

## Arch324 STRUCTURES II

Winter 2025 Recitation

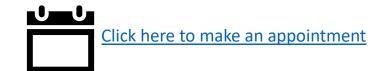
FACULTY: Prof. Peter von Bülow Mohsen Vatandoost

### Arch324: STRUCTURES II

### Welcome to Recitation session 03/14 Mohsen Vatandoost {Ph.D., M.Sc., M. Arch}

mohsenv@umich.edu

Office: Room 3122 hours: Fri: 11:30 – 12:30 Mon, Wed: 11:00 - 12:00 walk-ins welcome!



Please feel free to ask questions.



### Arch324: STRUCTURES II

### Welcome to Recitation session 03/14

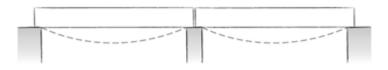
Outline:

- Quick **Recap** of the week
- Provide the solution for the assignment (Homework 7)
- Answering student's questions
- Lab: Continuous Beams
- Tower Project: Preliminary report (revision) + Test date: March 24

Please feel free to ask questions.



### Continuous beams



two spans - simply supported

## Methods for solving internal forces in Continuous beams:

- Deflection Method
- Slope Method
- Three-Moment Theorem





#### Statically indeterminate:

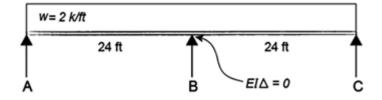
- Cannot be solved by the three equations of statics alone
- Internal forces (shear & moment) as well as reactions are affected by movement or settlement of the supports



### Continuous beams

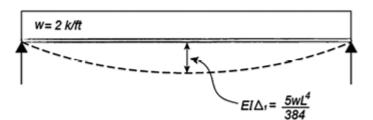
#### **Deflection Method**

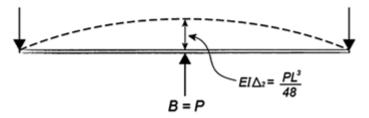
- Two continuous, symmetric spans
- Symmetric Load



Procedure:

- 1. Remove the center support, and calculate the center deflection for each load case as a simple span.
- 2. Remove the applied loads and replace the center support. Set the deflection equation for this case (center point load) equal to the deflection from step 1.
- 3. Solve the resulting equation for the center reaction force. (upward point load)
- 4. Calculate the remaining two end reactions.
- 5. Draw shear and moment diagrams as usual.





$EI\Delta_1 + EI\Delta_2 = 0$
-------------------------------



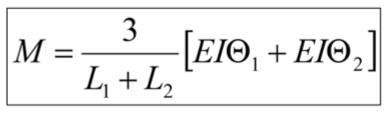
### Continuous beams

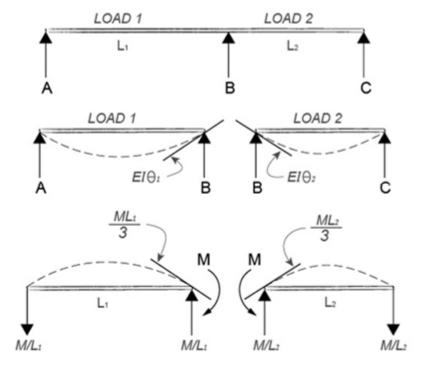
#### Slope Method

- Two continuous spans
- Non-symmetric loads and spans

#### Procedure:

- 1. Break the beam into two halves at the interior support, and calculate the interior slopes of the two simple spans.
- 2. Use the Slope Equation to solve for the negative interior moment.
- 3. Find the reactions of each of the simple spans plus the M/L reactions caused by the interior moment.
- 4. Add all the reactions by superposition.
- 5. Draw the shear and moment diagrams as usual.



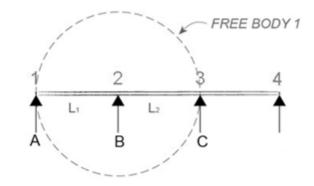


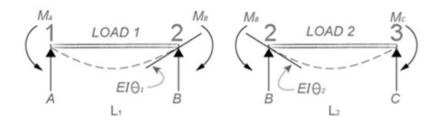


### Continuous beams

**Three-Moment Theorem** 

- Any number of spans
- Symmetric or non-symmetric





$$M_{A}L_{1} + 2M_{B}(L_{1} + L_{2}) + M_{C}L_{2} = 6[EI\Theta_{1} + EI\Theta_{2}]$$



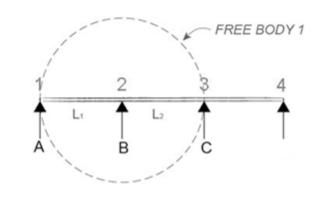
### Continuous beams

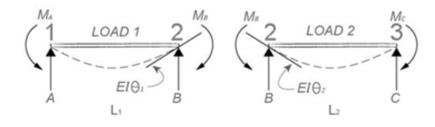
**Three-Moment Theorem** 

- Any number of spans
- Symmetric or non-symmetric

Procedure:

- Draw a free body diagram of the first two spans.
- Label the spans L1 and L2 and the supports (or free end) A, B and C as show.
- Use the Three-Moment equation to solve for each unknown moment, either as a value or as an equation.





$$M_{A}L_{1} + 2M_{B}(L_{1} + L_{2}) + M_{C}L_{2} = 6[EI\Theta_{1} + EI\Theta_{2}]$$

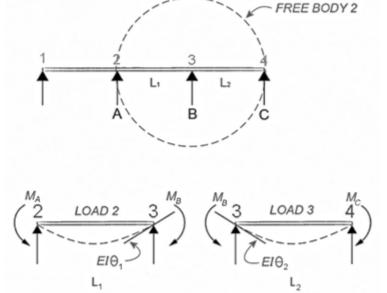


### Continuous beams

Three-Moment Theorem

Procedure (continued):

- 4. Move one span further and repeat the procedure.
- In a 3 span beam, the mid-moment from step 3 above (B), can now be solved using the two equations from step 4 and 3 together, by writing 2 equations with 2 unknowns.
- 6. Repeat as needed, always moving one span to the right and writing a new set of moment equations.
- Solve 2 simultaneous equations for 3 spans, or 3 equations for more than 3 spans, to get the interior moments.
- Once all interior moments are known, solve for reactions using free body diagrams of individual spans.
- Draw shear and moment diagrams as usual. This will also serve as a check for the moment values.



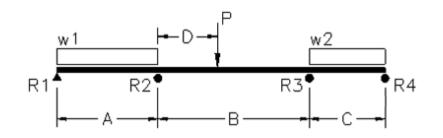


$$M_{A}L_{1} + 2M_{B}(L_{1} + L_{2}) + M_{C}L_{2} = 6[EI\Theta_{1} + EI\Theta_{2}]$$

#### 7. Three Moment Theorem

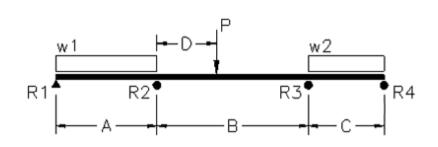
Use the Three Moment Theorem to determine all reactions and support moments for the given continuous beam.

DATASET: 1 -23-	
Span A	28 FT
Span B	21 FT
Span C	24 FT
Uniform load on span A, w1	4 KLF
Uniform load on span C, w2	5 KLF
Point load on span b, P	60 K
Distance to point load P from R2, D	14 FT

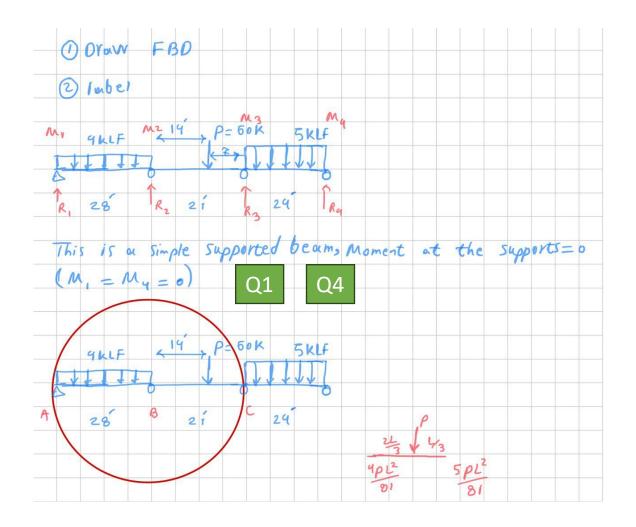




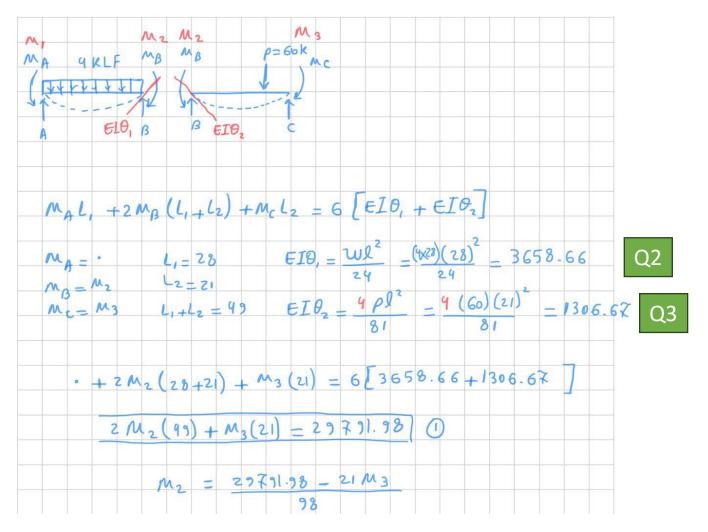
<u>#</u>	Question	Your Response
1	Moment at support R1, M1 (- if tension on top)	K-FT
2	El Theta on left side of R2	
3	EI Theta on right side of R2	
4	Moment at support R4, M4 (- if tension on top)	K-FT
5	El Theta on left side of R3	
6	EI Theta on right side of R3	
7	Moment at support R2, M2 (- if tension on top)	K-FT
8	Moment at support R3, M3 (- if tension on top)	K-FT
9	Support reaction, R1 (- if downward)	K
10	Support reaction, R2 (- if downward)	K
11	Support reaction, R3 (- if downward)	K
12	Support reaction, R4 (- if downward)	K



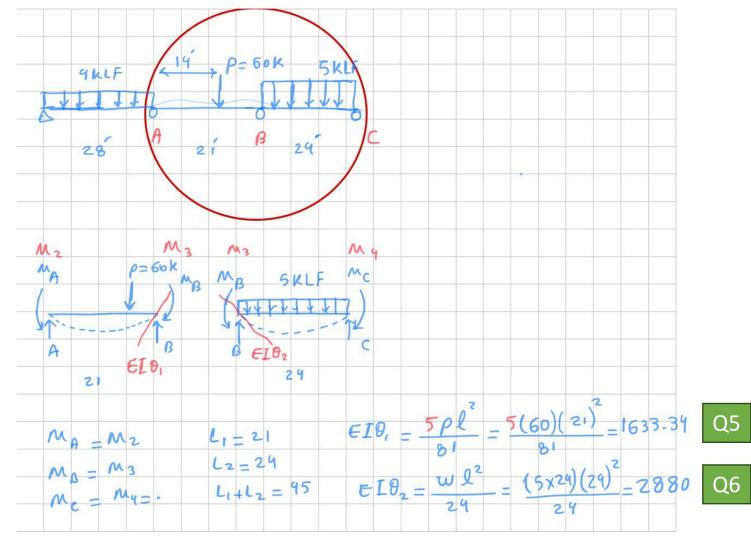




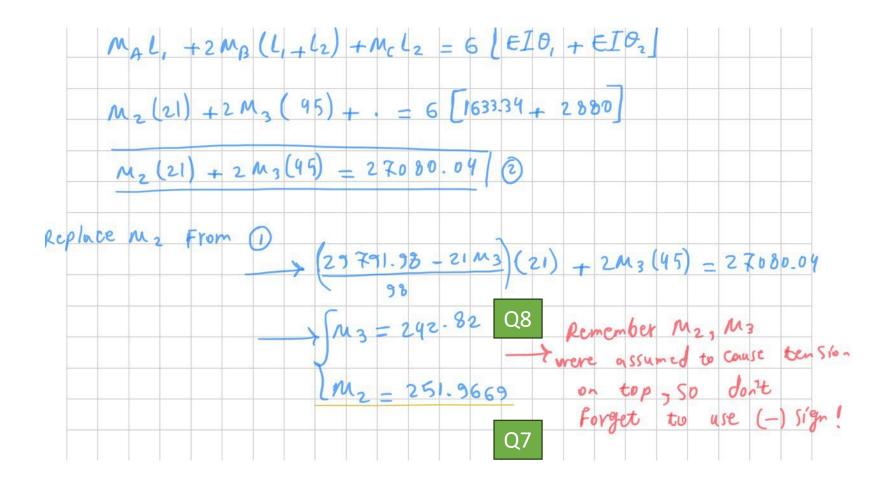




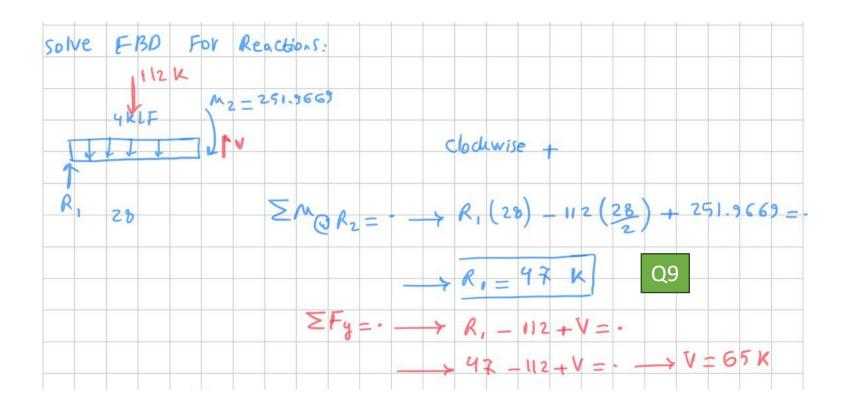




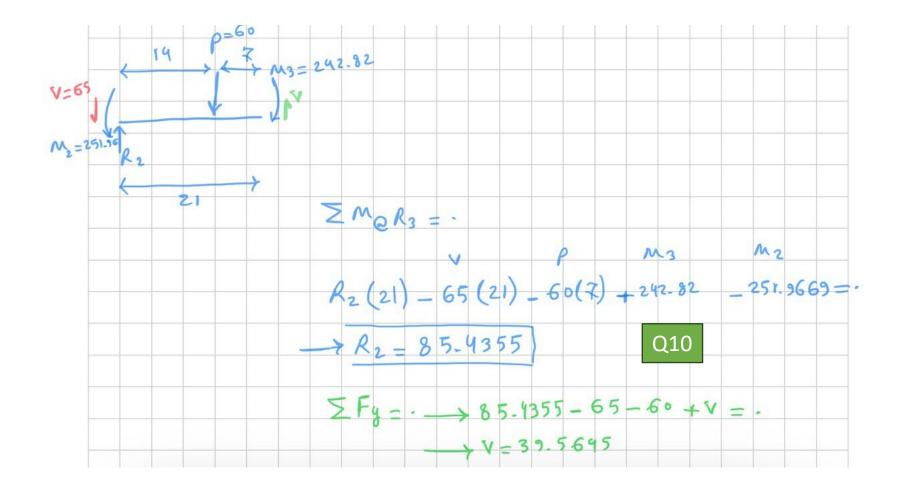




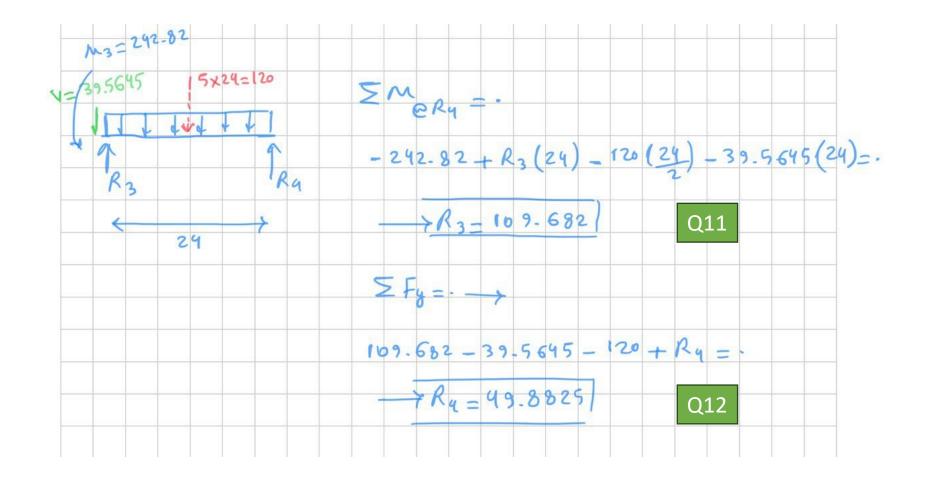






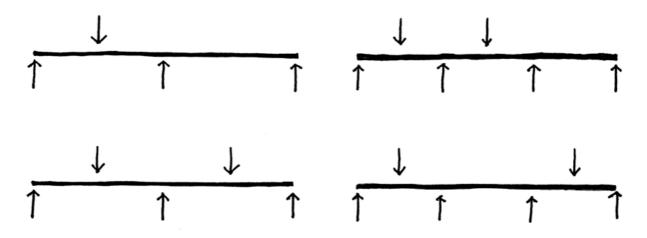








### Lab : Continuous Beams



#### Description

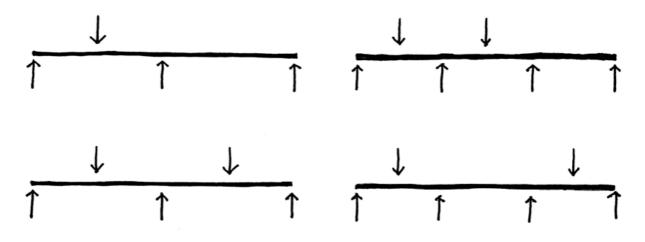
This project uses observation to understand the behavior of beams continuous over multiple supports.

#### Goals

To observe the behavior of continuous beams under different loadings To estimate locations of contraflexure and effective lengths To determine areas of positive and negative moment based on curvature



### Lab : Continuous Beams



#### Procedure

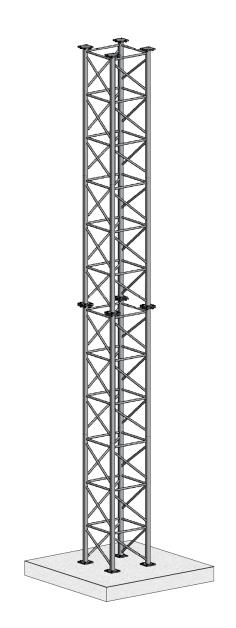
- Using the 24 inch stick, position the supports and loads (with your finger) as shown in the diagrams below. Hold the beam down on the reactions if it lifts up.
- 2. For each case observe and draw the elastic curve.
- 3. Label + and curvature (moment) and points of contraflexure.
- 4. Estimate the effective lengths,  $\ell_e$ , across the beam. (between points of M=0)

Link to Prof. von Buelow's description of this lab.



Due date for the submission of **revision** of the Preliminary report is March 19

Tower Test : March 24





Arch324: STRUCTURES II

# Thank you.

# Any question?

Please feel free to ask questions.



Contact: