

A green triangle is plotted on a coordinate plane. The vertices are located at $(-10, 0)$, $(-10, 10)$, and $(0, 0)$. The triangle is shaded green.

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Recitation



1. Wood Beam Analysis

Analyze the given 4x dimensioned lumber beam to determine if it passes or fails the NDS code criteria. The beam carries both dead and live floor load plus its own selfweight. Check the actual shear and bending stresses against the factored allowable stresses including all applicable factors from the NDS. Load duration is based on the live load ($CD = 1.0$). Assume normal temperature, and no incising ($C_t = C_i = 1.0$). Find the beam selfweight including the given moisture content. The beam is braced at the ends and the C.L. (meets criteria in 4.4.1) so $CL = 1.0$.

DATASET: 1

-2-

-3-

Wood Species

EASTERN
SOFTWOODS

Wood Grade

Select
Structural

Span A

20 FT

Span B

14 FT

Nominal Depth of Beam, d

12 IN

Moisture Content, m.c.

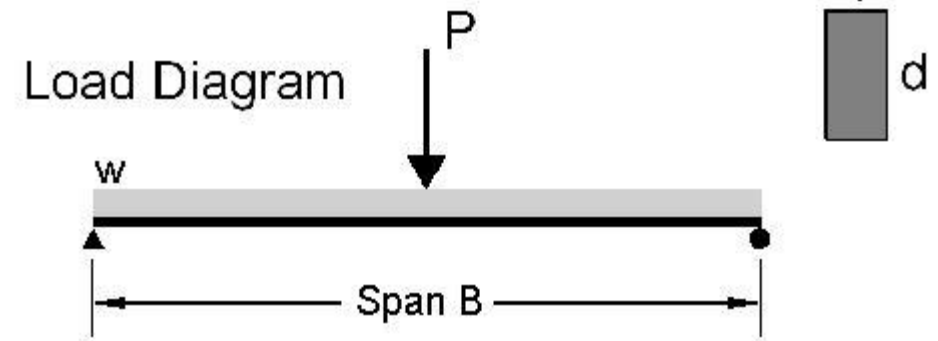
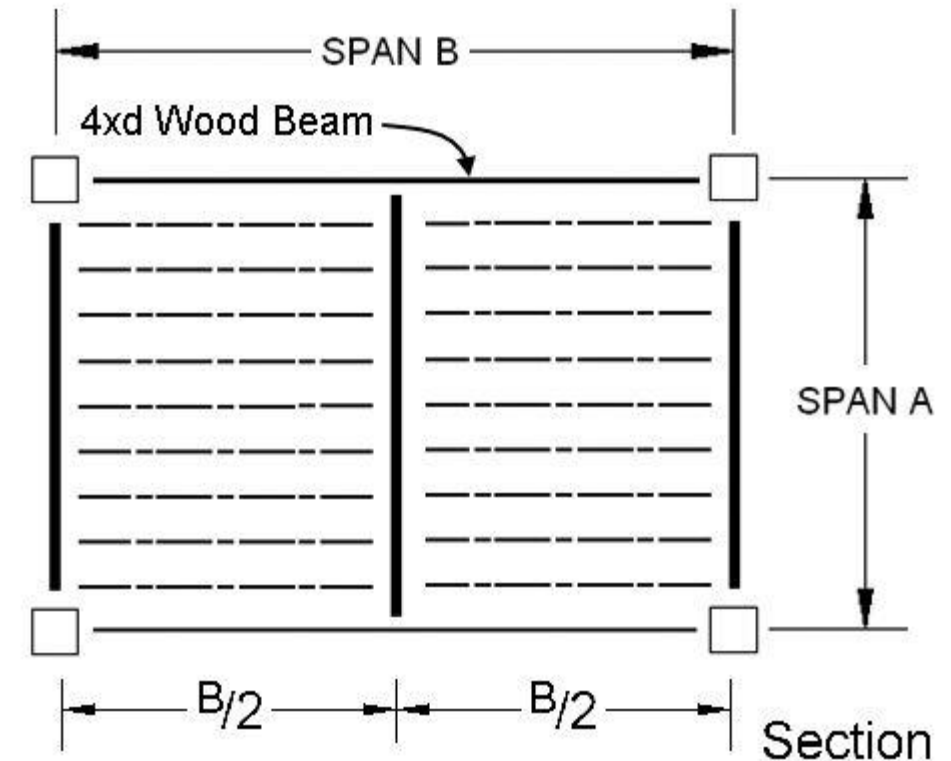
12 %

Floor DL

7 PSF

Floor LL

40 PSF



**Table 4A
(Cont.)**

**Reference Design Values for Visually Graded Dimension Lumber
(2" - 4" thick)^{1,2,3}**

(All species except Southern Pine — see Table 4B) (Tabulated design values are for normal load duration and dry service conditions. See NDS 4.3 for a comprehensive description of design value adjustment factors.)

USE WITH TABLE 4A ADJUSTMENT FACTORS

Species and commercial grade	Size classification	Design values in pounds per square inch (psi)							Specific Gravity ⁴ G	Grading Rules Agency
		Bending F _b	Tension parallel to grain F _t	Shear parallel to grain F _v	Compression perpendicular to grain F _{c⊥}	Compression parallel to grain F _c	Modulus of Elasticity			
							E	E _{min}		
EASTERN SOFTWOODS										
Select Structural		1,250	575	140	335	1,200	1,200,000	440,000	0.36	NELMA
No. 1	2" & wider	775	350	140	335	1,000	1,100,000	400,000		
No. 2		575	275	140	335	825	1,100,000	400,000		
No. 3		350	150	140	335	475	900,000	330,000		
Stud	2" & wider	450	200	140	335	525	900,000	330,000		
Construction	2" - 4" wide	675	300	140	335	1,050	1,000,000	370,000		
Standard		375	175	140	335	850	900,000	330,000		
Utility		175	75	140	335	550	800,000	290,000		

Wood type: Eastern softwoods
Wood grade: structural



F_b=1250
F_v=140
G=0.36

The following formula shall be used to determine the density in lbs/ft³ of wood:

$$\text{density} = 62.4 \left[\frac{G}{1 + G(0.009)(\text{m.c.})} \right] \left[1 + \frac{\text{m.c.}}{100} \right]$$

where:

G = specific gravity of wood

m.c. = moisture content of wood, %

$$\text{density} = 62.4 \left[\frac{0.36}{1 + 0.36(0.009)(12)} \right] \left[1 + \frac{12}{100} \right]$$

$$= 24,21 \text{ PCF}$$

BEAM
SELF
WEIGHT

Density weight

25 6,836

24,21 n

n = 6,619

Table 1B Section Properties of Standard Dressed (S4S) Sawn Lumber

Nominal Size b x d	Standard Dressed Size (S4S) b x d in. x in.	Area of Section A in. ²	X-X AXIS		Y-Y AXIS		Approximate weight in pounds per linear foot (lbs/ft) of piece when density of wood equals:					
			Section Modulus S _{xx} in. ³	Moment of Inertia I _{xx} in. ⁴	Section Modulus S _{yy} in. ³	Moment of Inertia I _{yy} in. ⁴	25 lbs/ft ³	30 lbs/ft ³	35 lbs/ft ³	40 lbs/ft ³	45 lbs/ft ³	50 lbs/ft ³
2 x 3	1-1/2 x 2-1/2	3.750	1.56	1.953	0.938	0.703	0.651	0.781	0.911	1.042	1.172	1.302
2 x 4	1-1/2 x 3-1/2	5.250	3.06	5.359	1.313	0.984	0.911	1.094	1.276	1.458	1.641	1.823
2 x 5	1-1/2 x 4-1/2	6.750	5.06	11.39	1.688	1.266	1.172	1.406	1.641	1.875	2.109	2.344
2 x 6	1-1/2 x 5-1/2	8.250	7.56	20.80	2.063	1.547	1.432	1.719	2.005	2.292	2.578	2.865
2 x 8	1-1/2 x 7-1/4	10.88	13.14	47.63	2.719	2.039	1.888	2.266	2.643	3.021	3.398	3.776
2 x 10	1-1/2 x 9-1/4	13.88	21.39	98.93	3.469	2.602	2.409	2.891	3.372	3.854	4.336	4.818
2 x 12	1-1/2 x 11-1/4	16.88	31.64	178.0	4.219	3.164	2.930	3.516	4.102	4.688	5.273	5.859
2 x 14	1-1/2 x 13-1/4	19.88	43.89	290.8	4.969	3.727	3.451	4.141	4.831	5.521	6.211	6.901
3 x 4	2-1/2 x 3-1/2	8.75	5.10	8.932	3.646	4.557	1.519	1.823	2.127	2.431	2.734	3.038
3 x 5	2-1/2 x 4-1/2	11.25	8.44	18.98	4.688	5.859	1.953	2.344	2.734	3.125	3.516	3.906
3 x 6	2-1/2 x 5-1/2	13.75	12.60	34.66	5.729	7.161	2.387	2.865	3.342	3.819	4.297	4.774
3 x 8	2-1/2 x 7-1/4	18.13	21.90	79.39	7.552	9.440	3.147	3.776	4.405	5.035	5.664	6.293
3 x 10	2-1/2 x 9-1/4	23.13	35.65	164.9	9.635	12.04	4.015	4.818	5.621	6.424	7.227	8.030
3 x 12	2-1/2 x 11-1/4	28.13	52.73	296.6	11.72	14.65	4.883	5.859	6.836	7.813	8.789	9.766
3 x 14	2-1/2 x 13-1/4	33.13	73.15	484.6	13.80	17.25	5.751	6.901	8.051	9.201	10.35	11.50
3 x 16	2-1/2 x 15-1/4	38.13	96.90	738.9	15.89	19.86	6.619	7.943	9.266	10.59	11.91	13.24
4 x 4	3-1/2 x 3-1/2	12.25	7.15	12.51	7.146	12.51	2.127	2.552	2.977	3.403	3.828	4.253
4 x 5	3-1/2 x 4-1/2	15.75	11.81	26.58	9.188	16.08	2.734	3.281	3.828	4.375	4.922	5.469
4 x 6	3-1/2 x 5-1/2	19.25	17.65	48.53	11.23	19.65	3.342	4.010	4.679	5.347	6.016	6.684
4 x 8	3-1/2 x 7-1/4	25.38	30.66	111.1	14.80	25.90	4.405	5.286	6.168	7.049	7.930	8.811
4 x 10	3-1/2 x 9-1/4	32.38	49.91	230.8	18.89	33.05	5.621	6.745	7.869	8.993	10.12	11.24
4 x 12	3-1/2 x 11-1/4	39.38	73.83	415.3	22.97	40.20	6.836	8.203	9.570	10.94	12.30	13.67
4 x 14	3-1/2 x 13-1/4	46.38	102.41	678.5	27.05	47.34	8.051	9.661	11.27	12.88	14.49	16.10
4 x 16	3-1/2 x 15-1/4	53.38	135.66	1034	31.14	54.49	9.266	11.12	12.97	14.83	16.68	18.53

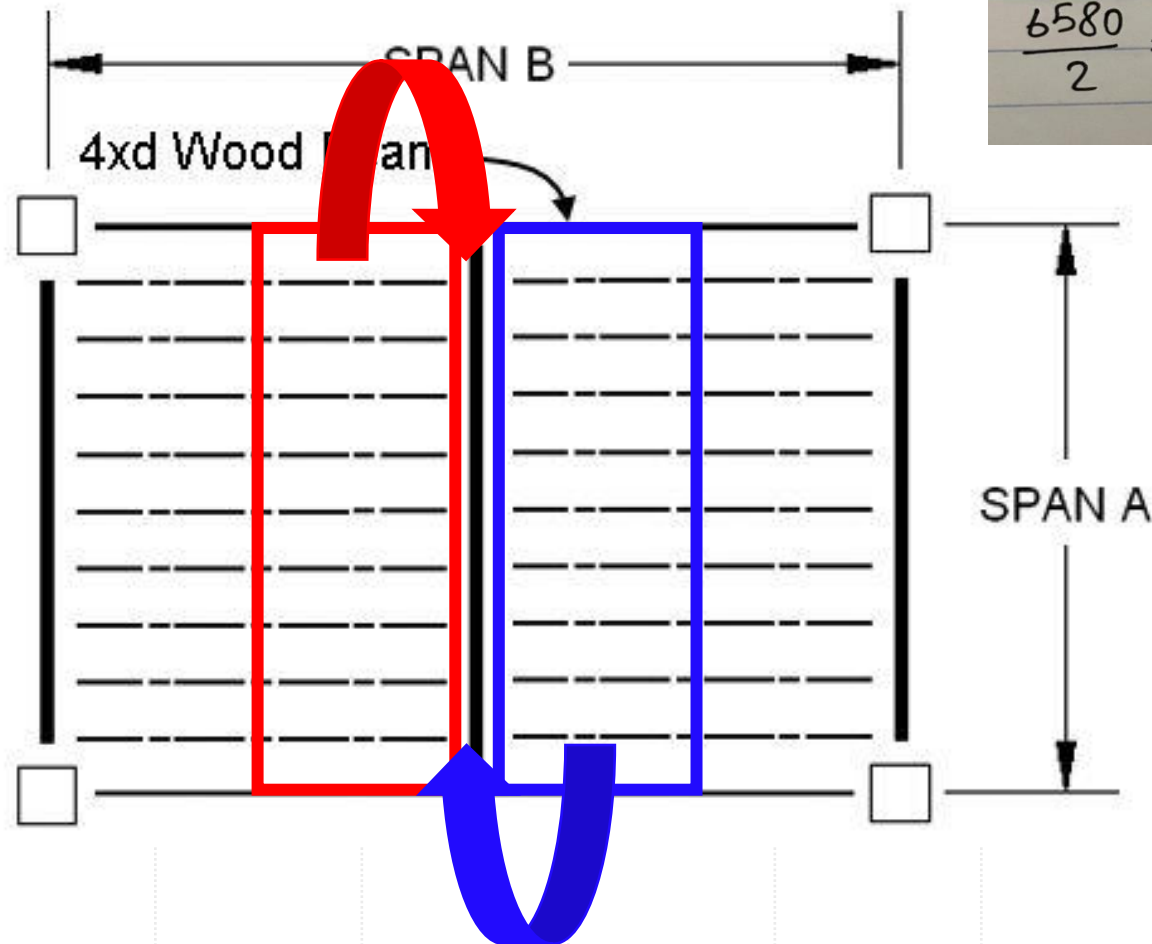
POINT
LOAD

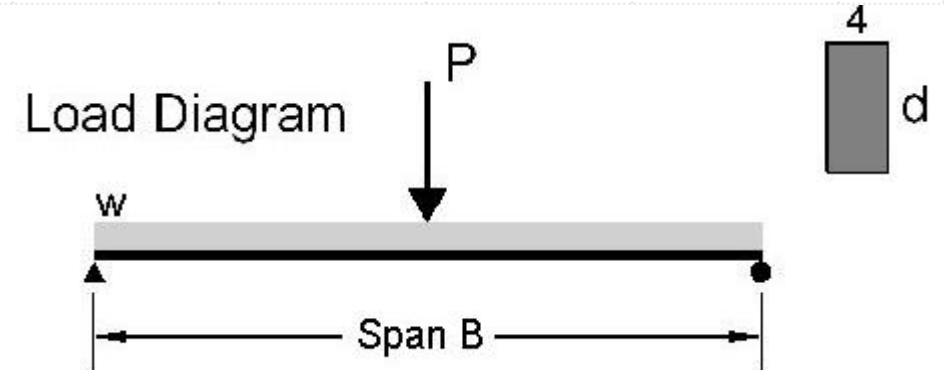
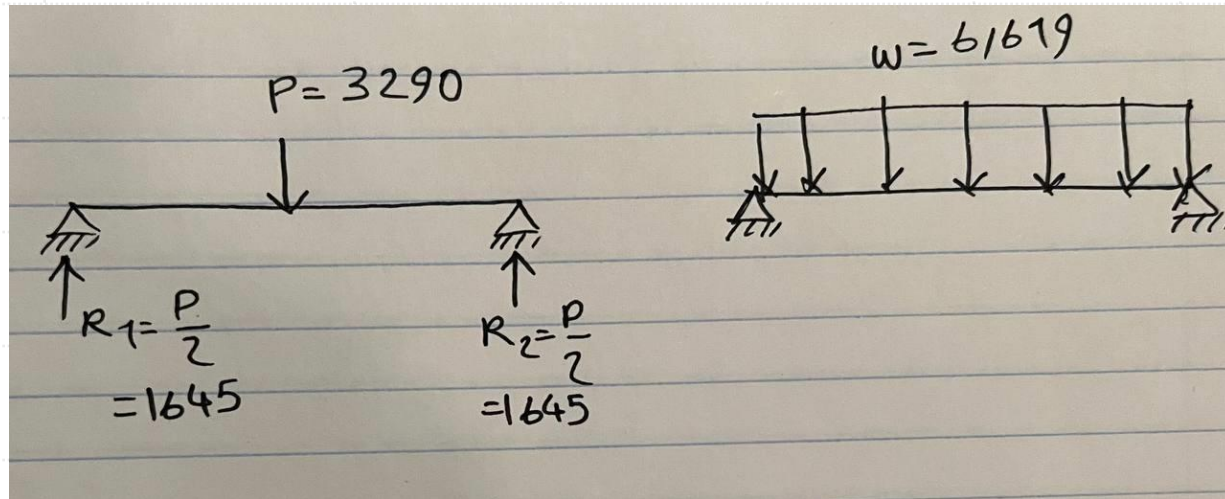
FLOOR DL: 7PSF
FLOOR LL: 40PSF
LOAD CASE=DL+LL

SPAN A: 20ft
SPAN B: 14ft

$$\left(\frac{B}{2} \times A\right) DL + \left(\frac{B}{2} \times A\right) LL$$
$$(7 \times 20)(7) + (7 \times 20)40$$
$$= 6580$$

$$\frac{6580}{2} = 3290 \text{ LBS}$$





$$V_{\max} = 1645 + \frac{61619 \times 14}{2} = 1691,33$$

$$M = \frac{PL}{4} + \frac{wl^2}{8} = 3290 \left(\frac{14}{4} \right) + \frac{61619 \times (14)^2}{8} = 11677,16$$

Size Factors, C_F

		F _b		F _t	F _c
Grades	Width (depth)	Thickness (breadth)			
		2" & 3"	4"		
Select Structural, No.1 & Btr, No.1, No.2, No.3	2", 3", & 4"	1.5	1.5	1.5	1.15
	5"	1.4	1.4	1.4	1.1
	6"	1.3	1.3	1.3	1.1
	8"	1.2	1.3	1.2	1.05
	10"	1.1	1.2	1.1	1.0
	12"	1.0	1.1	1.0	1.0
	14" & wider	0.9	1.0	0.9	0.9
Stud	2", 3", & 4"	1.1	1.1	1.1	1.05
	5" & 6"	1.0	1.0	1.0	1.0
	8" & wider	Use No.3 Grade tabulated design values and size factors			
Construction, Standard	2", 3", & 4"	1.0	1.0	1.0	1.0
Utility	4"	1.0	1.0	1.0	1.0
	2" & 3"	0.4	—	0.4	0.6

Actual bending and actual shear

$$f_b = \frac{M}{S} = \frac{11677,16 \times 12}{73,83} = 1897,95$$

Based on Table 1B

$$f_v = 1,5 \frac{V}{A} = 1,5 \frac{1691,33}{39,38} = 63,45$$

Based on Table 1B

Wet service factor

Wet Service Factors, C_M

F_b	F_t	F_v	F_{cl}	F_c	E and E_{min}
1.00	1.00	1.00	0.67	0.91	1.00

Allow bending + shear

$$F'_b = C_D \cdot C_M \cdot C_t \cdot C_L \cdot C_F \cdot C_{fu} \cdot C_i \cdot C_r \cdot F_b =$$
$$1 \times 1 \times 1 \times 1 \times 1 \times 1 \times 1 \times 1 \times 1250 =$$
$$1250 \times 1,1 = 1375$$

$$F'_v = C_D \cdot C_M \cdot C_t \cdot C_i \times F_v = 140$$

$$1897,95$$
$$F_b > F'_b \rightarrow 1375$$
$$F_v < F'_v \rightarrow 140$$
$$\downarrow$$
$$63,45$$

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- Thanks for your attention 😊