
- Reinforced with bars
- · Soil stabilization, tunnels







3D-Print Evolution



THANK YOU

Platinum Partner



Silver Partner









THEPOWEROFTEN

Gold Partner

https://www.youtube.com/watch?v=awpmJriWcEw

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